

Flat Passband Gain Design Algorithm for 2nd-order RC Polyphase Filter

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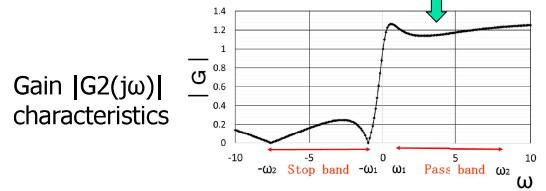
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Need for Flat Passband Gain Algorithm of 2nd-order RC Polyphase Filter

Transfer Function

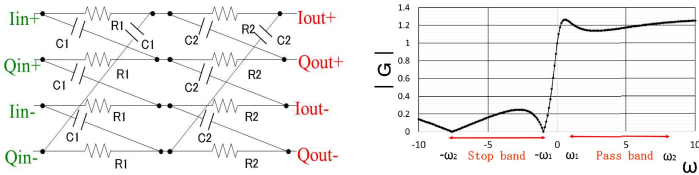
$$G_2(j\omega) = \frac{(1 + \omega R_1 C_1)(1 + \omega R_2 C_2)}{1 - \omega^2 R_1 C_1 R_2 C_2 + j\omega(C_1 R_1 + C_2 R_2 + 2R_1 C_2)}$$

We need flat passband gain



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Four Design Parameters



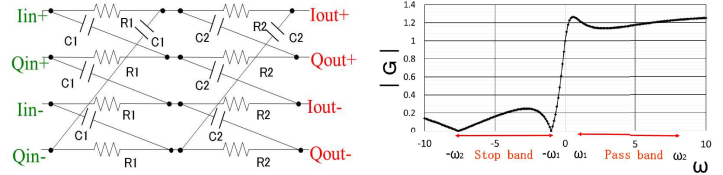
4 parameters : R_1, R_2, C_1, C_2

$$\omega_1 = \frac{1}{R_1 C_1}, \omega_2 = \frac{1}{R_2 C_2}, X = \frac{1}{R_2 C_1}, Y = \frac{1}{R_1 C_2}$$

4 constraints

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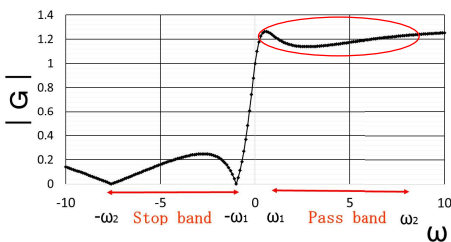
Two Constraints from Filter Spec.



- 2 zeros : $-\omega_1 = \frac{-1}{R_1 C_1}$, $-\omega_2 = \frac{-1}{R_2 C_2}$ are given from the filter specification.

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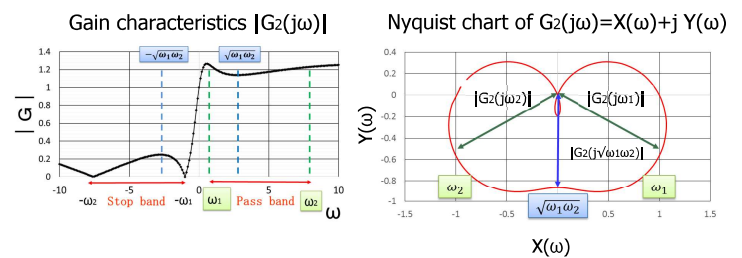
Proposed Algorithm Uses Third Constraint



- We use the third constraint $X = \frac{1}{R_2 C_1}$ for passband gain flattening.
- The fourth constraint is left for ease of IC realization.

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Nyquist Chart of $G_2(j\omega)$

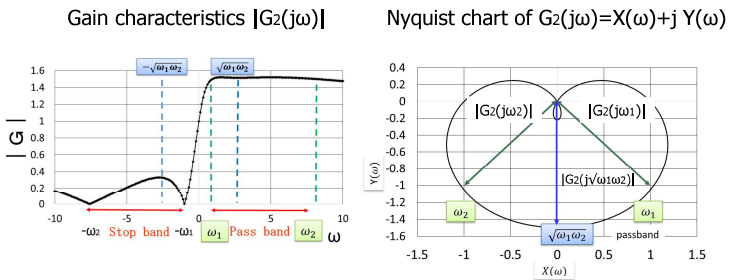


$$|G_2(j\omega_1)| = |G_2(j\omega_2)|$$

But in general $|G_2(j\omega_1)| = |G_2(j\omega_2)| \neq |G_2(j\sqrt{\omega_1\omega_2})|$

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Our Idea for Flat Passband Gain Algorithm



If we make $|G_2(j\omega_1)| = |G_2(j\omega_2)| = |G_2(j\sqrt{\omega_1\omega_2})|$, gain would be flat from ω_1 to ω_2 .

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Solving Third Constraint

Our algorithm

$$|G_2(j\omega_1)| = |G_2(j\omega_2)| = |G_2(j\sqrt{\omega_1\omega_2})|,$$



$$\alpha\omega_{21}^2 + \beta\omega_{21} + \gamma = 0 \quad \omega_{21} = \frac{1}{R_2C_1}$$

We need a positive real solution of ω_{21} .

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Condition for Solution

Third constraint

$$\omega_{21} = \frac{1}{R_2C_1} = \frac{-\beta + \sqrt{\beta^2 - 4\alpha\gamma}}{2\alpha}$$

$$\alpha = 6\omega_1^2 + 6\omega_2^2 + 4\omega_1\omega_2 - 8\sqrt{\omega_1\omega_2}(\omega_1 + \omega_2)$$

$$\beta = 6\omega_1^3 + 6\omega_2^3 + 10\omega_1\omega_2(\omega_1 + \omega_2) - 8\sqrt{\omega_1\omega_2}(\omega_1 + \omega_2)^2$$

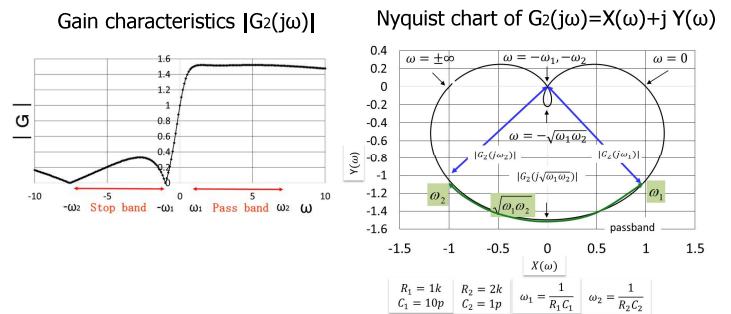
$$\gamma = \omega_1^4 + \omega_2^4 + 2\omega_1\omega_2(\omega_1^2 + \omega_2^2 + 5\omega_1\omega_2) - 4\sqrt{\omega_1\omega_2}(\omega_1^3 + \omega_1^2\omega_2 + \omega_1\omega_2^2)$$

For a positive real $\omega_{21} \Rightarrow 0.79142 < \frac{\omega_1}{\omega_2} < 12.63556$

This is obtained from numerical calculation.

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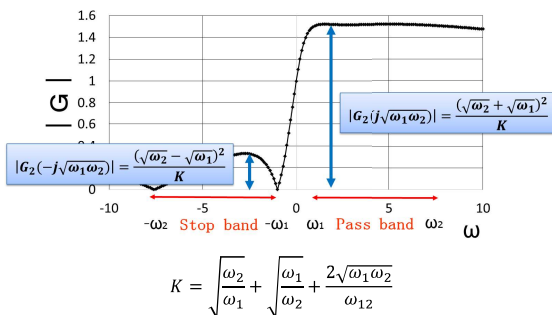
Numerical Simulation Result of Our Algorithm



Passband gain becomes flat.

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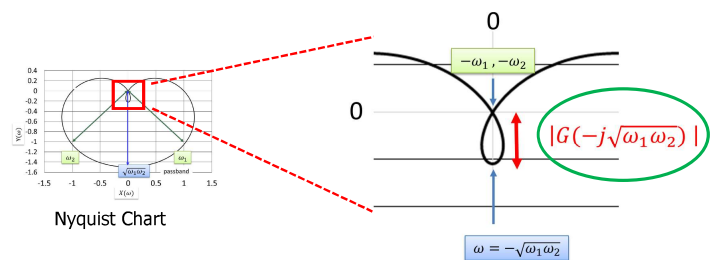
Image Rejection Ratio (IRR)



$$\bullet \text{Image Rejection Ratio} = \frac{\text{Passband Gain}}{(\text{Stopband Gain})_{\text{MAX}}} = \left(\frac{\sqrt{\omega_2} + \sqrt{\omega_1}}{\sqrt{\omega_2} - \sqrt{\omega_1}} \right)^2$$

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Nyquist Chart & Image Rejection Ratio



Nyquist chart visualizes image rejection ratio.

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