

# P96 Research on Gate Voltage Dependent 1/f Noise Variance Modeling for n-Channel MOSFETs

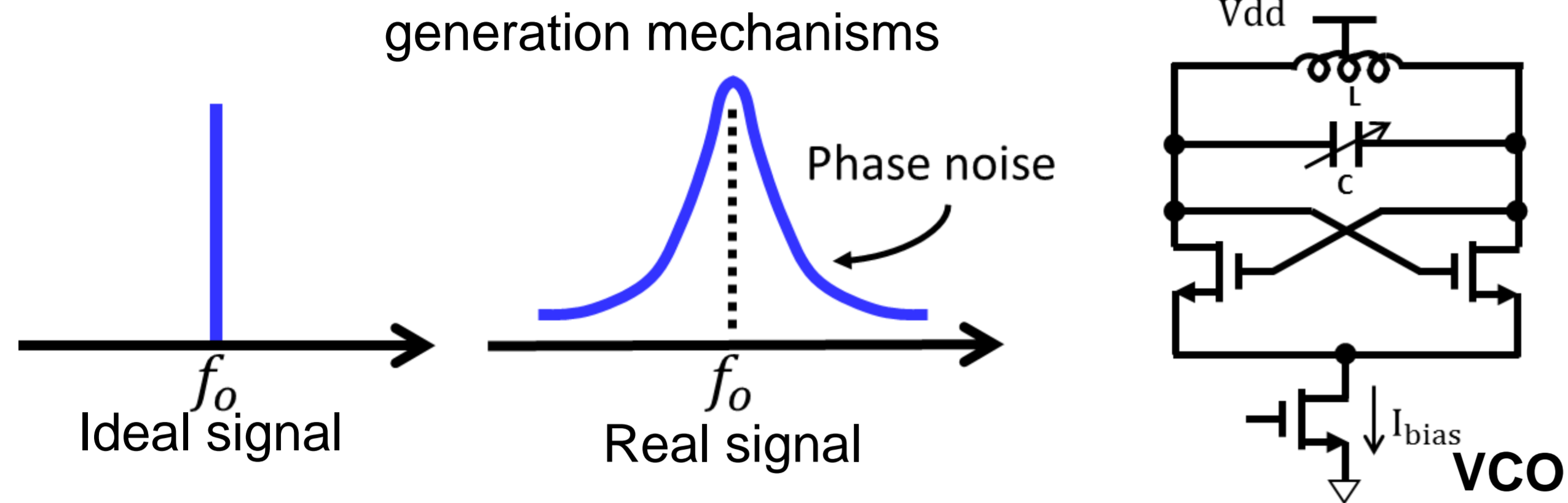
Yukiko Arai, Hitoshi Aoki, Fumitaka Abe, Shunichiro Todoroki, Ramin Khatami, Masaki Kazumi, Takuya Totsuka, Taifeng Wang, Haruo Kobayashi

Department of Electronic Engineering, Gunma University, 1-5-1 Tenjin-cho, Kiryu 365-8515, Japan

## Research Purpose

### 1/f noise in MOSFETs

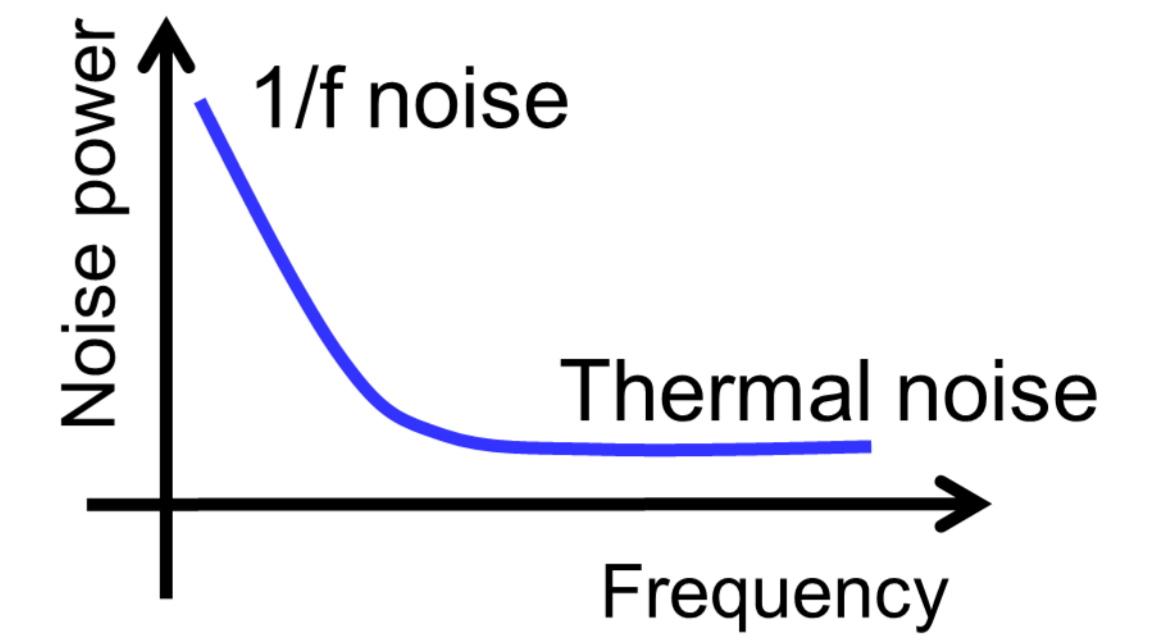
- Is an important property for any analog oscillator circuit design
- Induces degradation of phase noise performance in VCOs
- Must be based on correct noise generation mechanisms



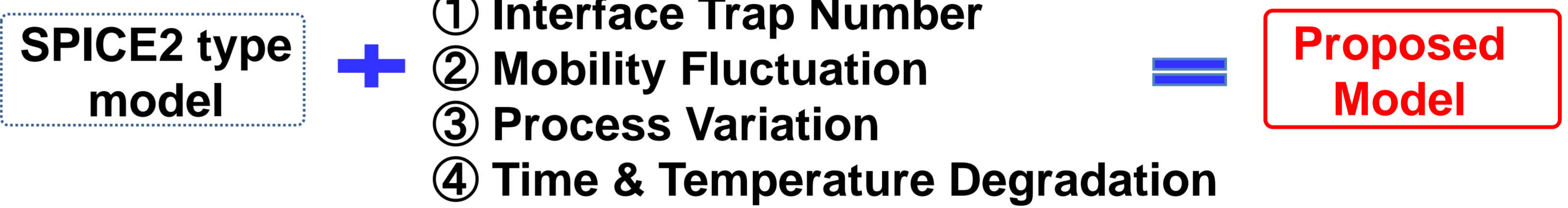
- Development of an accurate yet simple 1/f noise model
- Implementation on SPICE3 (MDW-SPICE) circuit simulator

## Research Background

- Refinement of semiconductor process  
→ **Difficulty of analog circuit design**
- Noise have no regularity  
→ **Necessity of noise simulation**
- Thermal noise and 1/f noise influence MOSFET characteristic  
→ **1/f noise is more dominant in low frequencies**  
⇒ **Discussion of 1/f noise**



## Research Approach



## MOSFET 1/f Noise Model Derivations

SPICE2 type model ↔ Hooge's model mobility fluctuations model

$$S_{I_D}(f) = \frac{KF \cdot I_D^{AF}}{C_{OX} L_{eff}^2 f^{EF}} \quad S_{I_D}(f) = \frac{\alpha_H \cdot \mu_{eff} \cdot 2kT \cdot I_D}{f \cdot L_{eff}^2}$$

Comparison assuming of  $AF = EF = 1$  as ideal 1/f noise

$$\alpha_H \cdot \mu_{eff} \cdot 2kT = \frac{KF}{C_{OX}} \quad \text{Replacing } KF \text{ with a mobility fluctuation equation}$$

$$KF = C_{OX} \cdot \alpha_H \cdot \mu_{eff} \cdot 2kT$$

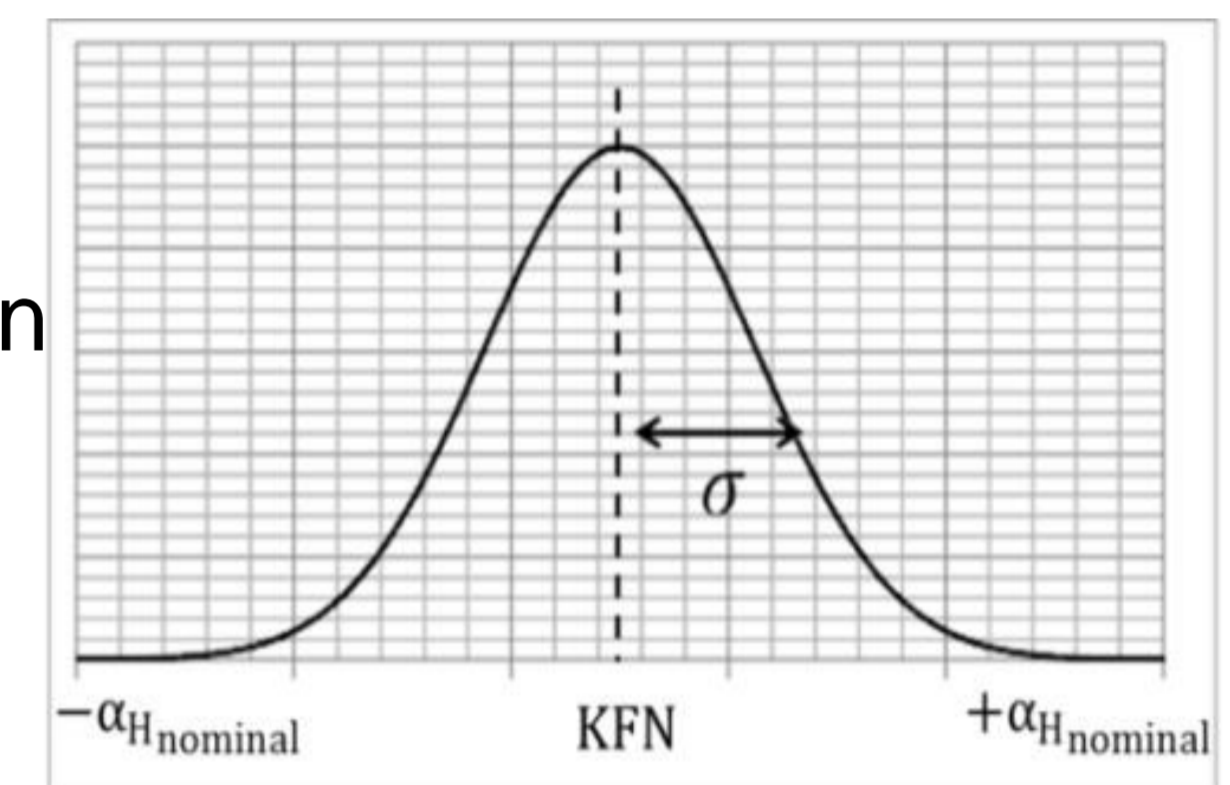
**We included Hooge's model in SPICE2 type model !**

## 1/f Noise Variation

- $\alpha_H$  is a coefficient caused by phonon scattering
  - Relation to mobility fluctuations
  - Decrease with a function of the effective  $V_{GS}$

$$\alpha_H \propto e^{-(V_{gs} - V_{TH})}$$

Variability is caused by the device process variation  
⇒ **Gaussian distribution**



- $D$  as Gaussian Normalized Random Number  
⇒ fluctuates from 0 to 1  
 $\alpha_H$  varies ⇒ **1/f noise vary**

$$\alpha_H = (2 \cdot \alpha_{H,nominal} \cdot (D - 0.5) + KFN) \cdot e^{-(V_{gs} - V_{TH})}$$

## Proposed Model

$$S_{I_D}(f) = \frac{KF \cdot I_D^{AF}}{C_{OX} \cdot L_{eff}^2 \cdot f^{EF}}$$

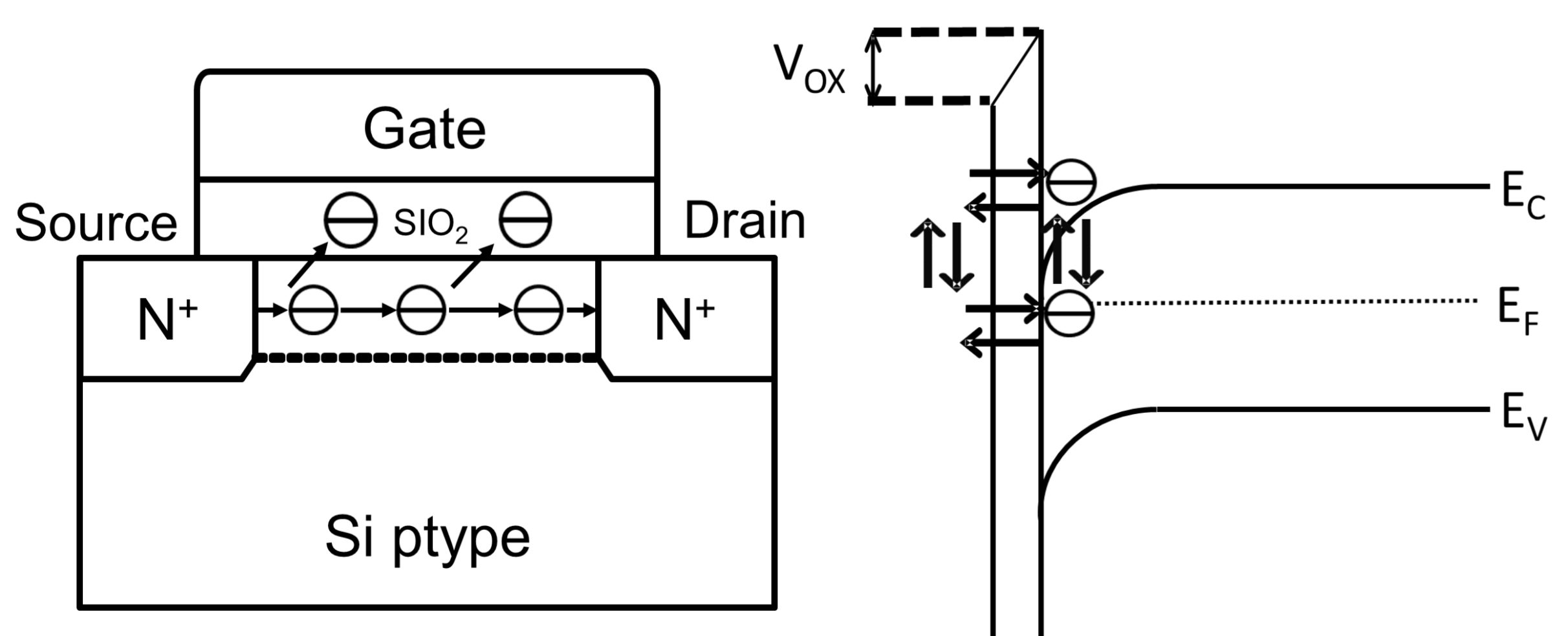
$$KF = C_{OX} \cdot \mu_{eff} \cdot 2kT \cdot (2 \cdot \alpha_{H,nominal} \cdot (D - 0.5) + KFN) \cdot e^{-(V_{gs} - V_{TH})}$$

Includes two noise generation mechanisms,

**mobility** and **interface trap number fluctuations**

## 1/f noise Generation Mechanisms

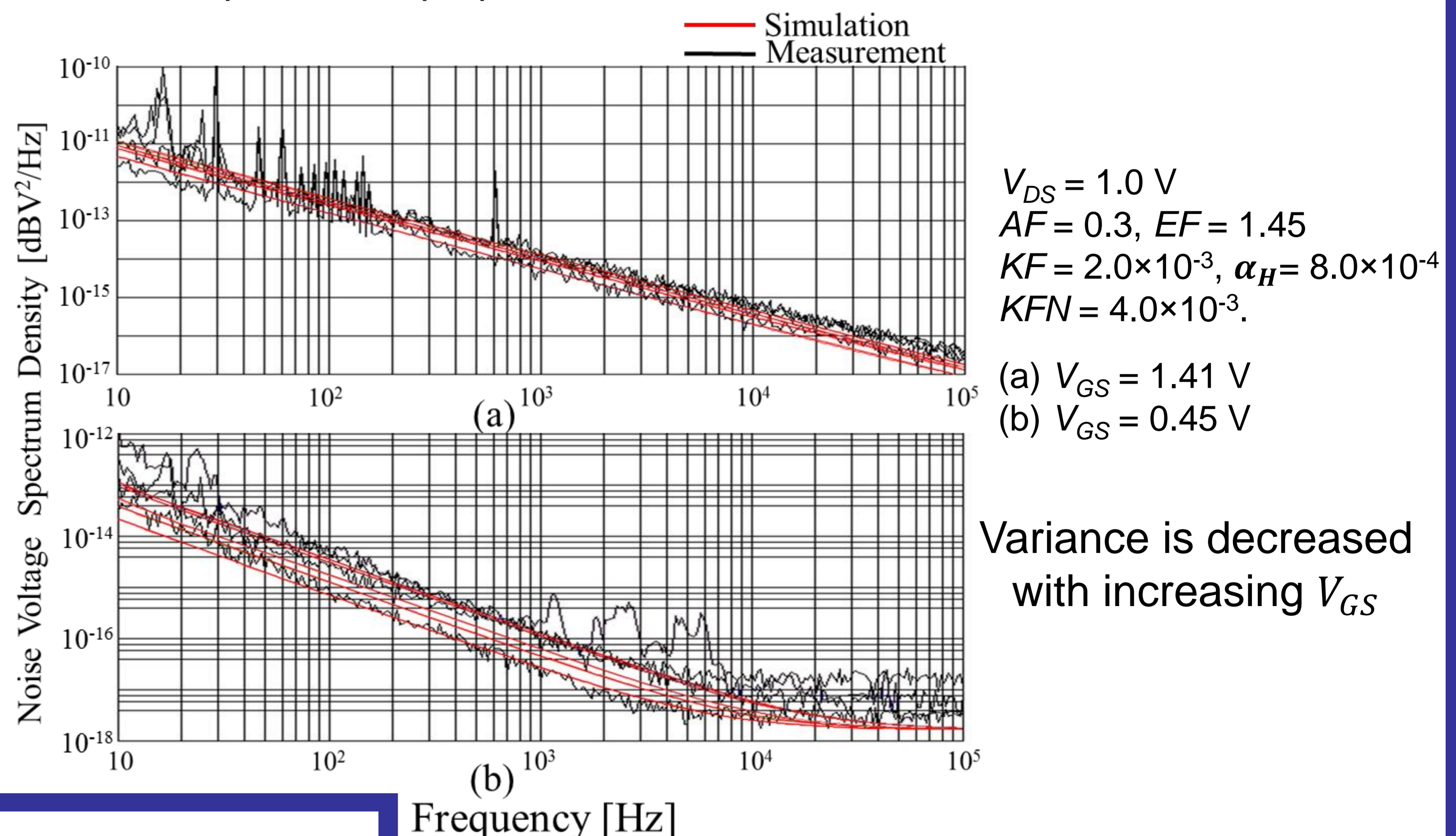
- **Mobility Fluctuations**
  - Caused by phonon scattering
  - Dependent on  $V_{GS}$
  - Mobility fluctuation ⇒ 1/f noise variability
- **Interface traps**
  - Caused by electron tunneling transitions



from the Si to the gate oxide      between interface traps

## Simulation and Measurement Results

We have implemented proposed model in BSIM4 model with our MDW-SPICE



Variance is decreased with increasing  $V_{GS}$

## Conclusion

- 1/f noise causes degradation of phase noise performance in oscillators  
⇒ Development of **new 1/f noise model**  
⇒ Inclusion of mobility and interface trap fluctuations with process variations
- Implementation on our MDW-SPICE circuit simulator  
⇒ Excellent agreements with measurement results
- Circuit design margin can be minimum !

**Proposed model agreed with measurement results**

**Gate voltage dependent 1/f noise variations are included in our model !**