



$\Delta\Sigma$ Digital-to-Time Converter and its Application to SSCG*

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*SSCG : Spread Spectrum Clock Generator

Outline

I. Background

II. Principle

- i. PCM $\Delta\Sigma$ DTC Algorithm
- ii. PPM $\Delta\Sigma$ DTC Algorithm
- iii. PWM $\Delta\Sigma$ DTC Algorithm
- iv. PRJ $\Delta\Sigma$ DTC Algorithm
- v. Other Possible Algorithms

III. Analysis

IV. Result

V. Conclusion

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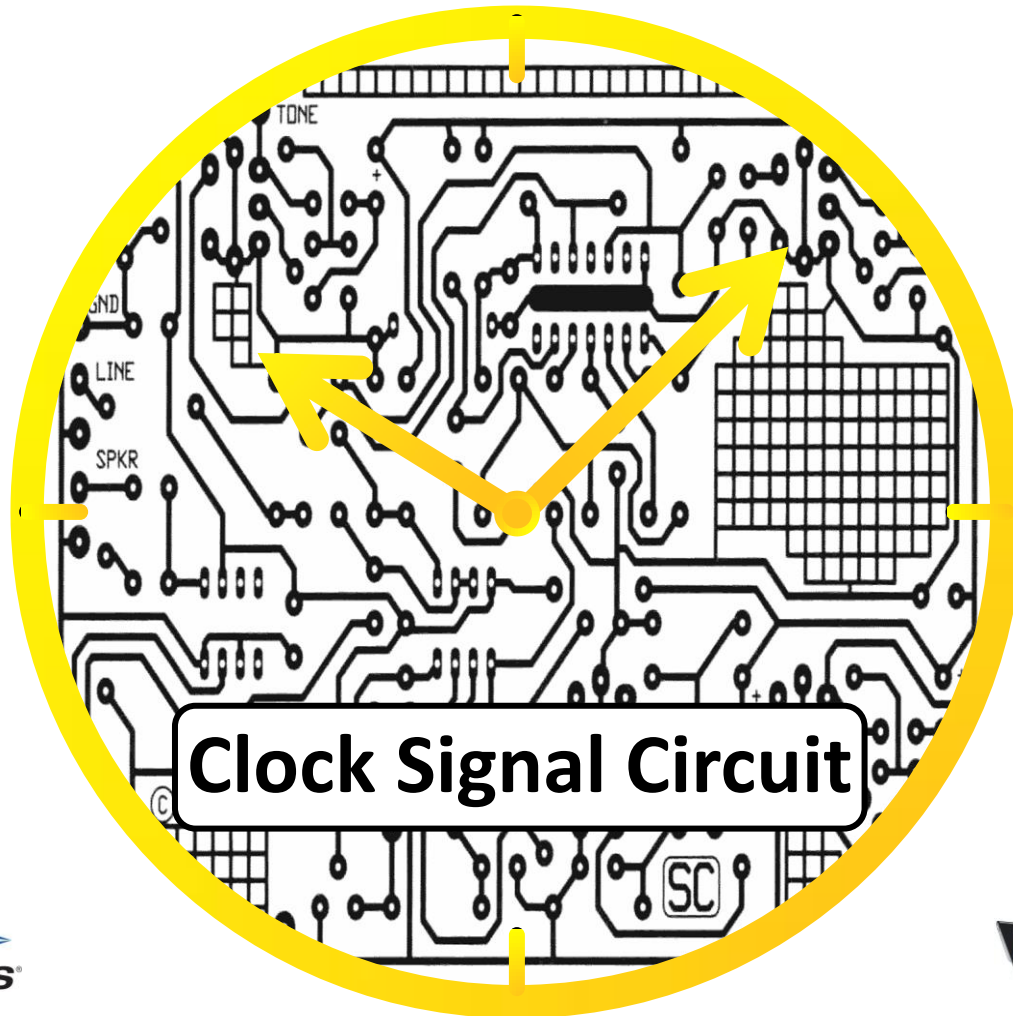
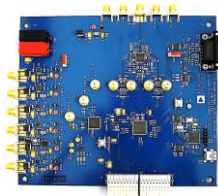
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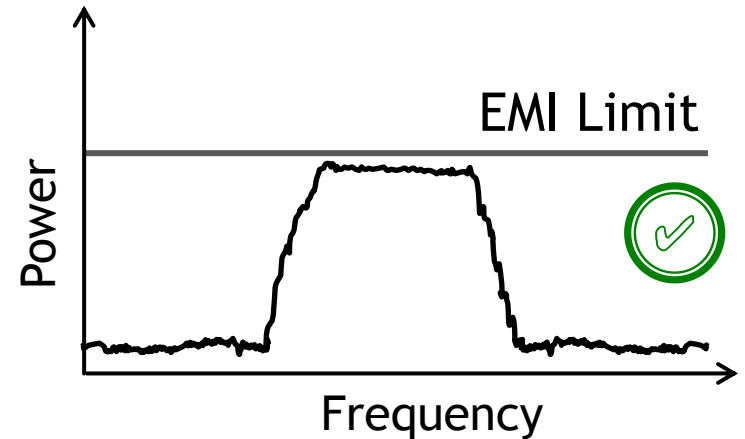
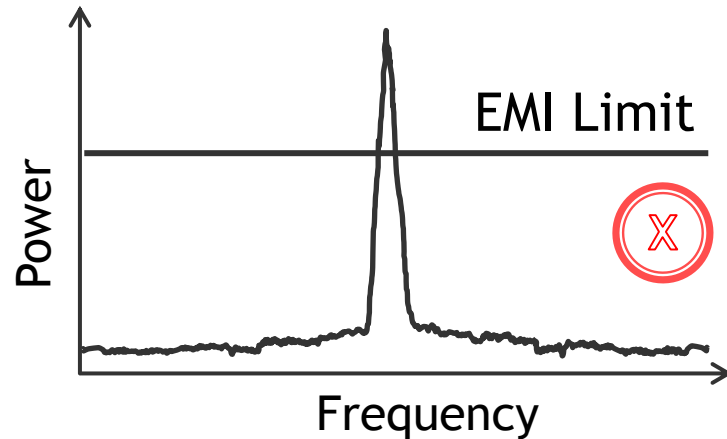
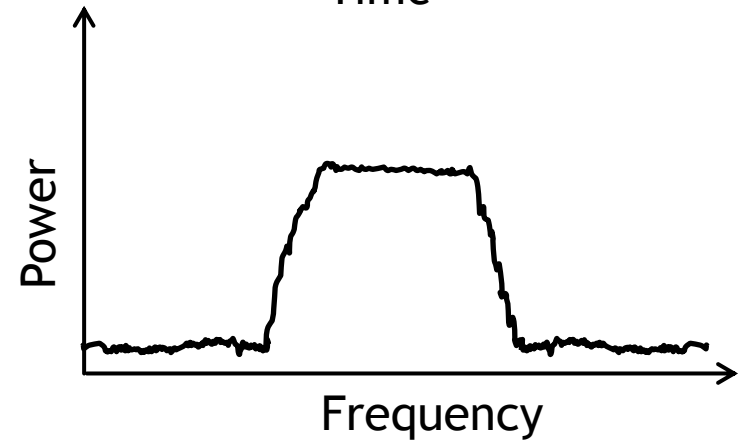
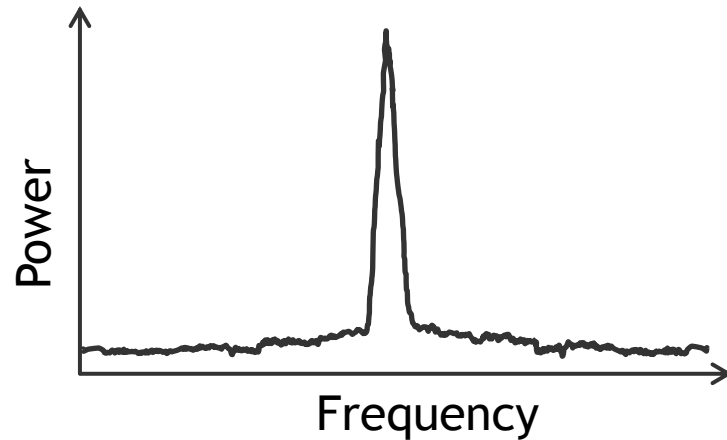
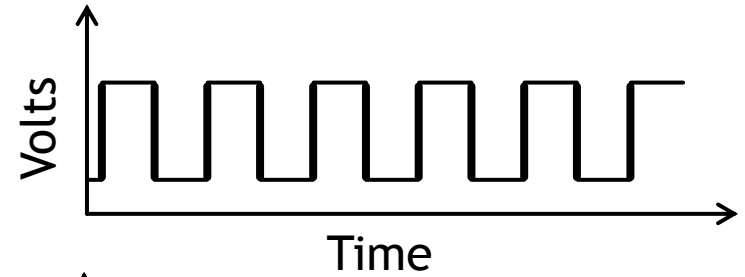
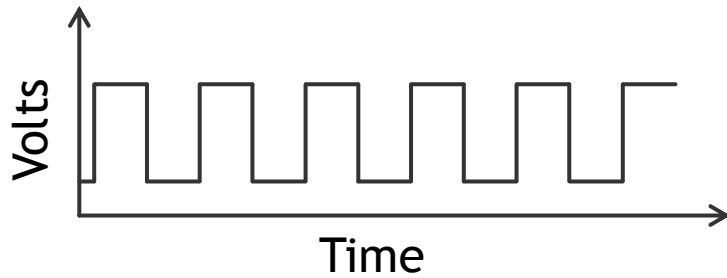
V. Conclusion

Common Object in All Electronic Devices

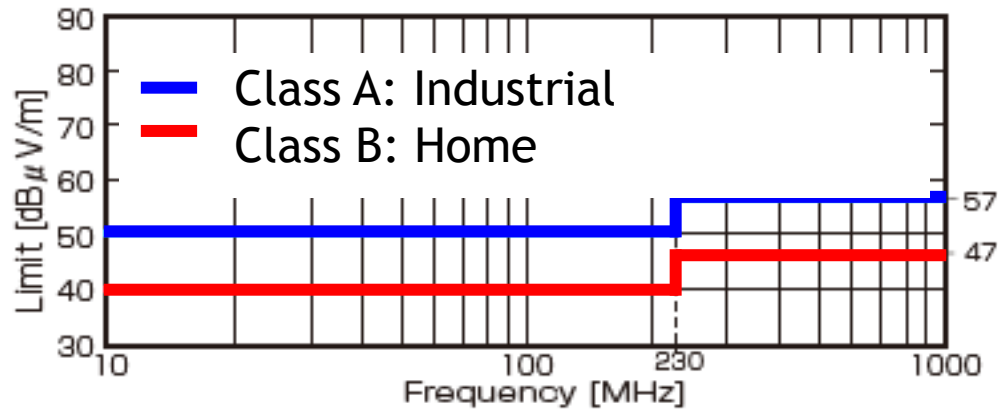


Clock is everywhere

Spread Spectrum Clock Technique



EMI Problem



EMI Regulation (CISPR22) in Japan

Ignoring is Dangerous



Lead to Malfunctioning of devices

Solving is difficult

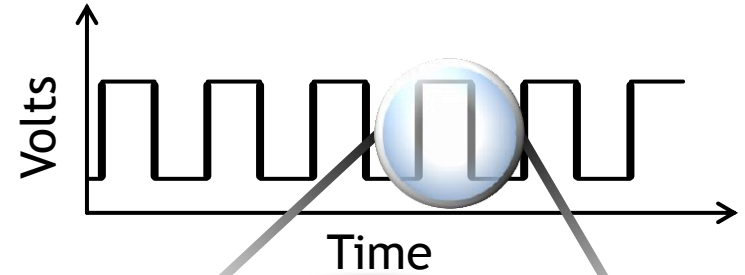
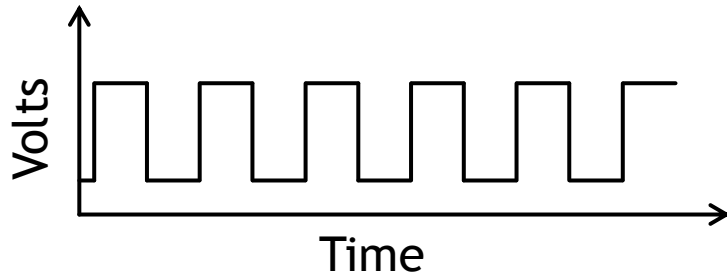


Time Consuming

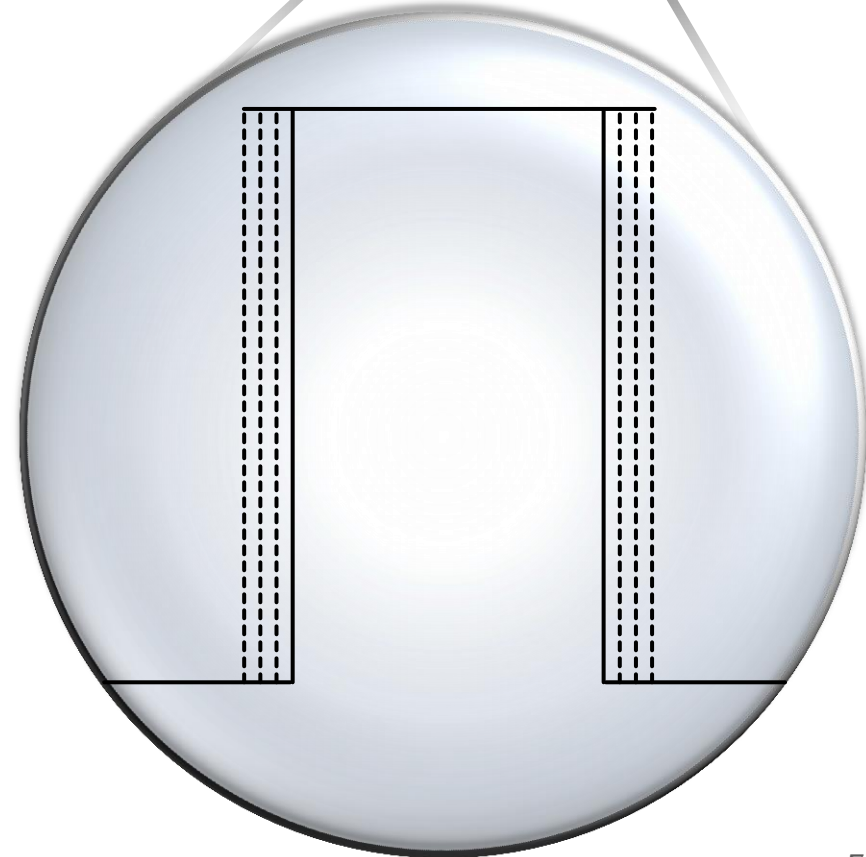


Costly

SSGC Approach

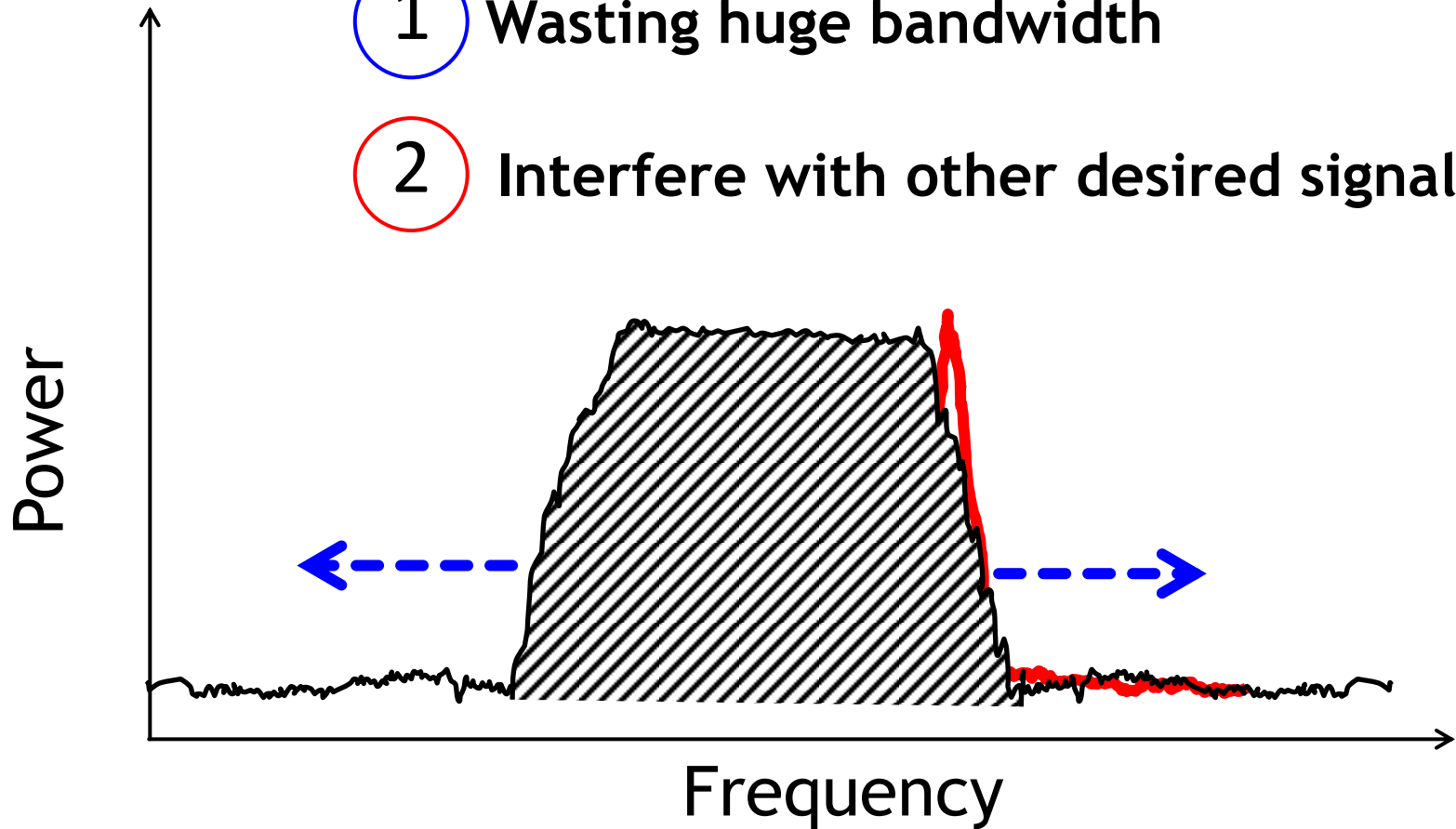


Solving Digital
Problem By
Analog
Approach



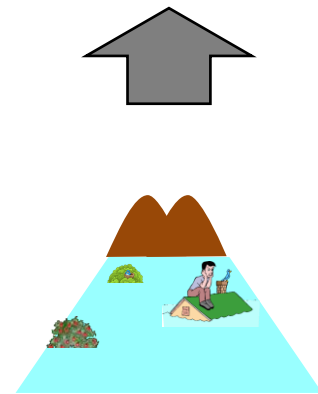
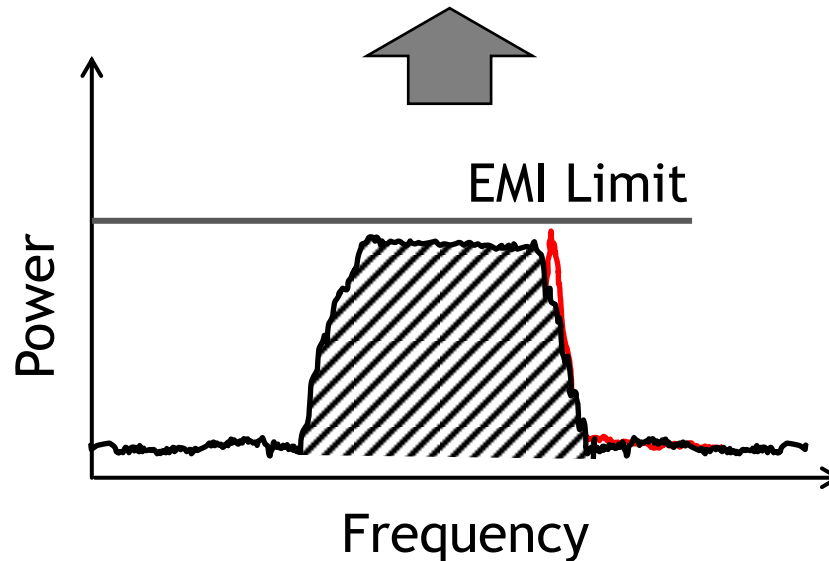
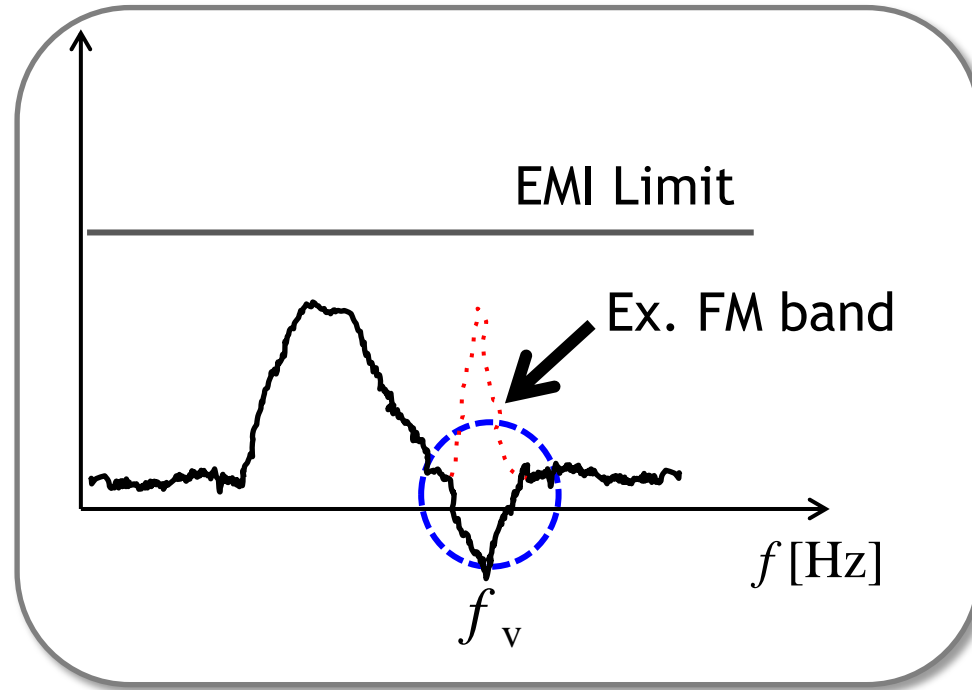
Conventional SSGC Problems

- 1 Wasting huge bandwidth
- 2 Interfere with other desired signals



Exclusive Noise Spectrum Selection

Our Target:



Goal

To compete with conventional methods,
Our method should be:

✓ **Simple**

✓ **Low cost**

✓ **Effective**

Converters Path

Devices miniaturization, speed, high frequency

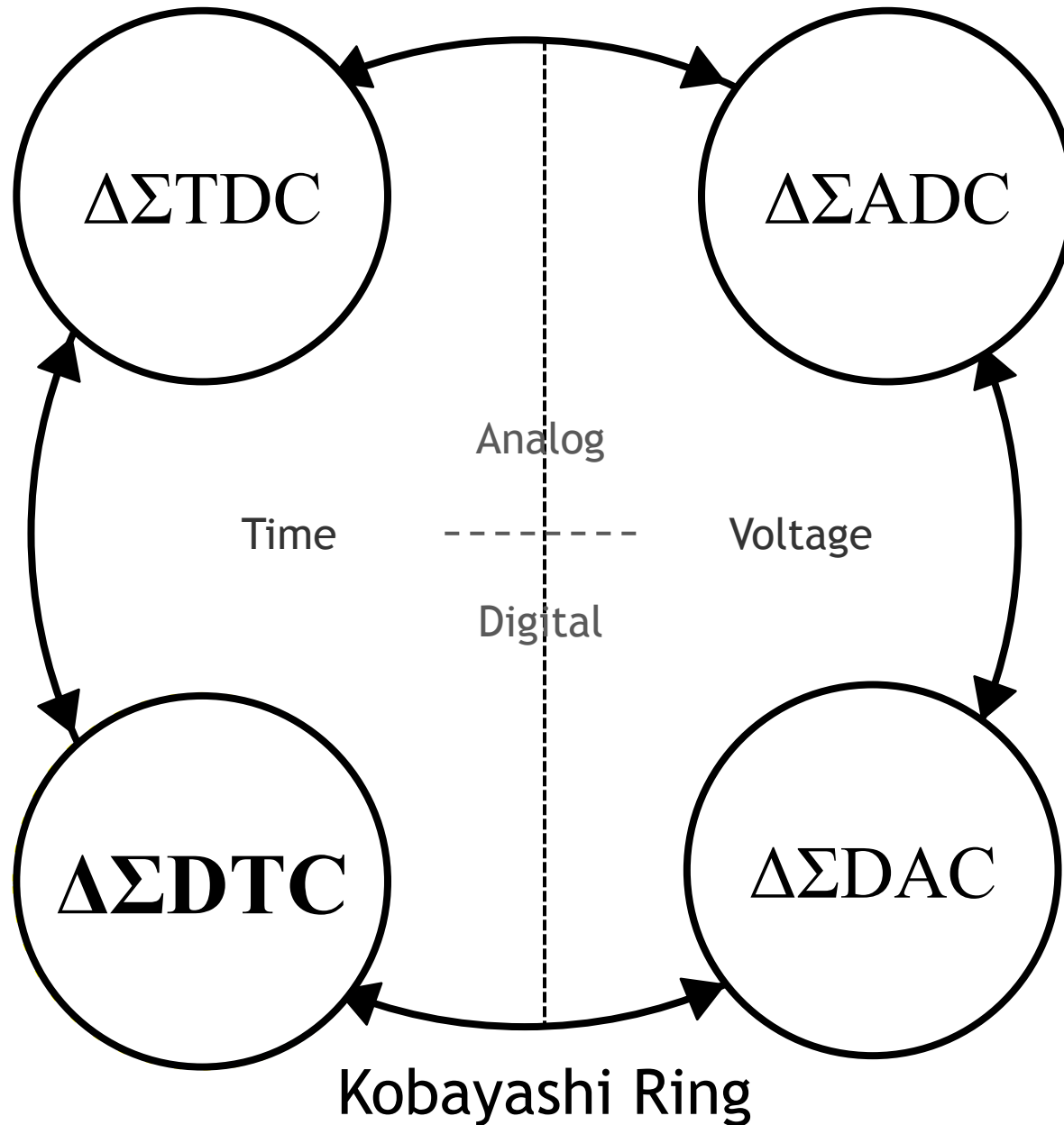
↳ Spreading $\Delta\Sigma$ oversampling Applications

↳ **Time domain signal processing**

↳ From $\Delta\Sigma$ ADC to $\Delta\Sigma$ TDC

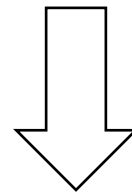
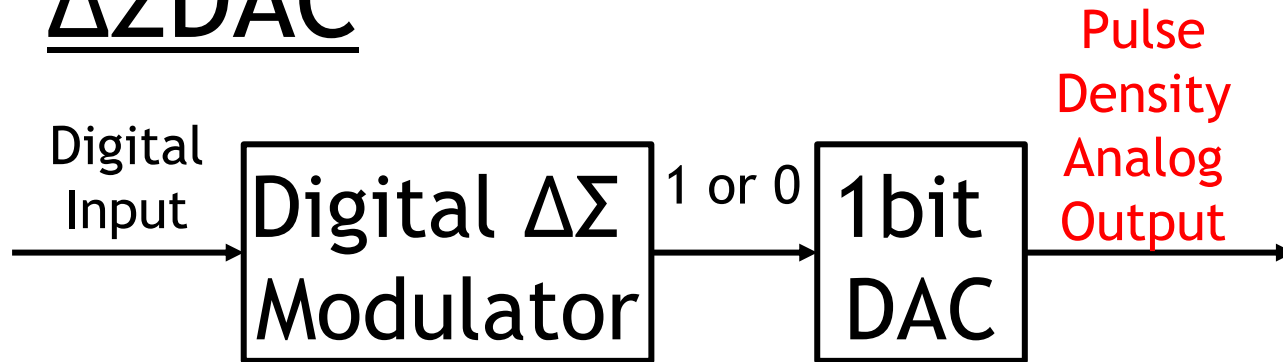
↳ From $\Delta\Sigma$ DAC to ???

Time Domain v.s. Voltage Domain



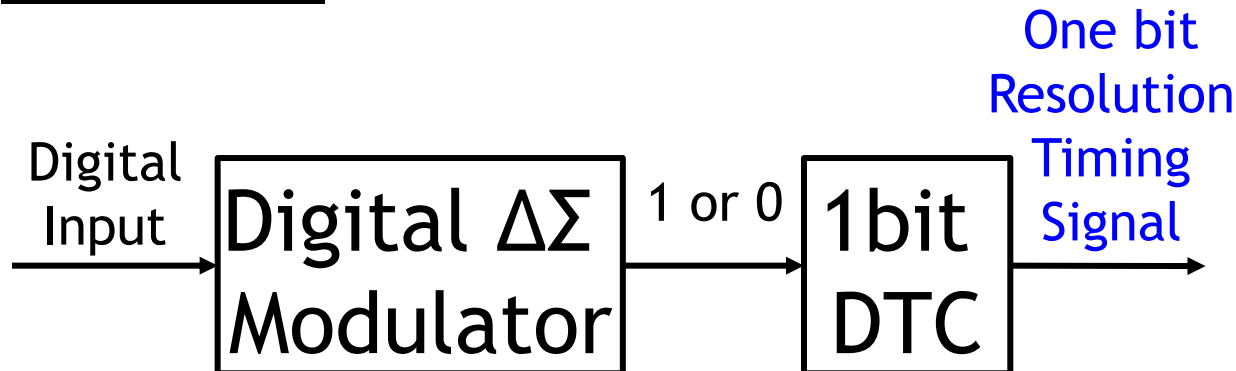
$\Delta\Sigma$ DAC & $\Delta\Sigma$ DTC Analogy

$\Delta\Sigma$ DAC



time domain

$\Delta\Sigma$ DTC



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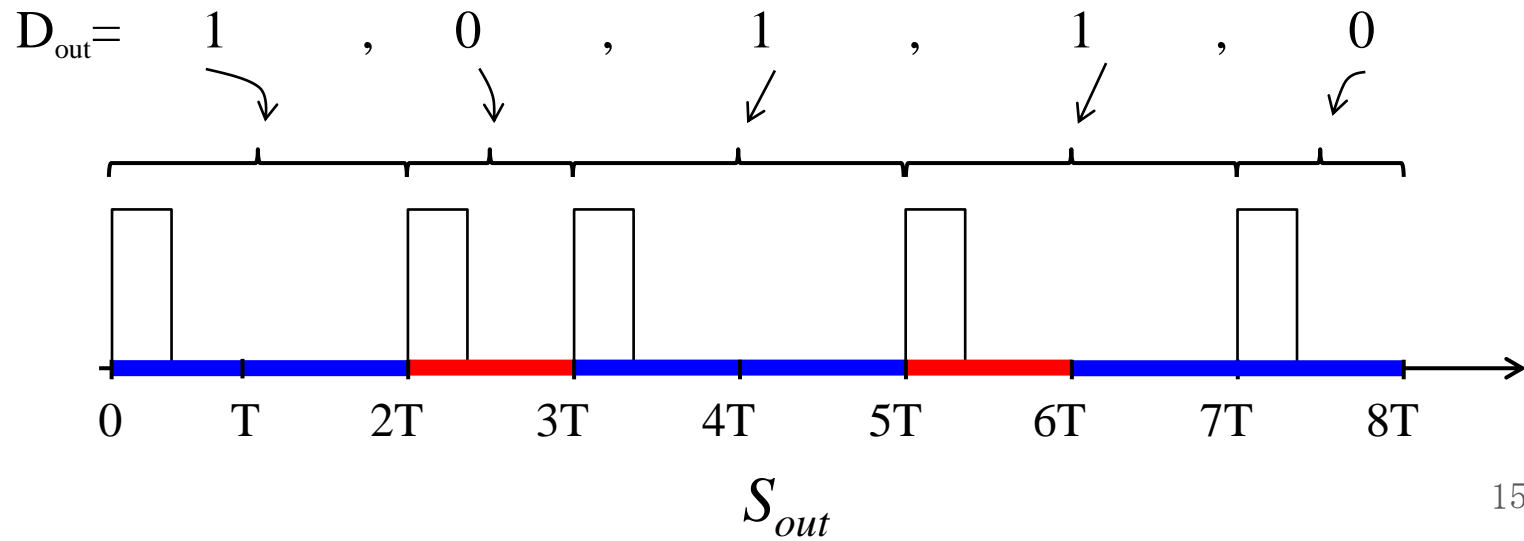
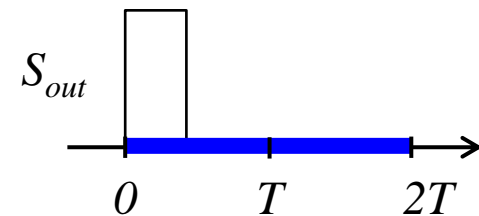
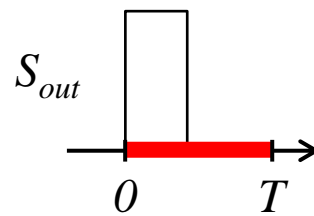
Pulse Cycle Modulation

■ Output Pulse Cycle Period = $f(D_{out})$

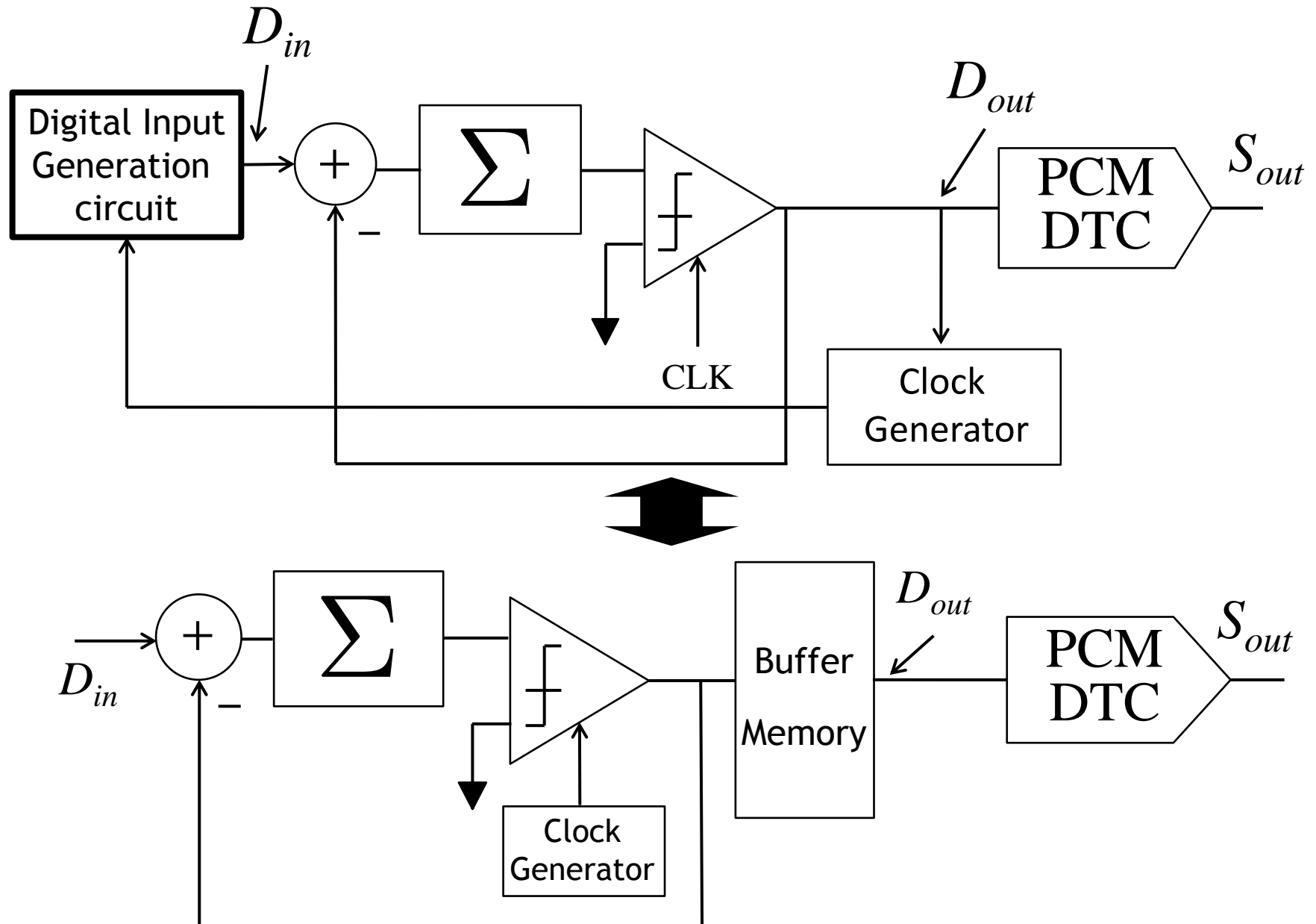
Exa. : ($D_{out} = 10110$)

$D_{out} = 0$

$D_{out} = 1$



PCMA Δ Σ DTC – Configuration



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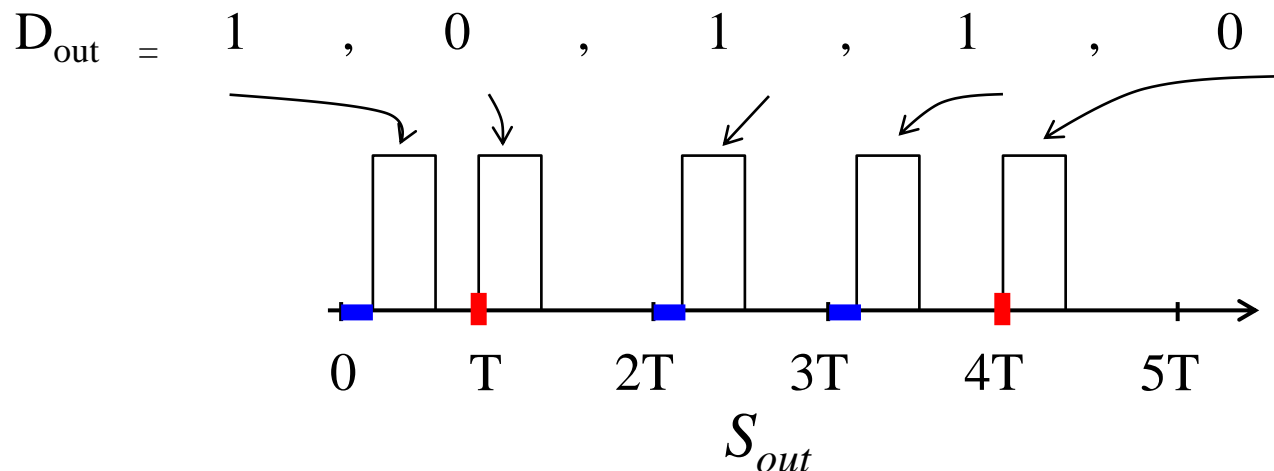
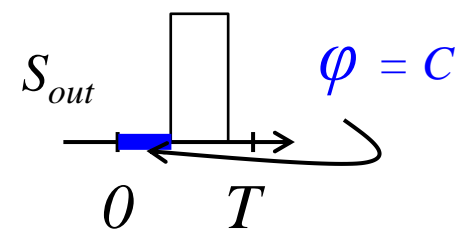
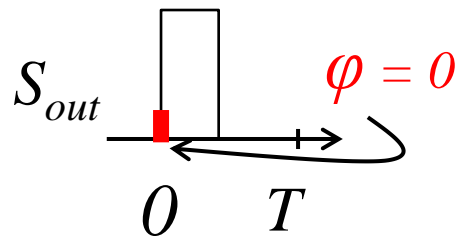
Pulse Position Modulation

■ Output pulse position (or phase) = $g(D_{out})$

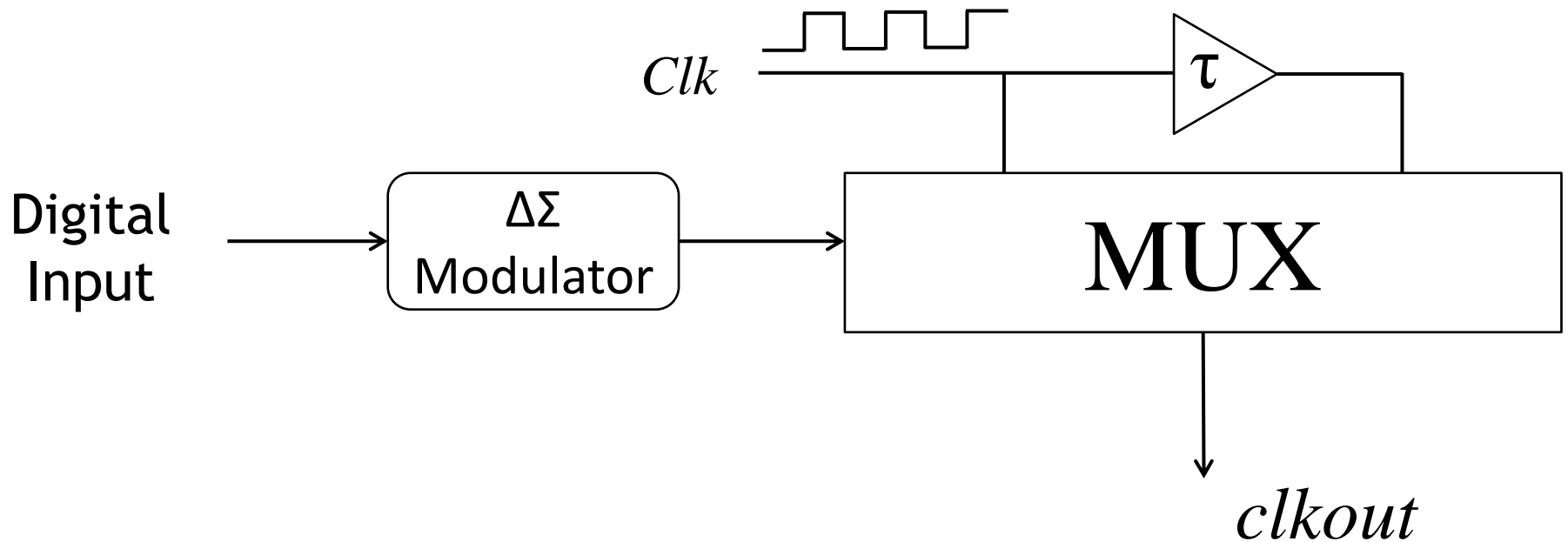
Ex. ($D=10110$)

$$D_{out} = 0$$

$$D_{out} = 1$$



PPMΔΣDTC - Configuration



High Frequency Clock

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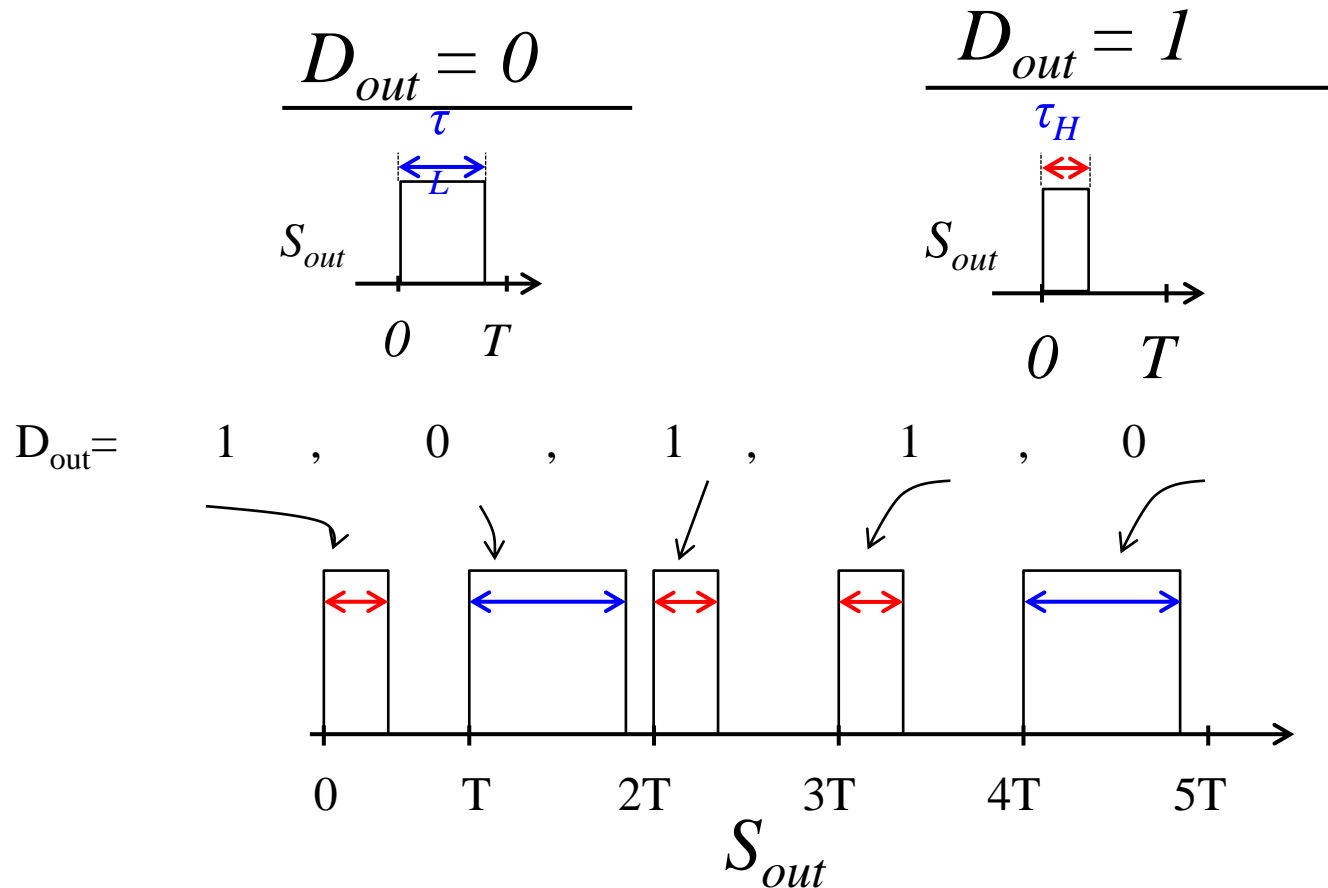
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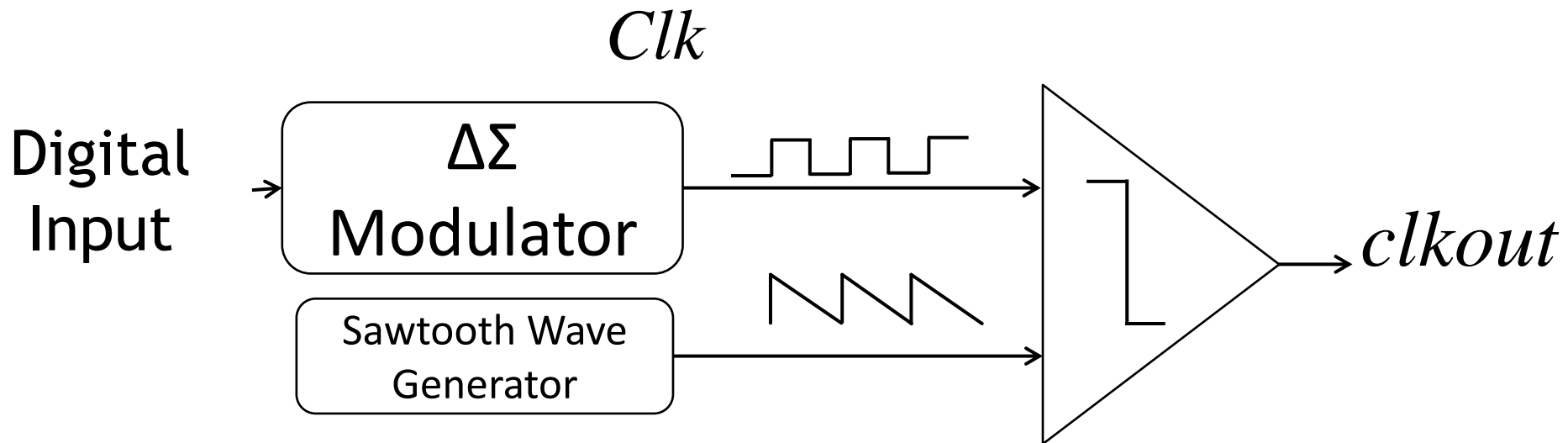
Pulse Width Modulation

■ Output pulse width = $h(D_{out})$

Exa. : ($D_{out} = 10110$)



PWM $\Delta\Sigma$ DTC - Configuration



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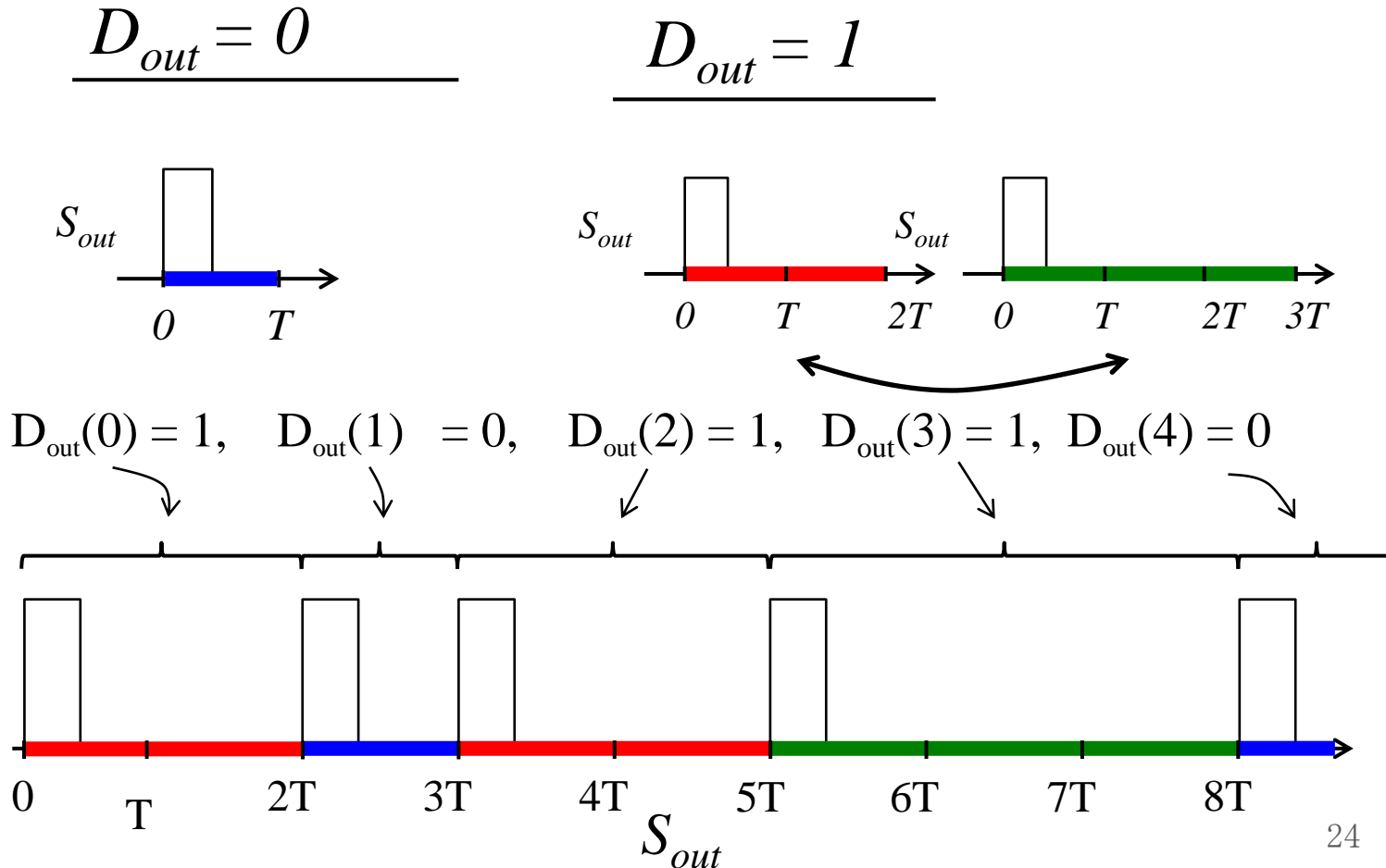
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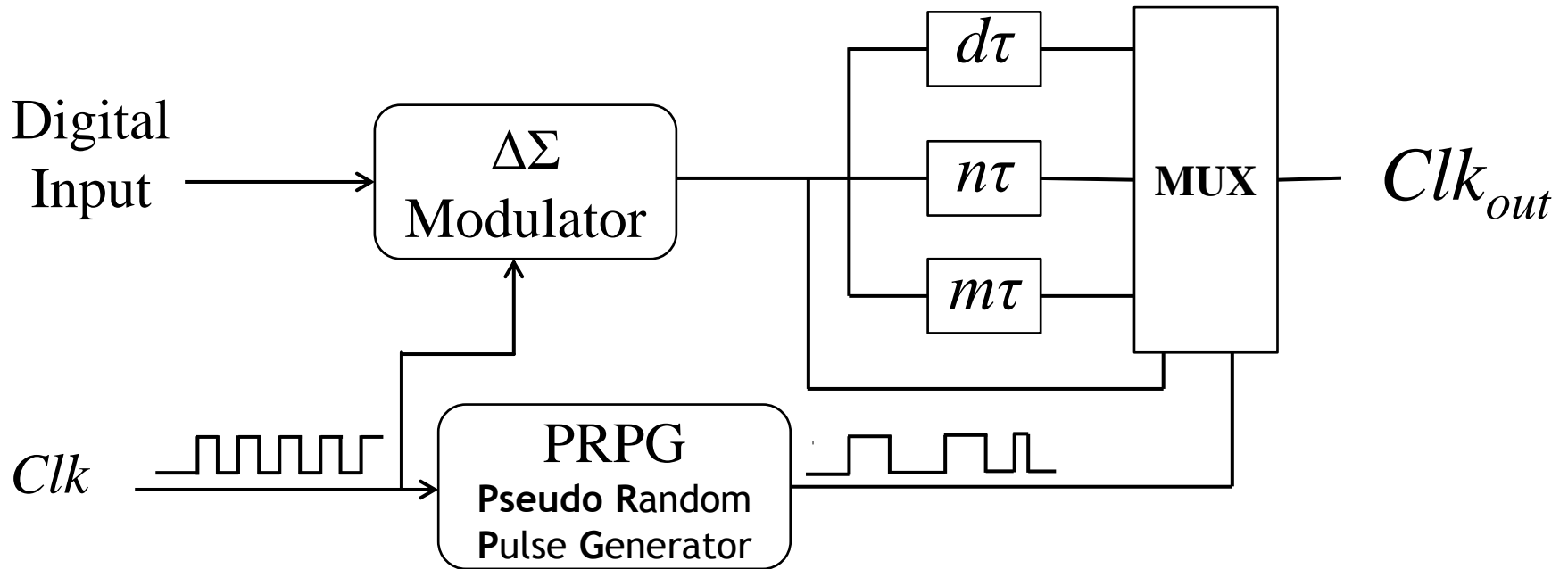
Pseudo Random Jitter

■ Output pulse cycle = $k(D_{out}, h)$

Exa. : ($D_{out} = 10110$)



PRJ $\Delta\Sigma$ DTC - Configuration



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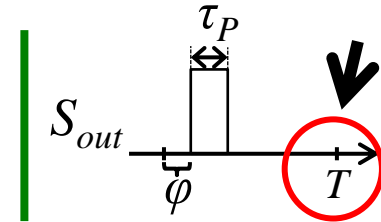
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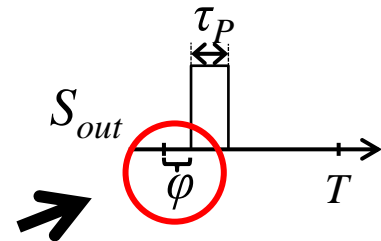
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Compound DTC...

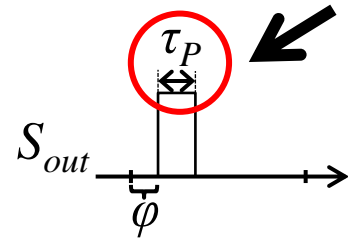
PCMDTC: *based on digital Input Alter T*



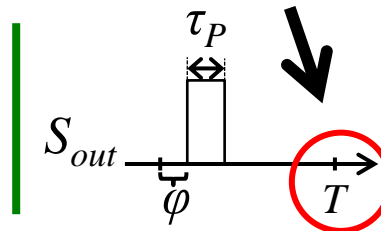
PPMDTC: *Alter φ*



PWMDTC: *Alter τ_p*



PRJDTC: *Alter T randomly*



PPCMDTC, PPWMDTC, PPCRJDTC, ...

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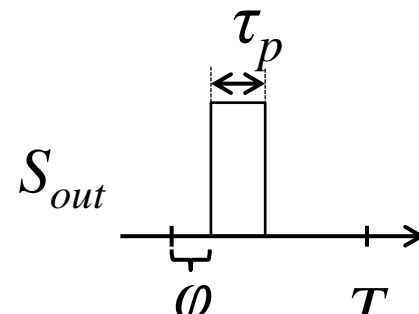
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SSGC with Exclusive Noise Spectrum using $\Delta\Sigma$ DTC

Digital Pulse

$$T_C = 1 \text{ (base)}, T = nT_C, \tau_P = mT_C, \varphi = 2\pi q/n$$



PCM $\Delta\Sigma$ DTC

$$f_{notch} = \frac{K \times (n_H + n_L)}{2|n_H - n_L|} f_s \quad (1)$$

$$K = |n_H - n_L| - 1, |n_H - n_L| - 2, \dots, 1.$$

$$n_H, n_L = 1, 2, 3, 4, \dots,$$

$$\text{defined as } n_H = T_H/T_C, n_L = T_L/T_C.$$

PPM $\Delta\Sigma$ DTC

$$f_{notch} = \frac{K}{|q_H - q_L|} f_s \quad (2)$$

$$K = |q_H - q_L| - 1, |q_H - q_L| - 2, \dots, 1.$$

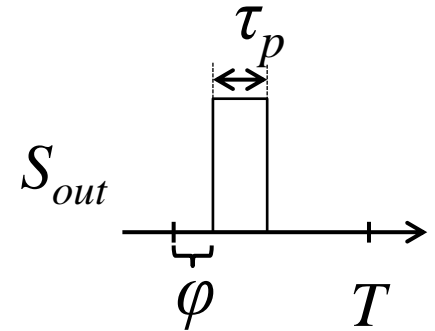
$$q_H, q_L = 1, 2, 3, 4, \dots,$$

$$\text{defined as } q_H = n_H(\phi_H/2\pi), q_L = n_L(\phi_L/2\pi).$$

SSGC using Delta-Sigma DTC

Digital Pulse

$$T_C = 1 \text{ (base)}, T = nT_C, \tau_P = mT_C, \varphi = 2\pi q/n$$



PWMΔΣDTC

$$f_{notch} = \frac{K}{|m_H - m_L|} f_s \quad (3)$$

$$K = |m_H - m_L| - 1, |m_H - m_L| - 2, \dots, 1.$$

$$m_H, m_L = 1, 2, 3, 4, \dots,$$

$$\text{defined as } m_H = \frac{\tau_H}{T_C}, m_L = \frac{\tau_L}{T_C}.$$

PRJΔΣDTC

$$f_{notch} \simeq K \left(\frac{4n_L + p + q}{4G} \right) f_s \quad (4)$$

$$K = G - 1, G - 2, \dots, 1.$$

G is the greatest common divisor between p and q

$$p = |n_{H1} - n_L|, q = |n_{H2} - n_L|.$$

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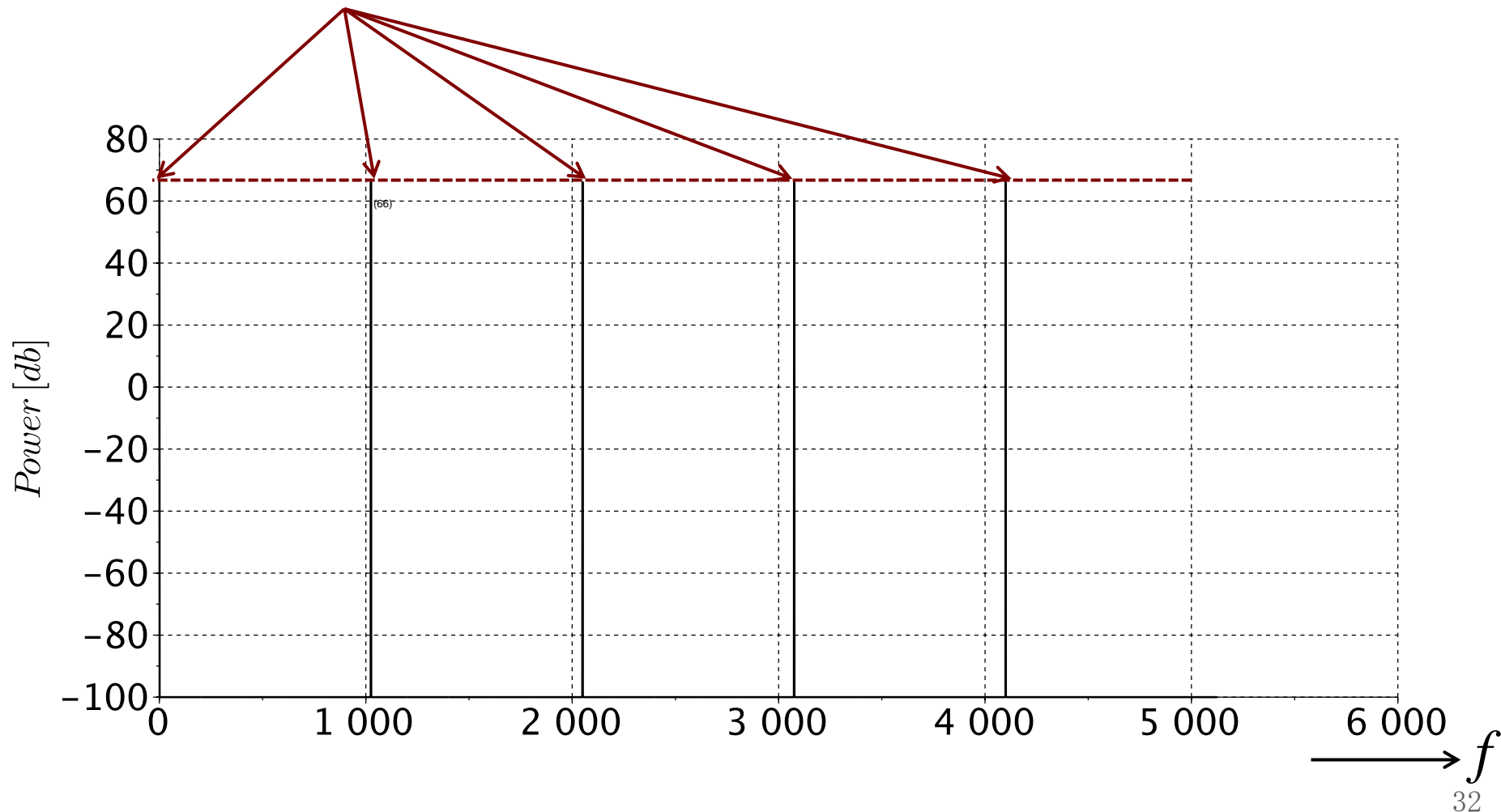
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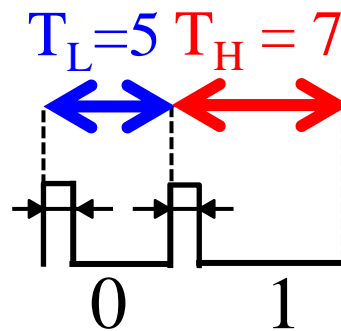
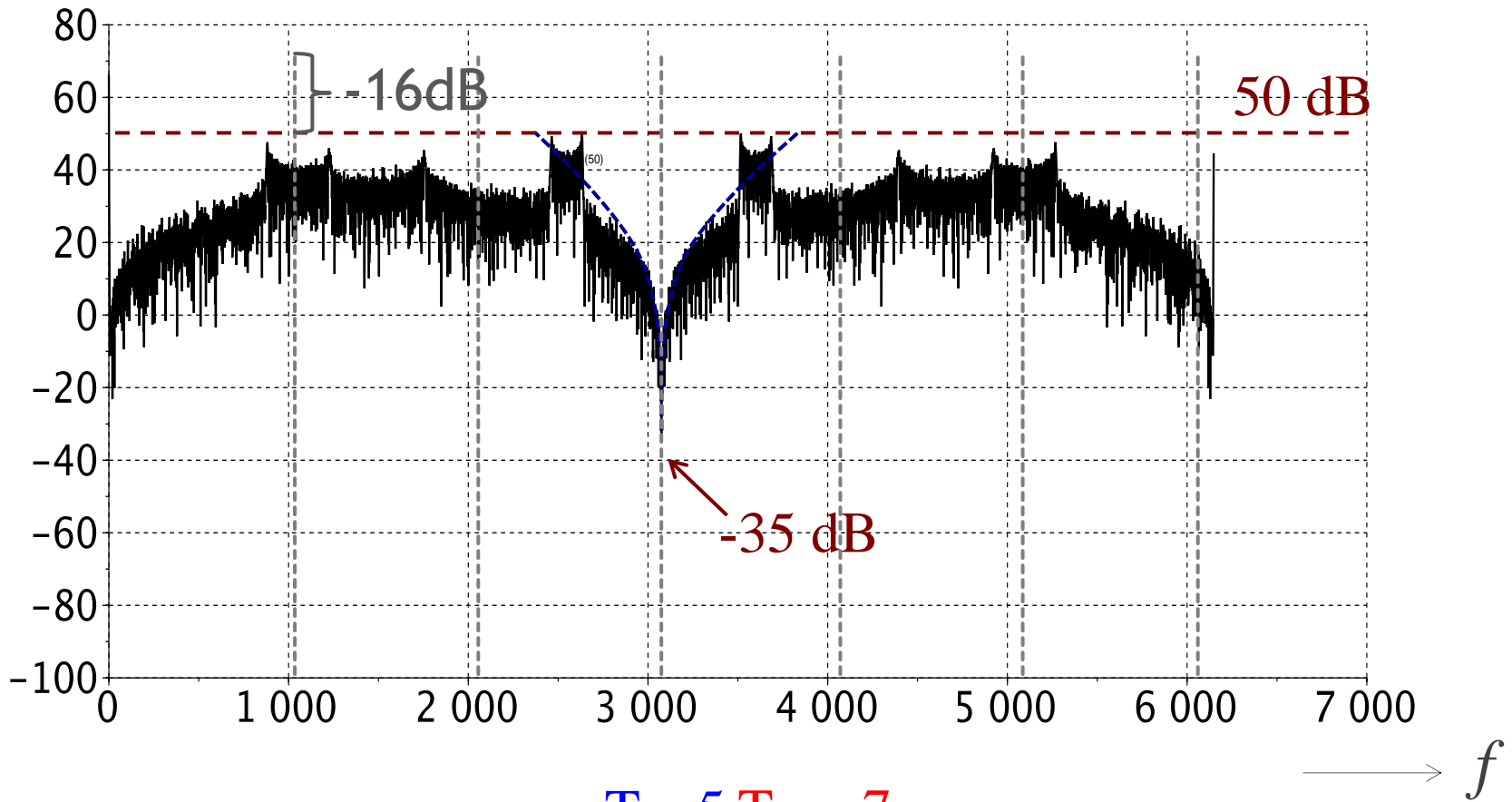
Result • Clock's PSD (**Without DTC**)

66 dB

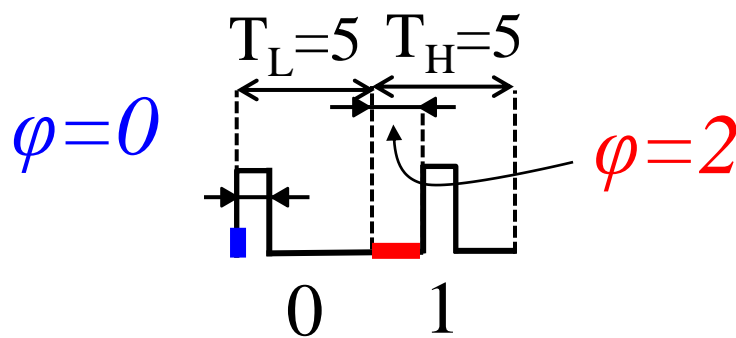
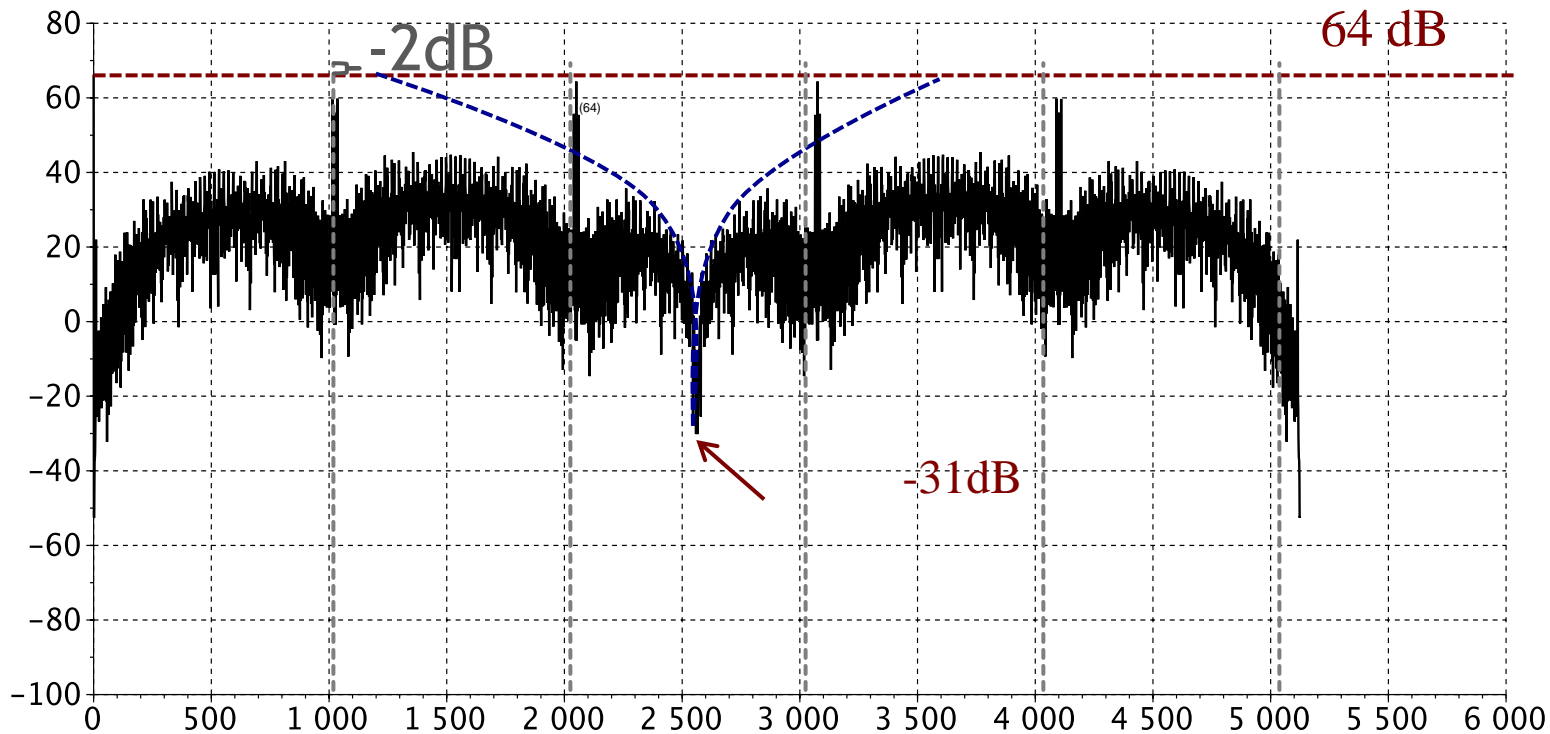
in Base & in Each
Clock Harmonics



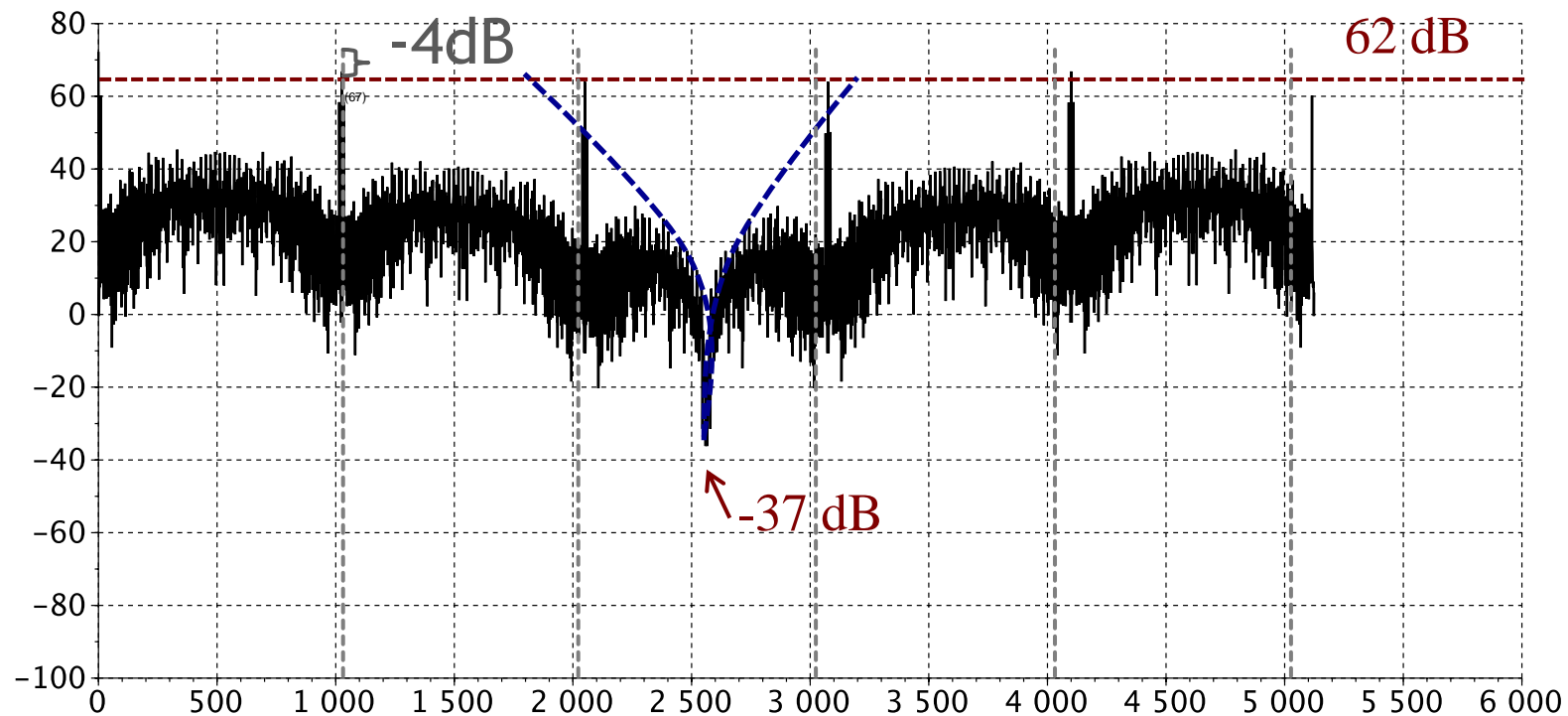
PCMA $\Delta\Sigma$ DTC



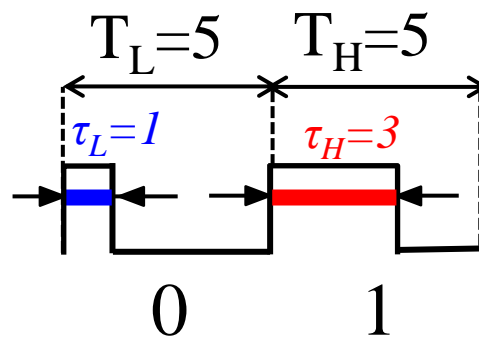
PPMΔΣDTC



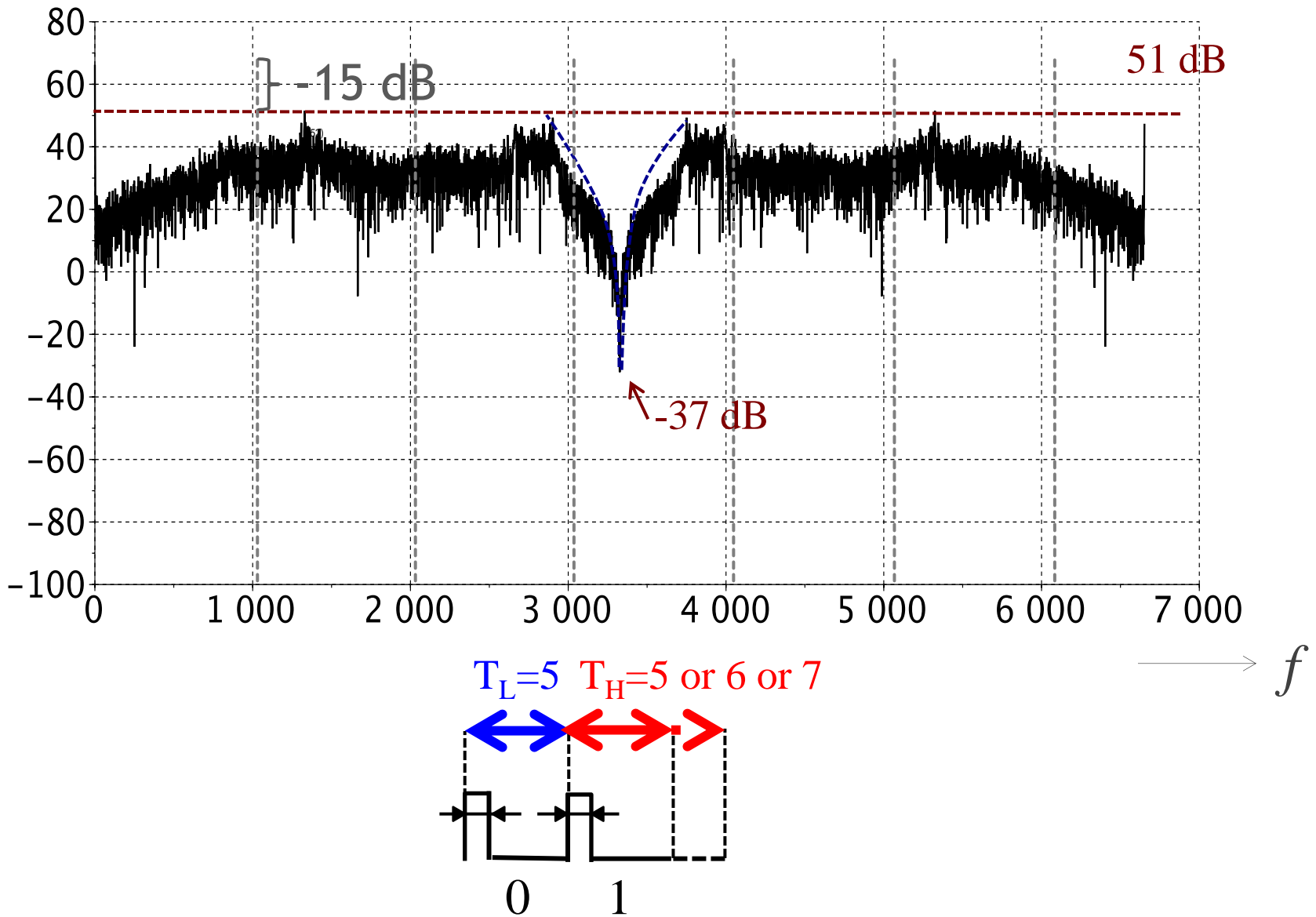
PWMΔΣDTC



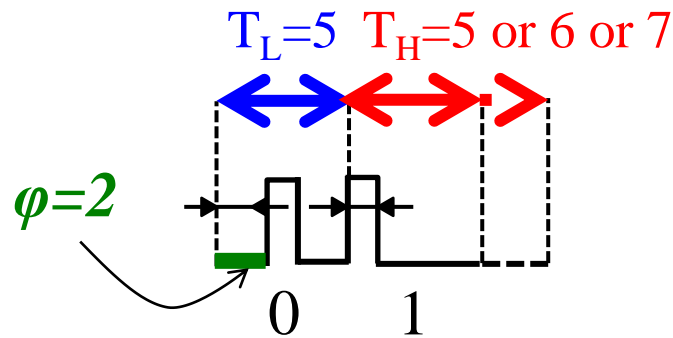
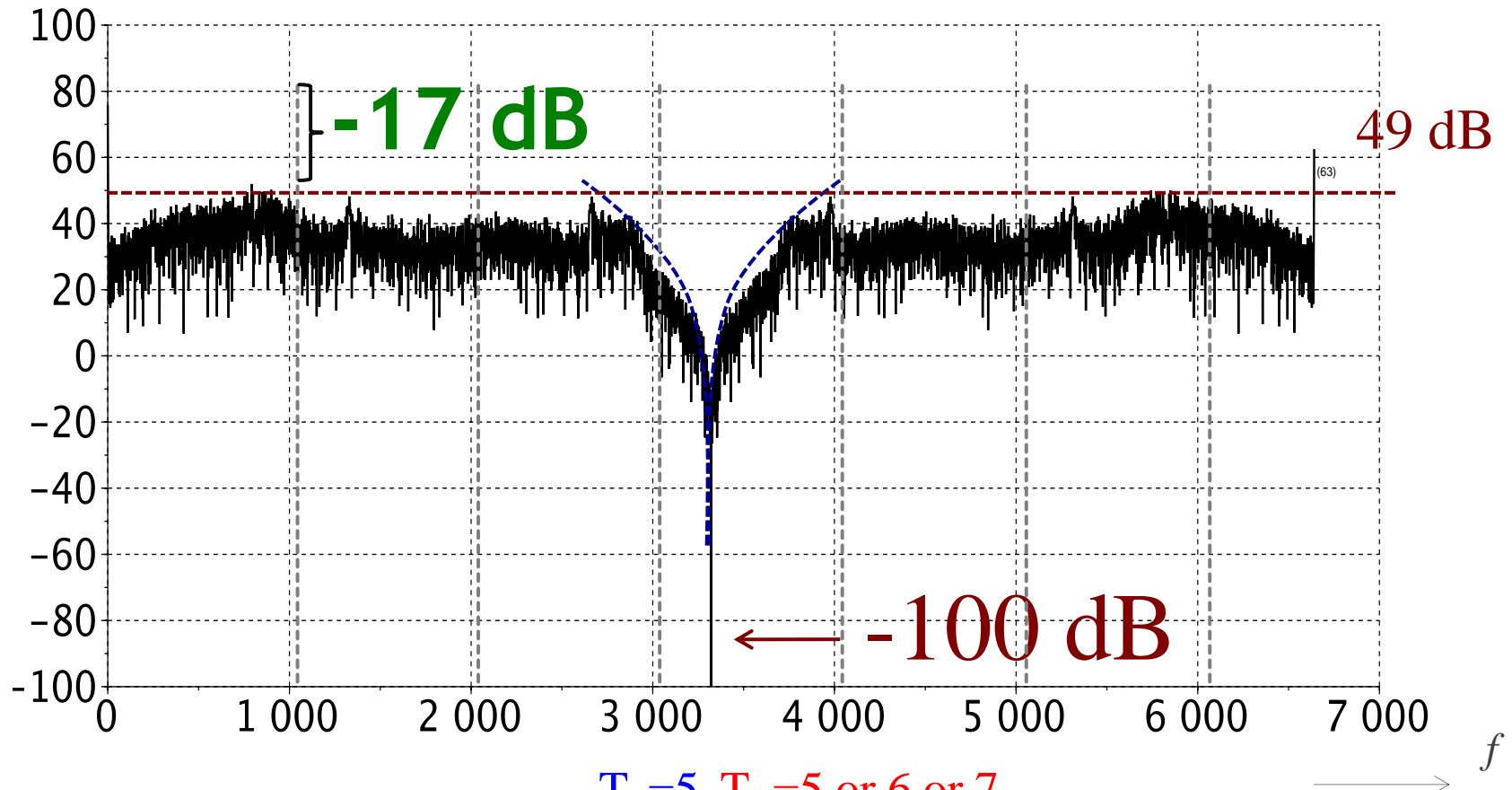
→ f



PRJΔΣDTC



Compound DTC: PRJWP $\Delta\Sigma$ DTC



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Result

Low Cost

Simplicity

Accuracy

**+ Completely Digital Circuit
+ High Frequency clock**

**Spreading Usage Spectrum of
SSCG With Exclusive Noise Spectrum!**

The End

小林先生ありがとうございます

ご清聴有り難う御座います

Cảm ơn bạn rất nhiều

非常感谢

Thank You Very Much

خیلی ممنون

Muchas gracias

Большое спасибо

Vielen Danken

Presentation



Presentation Start

Presentation



Kobayashi Ring



Conclusion

Presentation



Question and Answer