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## Estimation of Circuit Component Values in Buck Converter using Efficiency Curve

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# Outline

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1. Purpose of this work
2. Background
3. Estimation principle
4. Estimation result
5. Summary

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# Purpose of this work

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- Development of an estimation method for component values in DC-DC converter from its measured efficiency curve
- Validation of its transfer function estimation for phase compensation design with estimated component values

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# Background



Switching converter

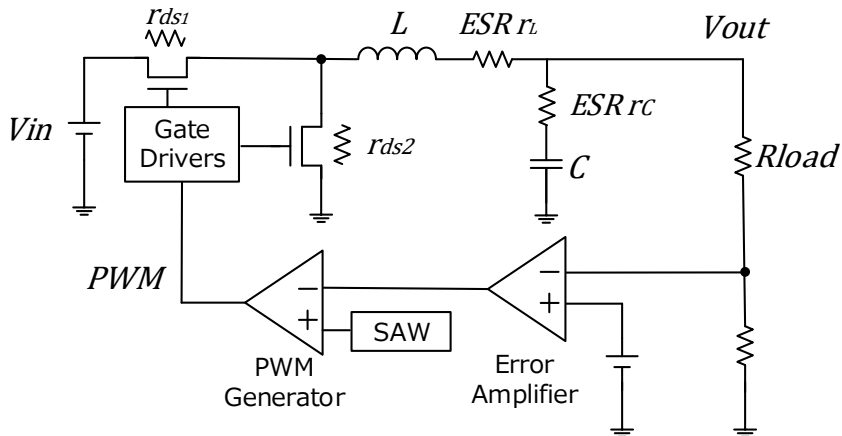
## Electronic Devices



IoT Device



Information Device



## Demands

Smaller  
Lighter  
Higher efficiency

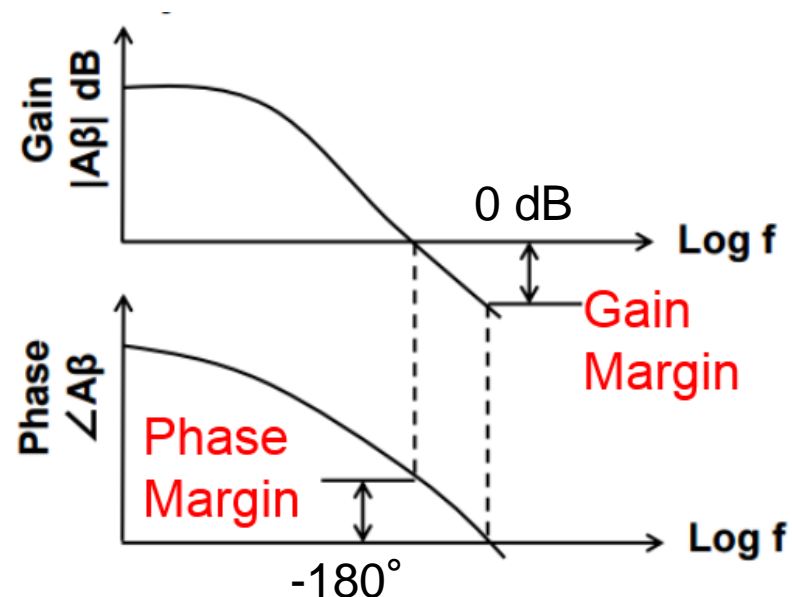
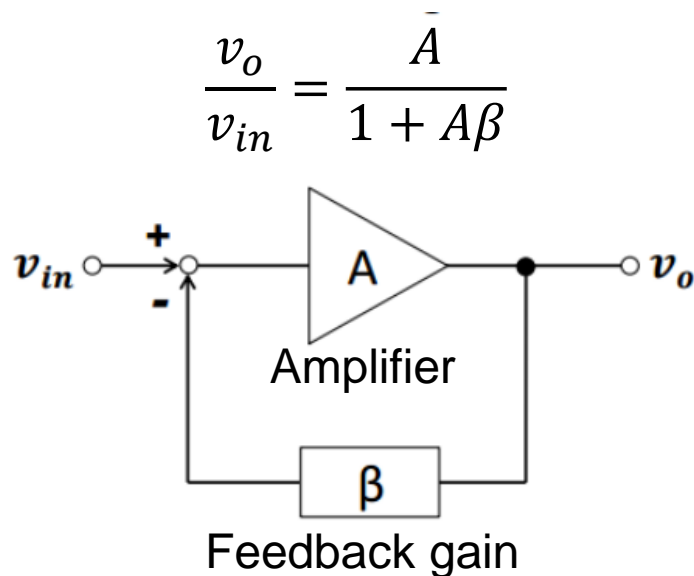
# Negative Feedback Circuit

Switching converter use negative feedback control

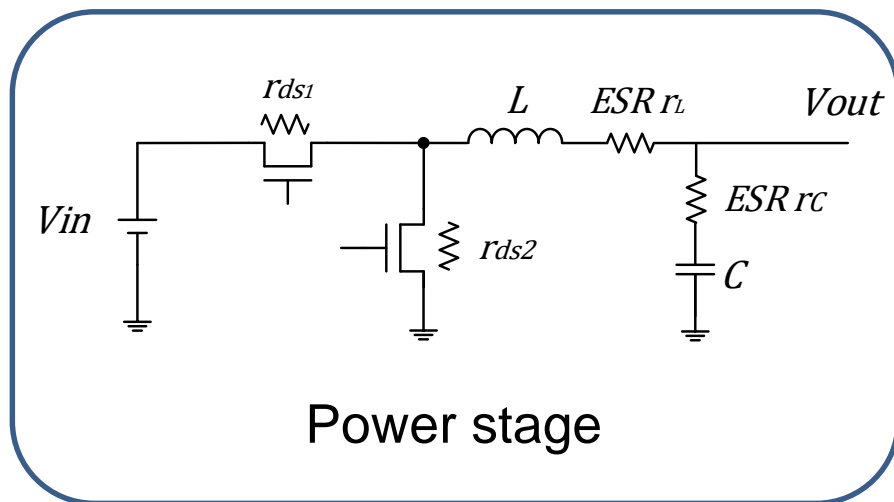
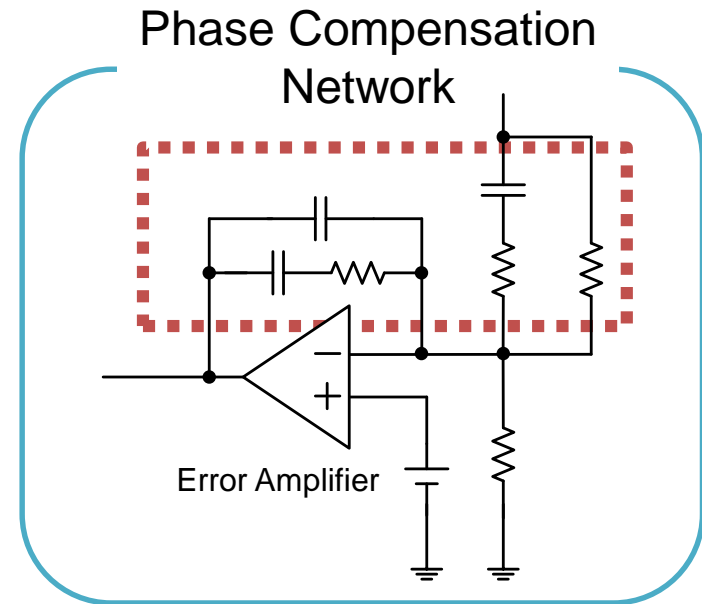
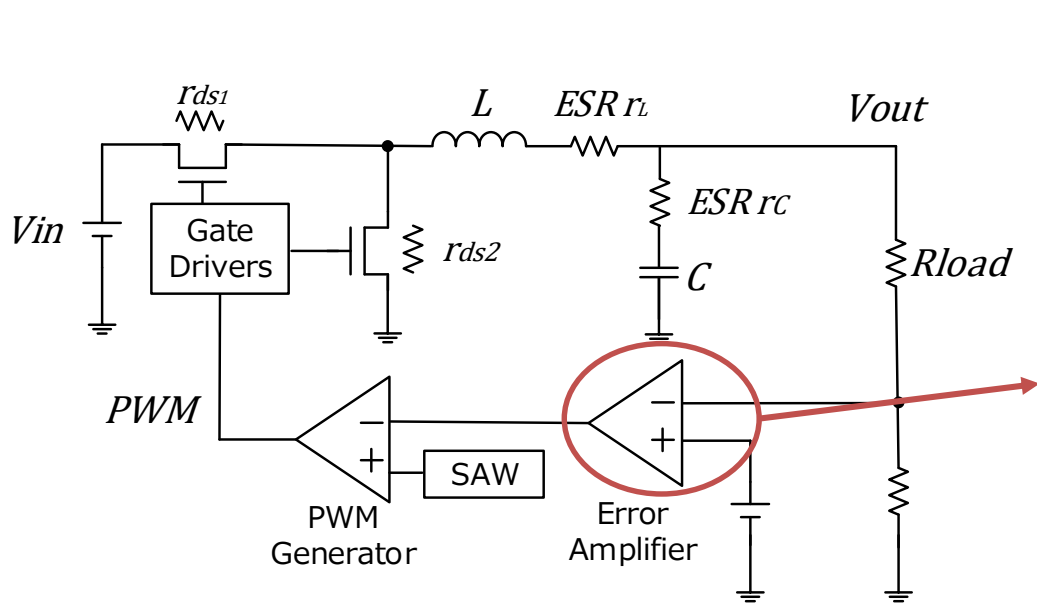
When loop gain  $A\beta = -1$ , circuit oscillates.



Need suitable phase compensation.

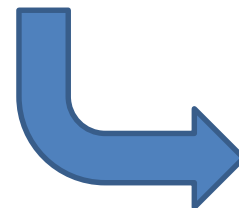


# Phase Compensation Design



$$G_{dv}(s) \Big|_{\substack{\Delta V_i=0 \\ \Delta I_o=0}} = \frac{\Delta V_o}{\Delta D} \rightarrow \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

Transfer function of power stage



is necessity



# Power-Stage Transfer Function and Component Values

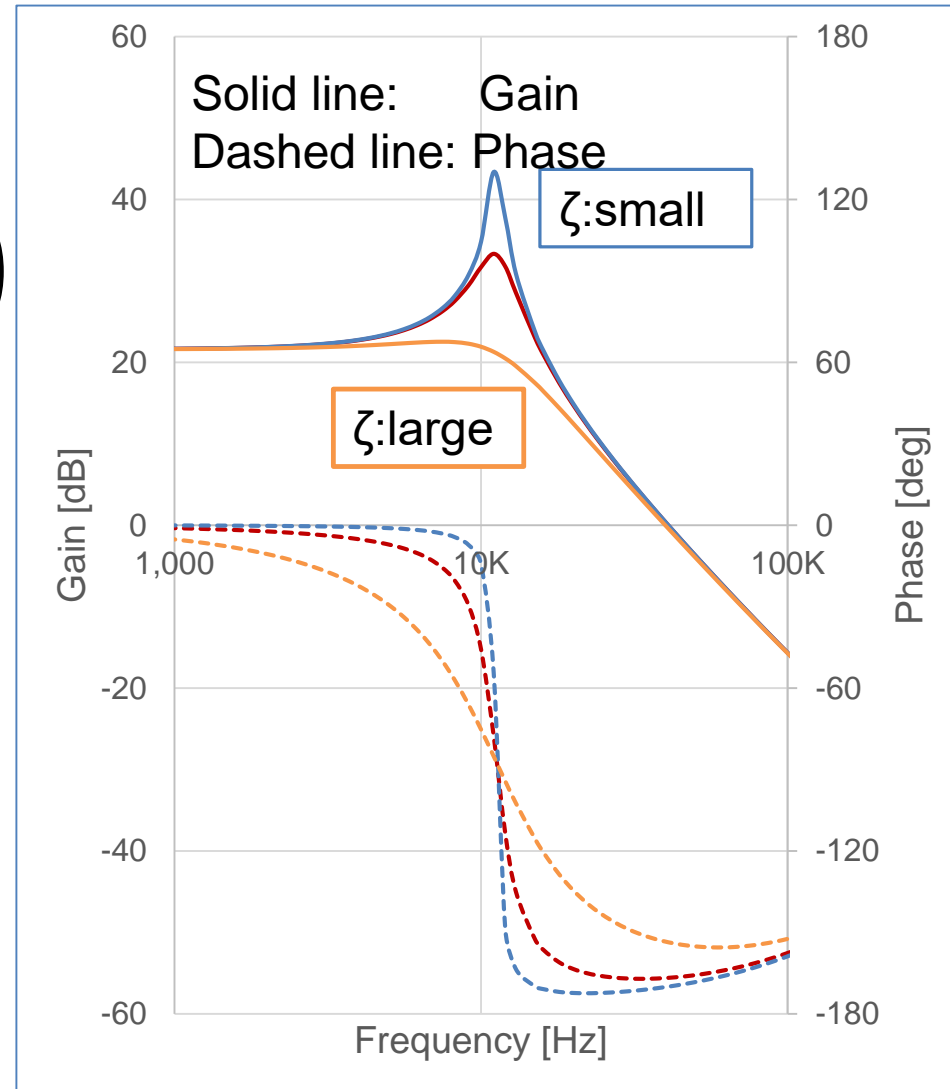
$$G_{dv}(s) \Big|_{\substack{\Delta V_i=0 \\ \Delta I_o=0}} = \frac{\Delta V_o}{\Delta D} \rightarrow \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$$

$$= \frac{V_i \cdot \omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \left( 1 + \frac{s}{\omega_{esr}} \right)$$

$$\zeta = \frac{r_L + r_C + r_{ds}}{2} \sqrt{\frac{C}{L}}, \quad \omega_n = \frac{1}{\sqrt{LC}}, \quad \omega_{esr} = \frac{1}{Cr_C}$$

Damping factor  $\zeta$

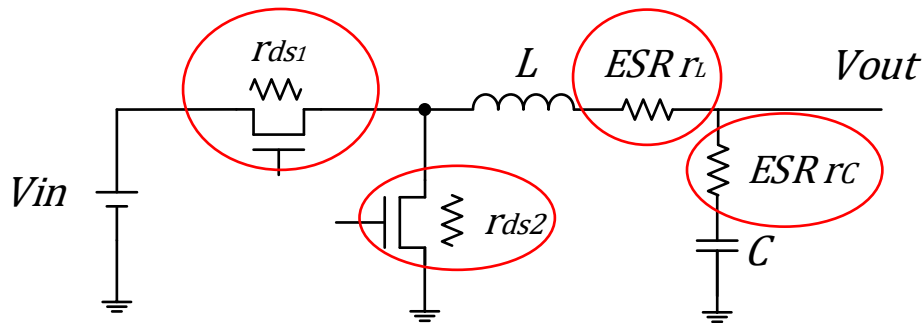
| $\zeta$ | Gain    | Phase   |
|---------|---------|---------|
| Larger  | Peak    | Looser  |
| Smaller | No peak | Steeper |



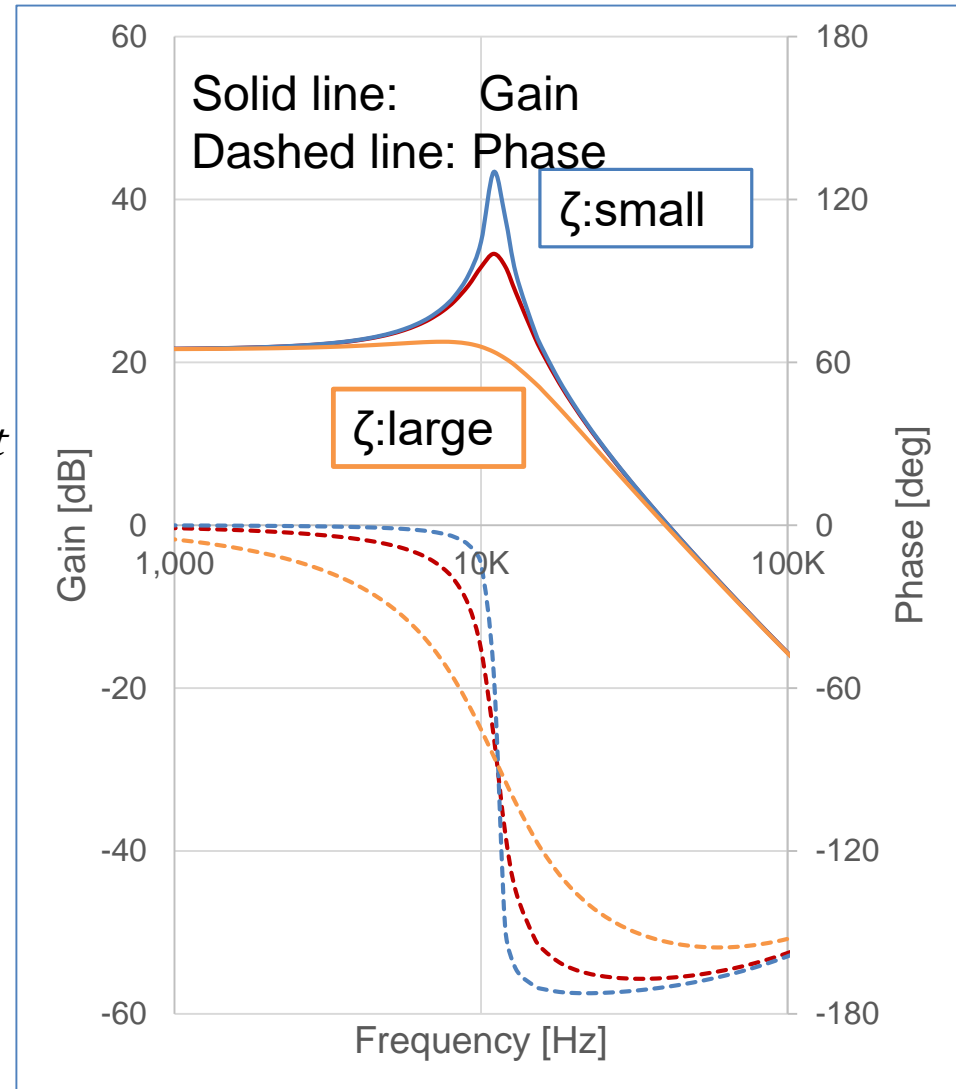
# Importance of Component Values

$\zeta$  depends on  
circuit component values

$$\zeta = \frac{r_L + r_{ds} + r_C}{2} \sqrt{\frac{C}{L}}$$

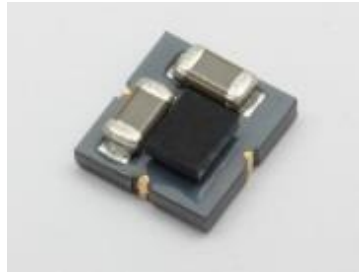


Necessary for  
phase compensation  
design

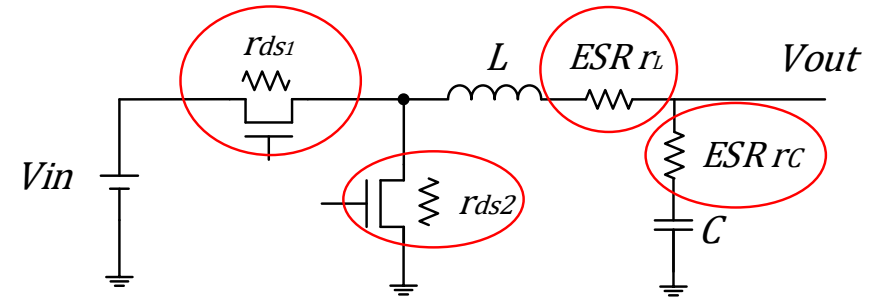


# Problems

Implemented power supply



Component values

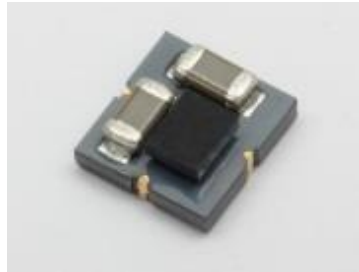
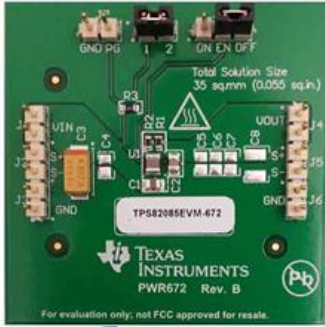


Difficult to measure



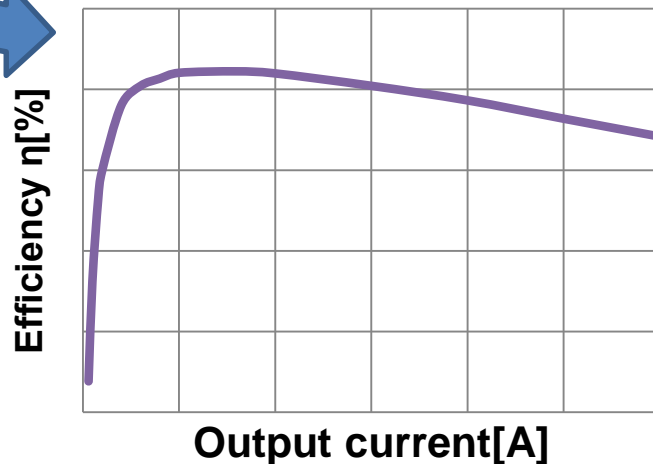
# Proposed method

Implemented power supply

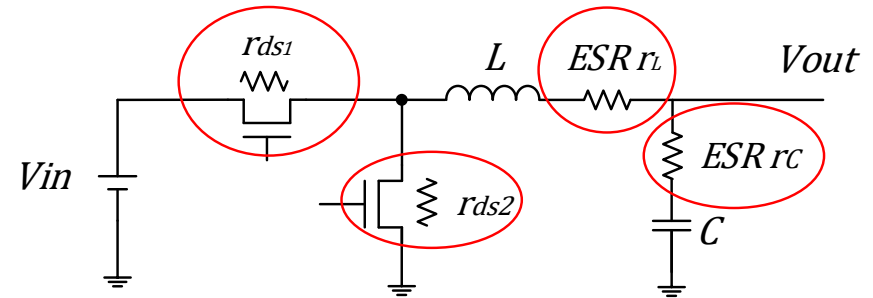


Easy

Measure efficiency curve



Component values



Estimate

Our proposal

Not directly measure.

Estimation from  
measured efficiency curve.

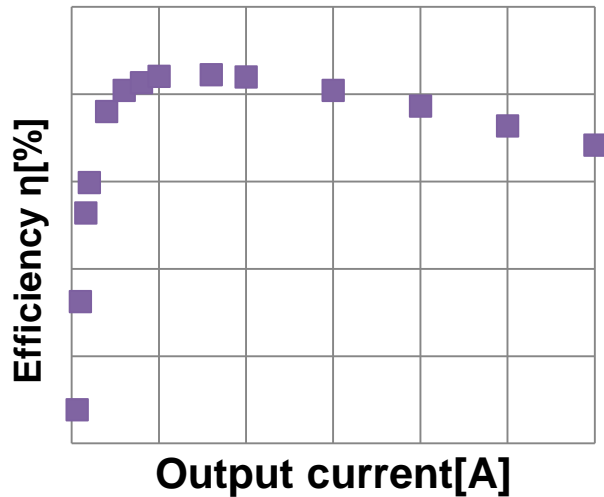
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# Estimation Principle

## Measured efficiency



## Theoretical formula of losses

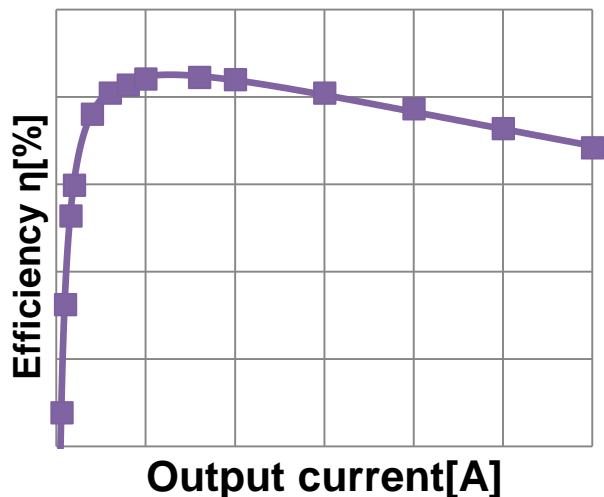
$$P_{sw\ loss} = \frac{1}{6} V_i I_o (\Delta T_{ON} + \Delta T_{OFF}) \cdot f_{sw}$$

$$P_L = R_L \cdot I_o^2 \quad P_C = R_C \cdot I_C^2$$

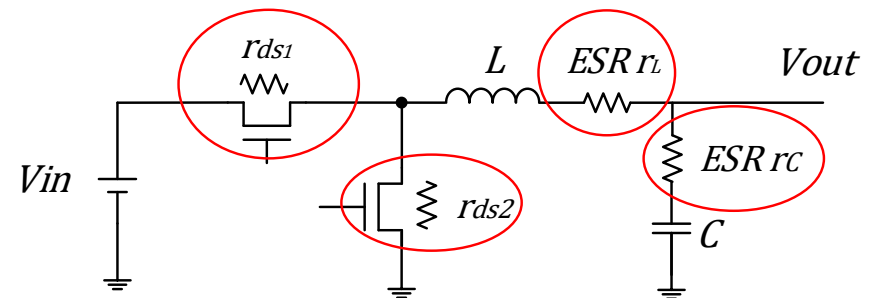
$$\eta = \frac{V_{out} \cdot I_o}{V_{out} \cdot I_o + P_{loss}}$$

Fitting

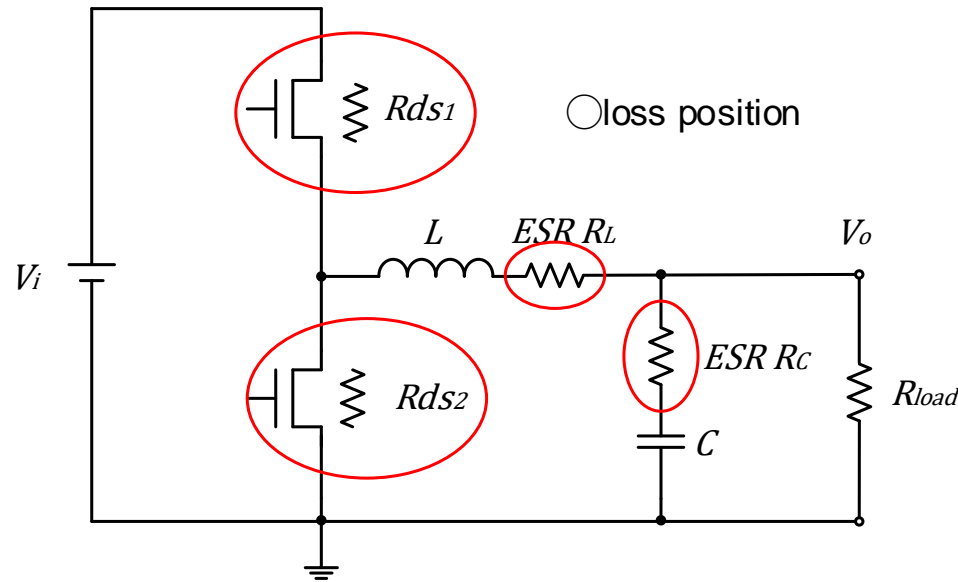
## Fitted efficiency curve



## Component values



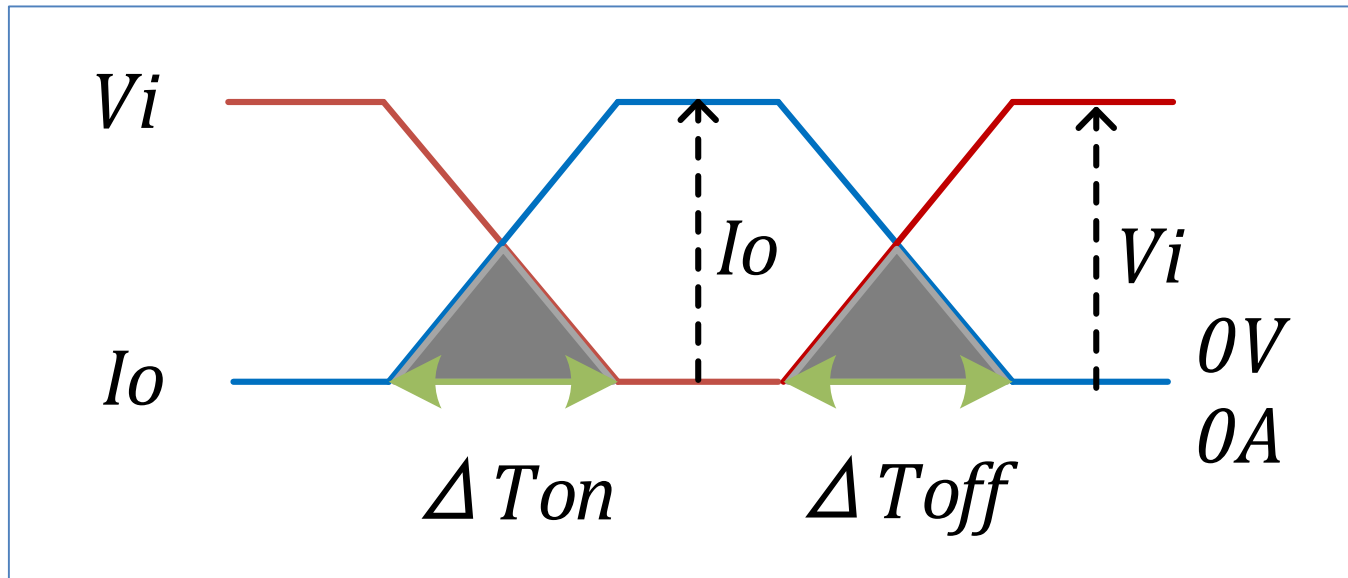
# Loss Classification of Switching Regulator



1. Proportional to the load current :  $P_1 [W]$   
Switching loss
2. Proportional to **square** of the load current :  $P_2 [W]$   
Conduction loss
3. Constant loss :  $P_{const} [W]$

# Switching Loss ( $P_1$ )

## First loss



$$P_{sw\ loss} = f_{sw} \left[ \int_0^{\Delta T_{on}} v_{tr}(t) \cdot i_{tr}(t) dt + \int_0^{\Delta T_{off}} v_{tr}(t) \cdot i_{tr}(t) dt \right]$$

$$= \frac{1}{6} V_i \cdot I_o (\Delta T_{ON} + \Delta T_{OFF}) \cdot f_{sw}$$

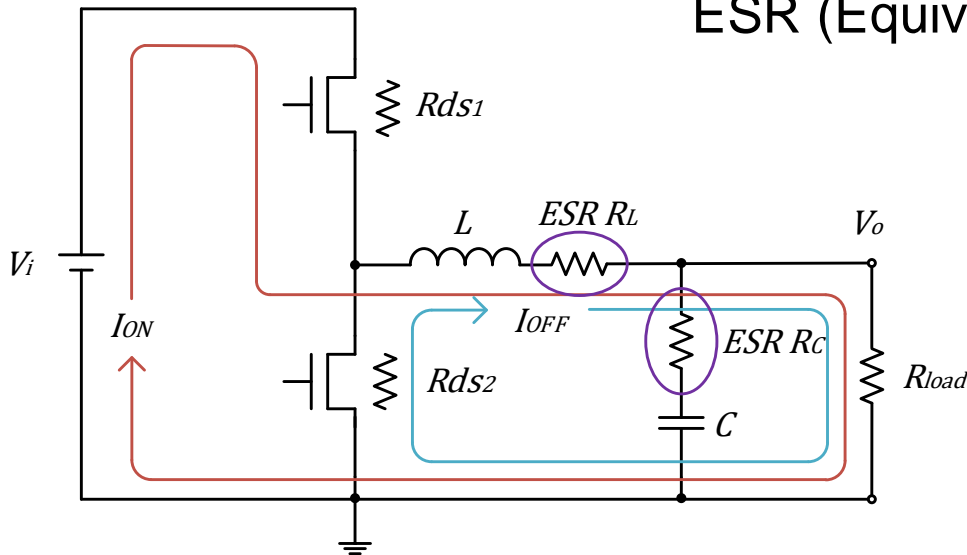
$V_i$ : Drain-source voltage [V]  
 $I_o$ : Load current [A]



# Conduction Loss of L , C ( $P_2$ )

## Second loss

ESR (Equivalent Series Resistance)



$I^2R$  drop by lead, metal coating

Caused by resistances of cable, metal

- Inductor loss

$$P_L = R_L \cdot I_o^2$$

$R_L$  : Inductor ESR

$I_o$  : Load current

- Capacitor loss

$$P_C = R_C \cdot I_C^2 \quad \text{※ } I_C \propto I_o$$

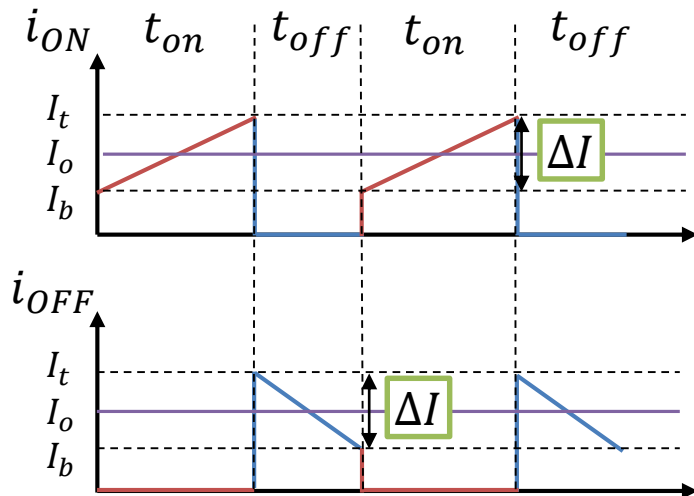
$R_C$  : Capacitor ESR

$I_C$  : Ripple current

# MOSFET Conduction Loss ( $P_2$ )

## Second loss

### MOSFET Conduction loss

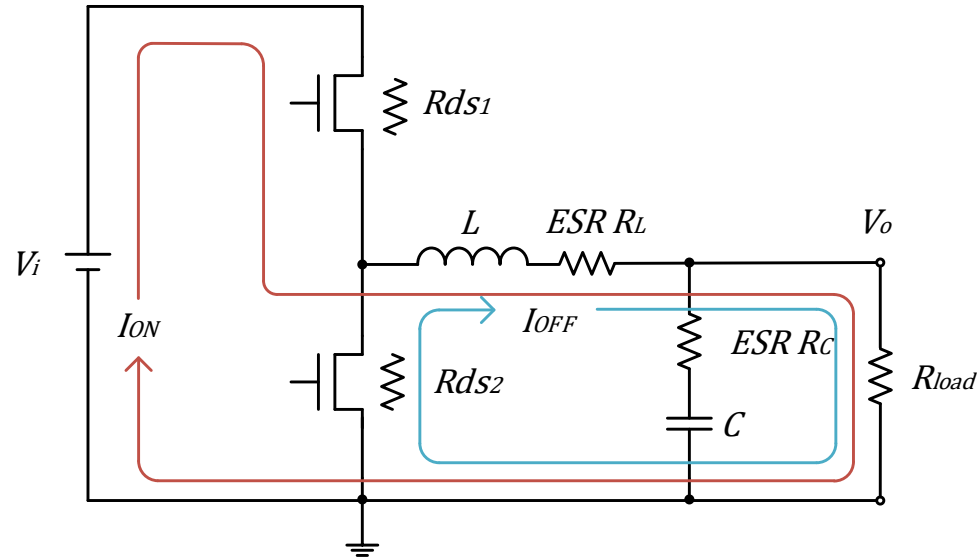


$$P_{cond1}$$

$$\frac{V_o}{V_{in}} \left( I_o^2 + \frac{\Delta I^2}{12} \right) \cdot R_{ds1}$$

$$P_{cond2}$$

$$\left( 1 - \frac{V_o}{V_{in}} \right) \left( I_o^2 + \frac{\Delta I^2}{12} \right) \cdot R_{ds2}$$



$$P_{cond} = I_o^2 \left[ \frac{V_o}{V_{in}} (R_{ds1} - R_{ds2}) + R_{ds2} \right]$$

$I_o$ : Load current

$\Delta I$ : Ripple current

$R_{DS1}$ : High-side MOS resistance

$R_{DS2}$ : Low-side MOS resistance

# Loss Equations

First loss:  $P_1$

$$P_{sw\ loss} = \frac{1}{6} V_i I_o (\Delta T_{ON} + \Delta T_{OFF}) \cdot f_{sw}$$

Second losses:  $P_2$

$$P_L = R_L \cdot I_o^2 \quad P_C = R_C \cdot I_C^2 \quad \times I_C \propto I_o$$

$$P_{cond} = I_o^2 \left[ \frac{V_o}{V_{in}} (R_{ds1(on)} - R_{ds2(on)}) + R_{ds2(on)} \right]$$

Constant loss:  $P_{const}$

|               |             |                   |
|---------------|-------------|-------------------|
| Control stage | Error amp   | Quiescent current |
|               | Comparator  |                   |
|               | Gate driver |                   |

Given as constant

# Loss Equations - Highlight

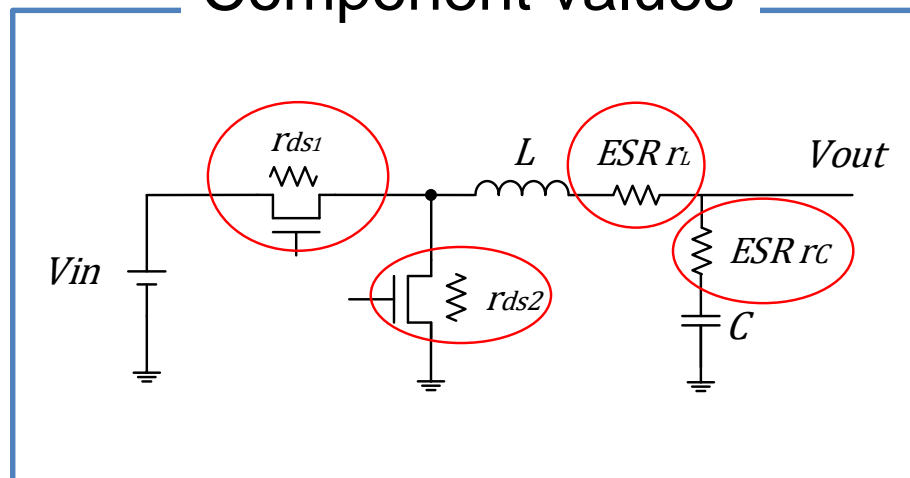
## Most important!

Second order losses:  $P_2$

$$P_L = R_L \cdot I_o^2 \quad P_C = R_C \cdot I_C^2 \quad \times I_C \propto I_o$$

$$P_{cond} = I_o^2 \left[ \frac{V_o}{V_{in}} (R_{ds1(on)} - R_{ds2(on)}) + R_{ds2(on)} \right]$$

## Component values



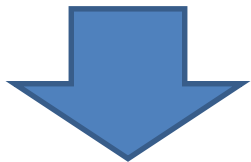
# Losses and Efficiency

$$P_2 = P_{MOS} + P_L + P_C = K_2 \cdot I_o^2$$

$$P_1 = P_{sw} = K_1 \cdot I_o$$

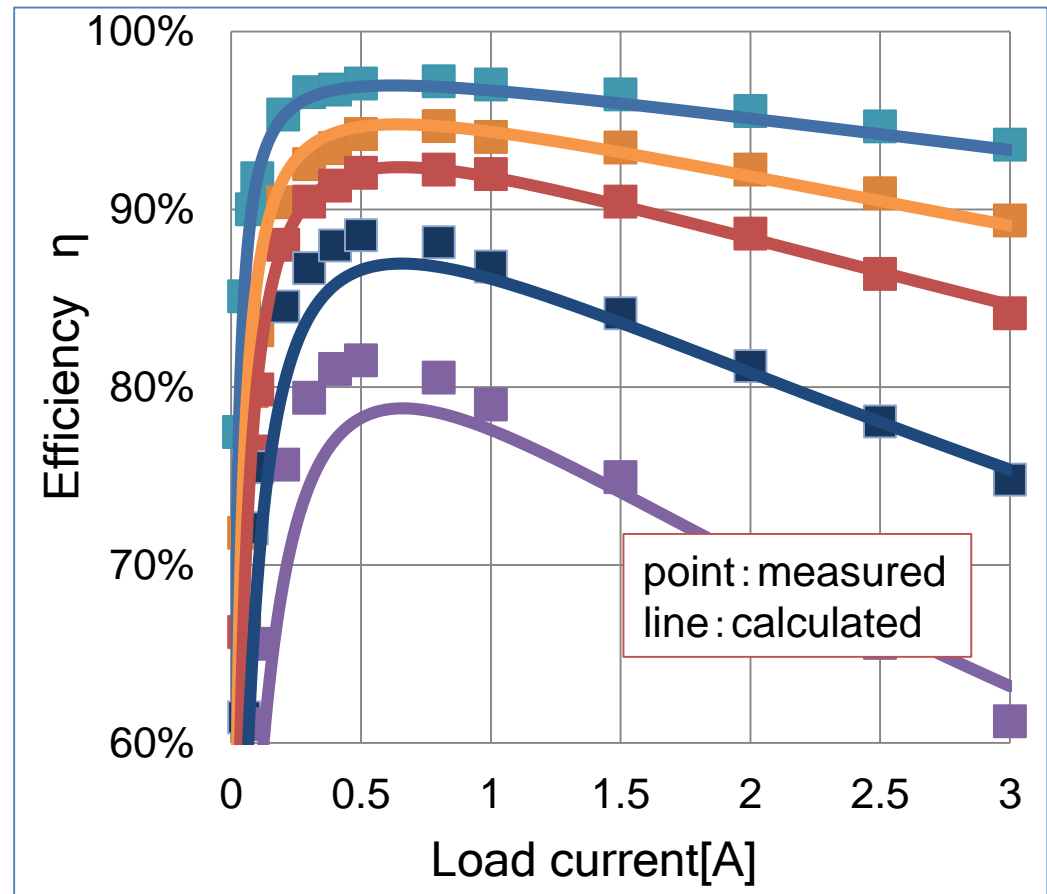
$P_{const}$

$$P_{loss} = P_2 + P_1 + P_{const}$$



Efficiency

$$\eta = \frac{V_{out} \cdot I_o}{V_{out} \cdot I_o + P_{loss}}$$

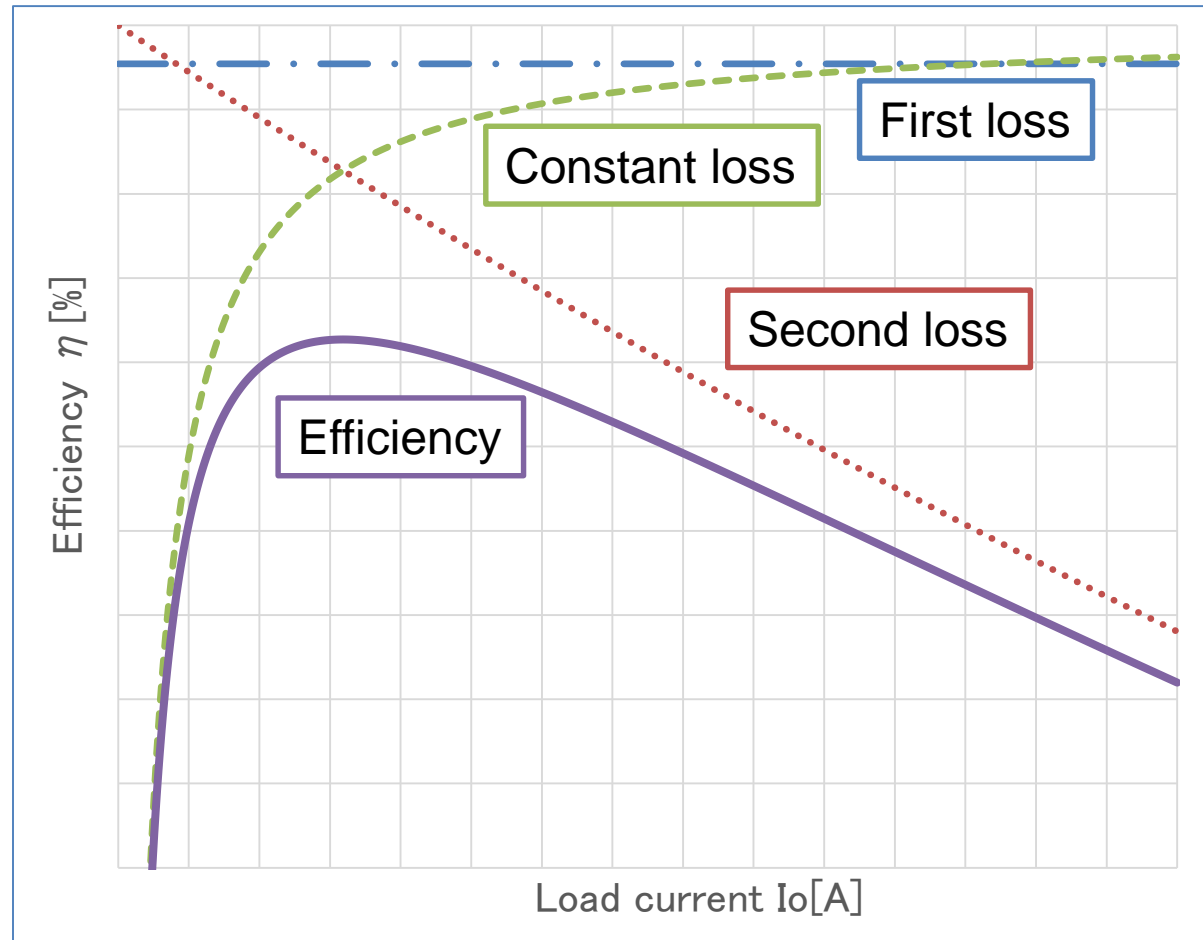


Fitting between calculation and measurement

# Effect of Each Loss to Efficiency

For load current increase

- First loss  
→ constant
- Second loss  
→ decrease
- Constant loss  
→ log increase



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# Experiment Conditions

- Synchronous step-down DC/DC converter  
(TPS54317 Texas Instruments)
- Only measured efficiency curve used

## Estimation parameters

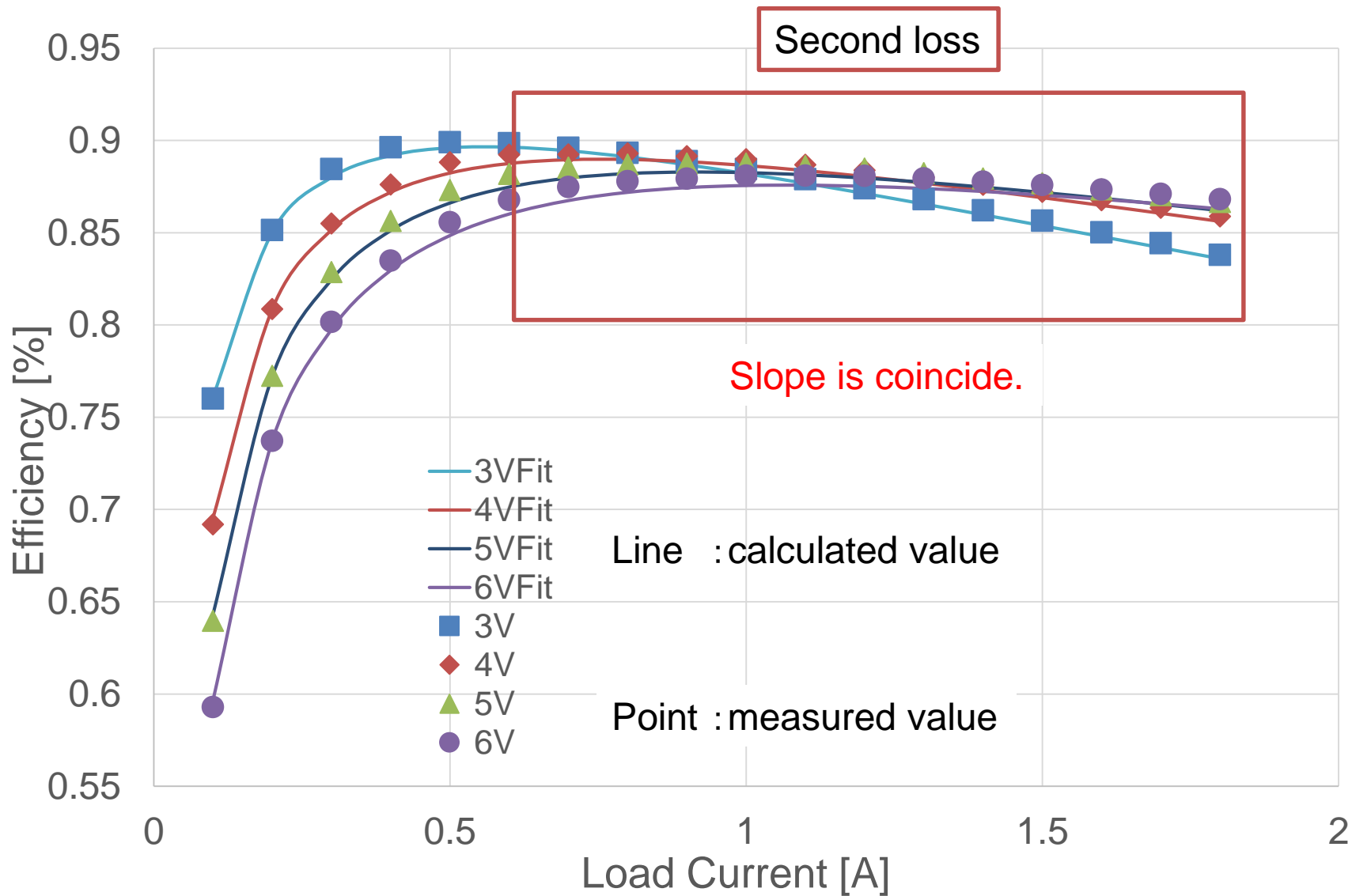
- |  |   |
|--|---|
| <input type="checkbox"/> Inductor ESR                | <input type="checkbox"/> Capacitor ESR              |
| <input type="checkbox"/> High side MOS DC resistance | <input type="checkbox"/> Low side MOS DC resistance |
| <input type="checkbox"/> MOSFET Turn on time         | <input type="checkbox"/> MOSFET Turn off time       |
| <input type="checkbox"/> Constant loss               |   |

## Setting parameter

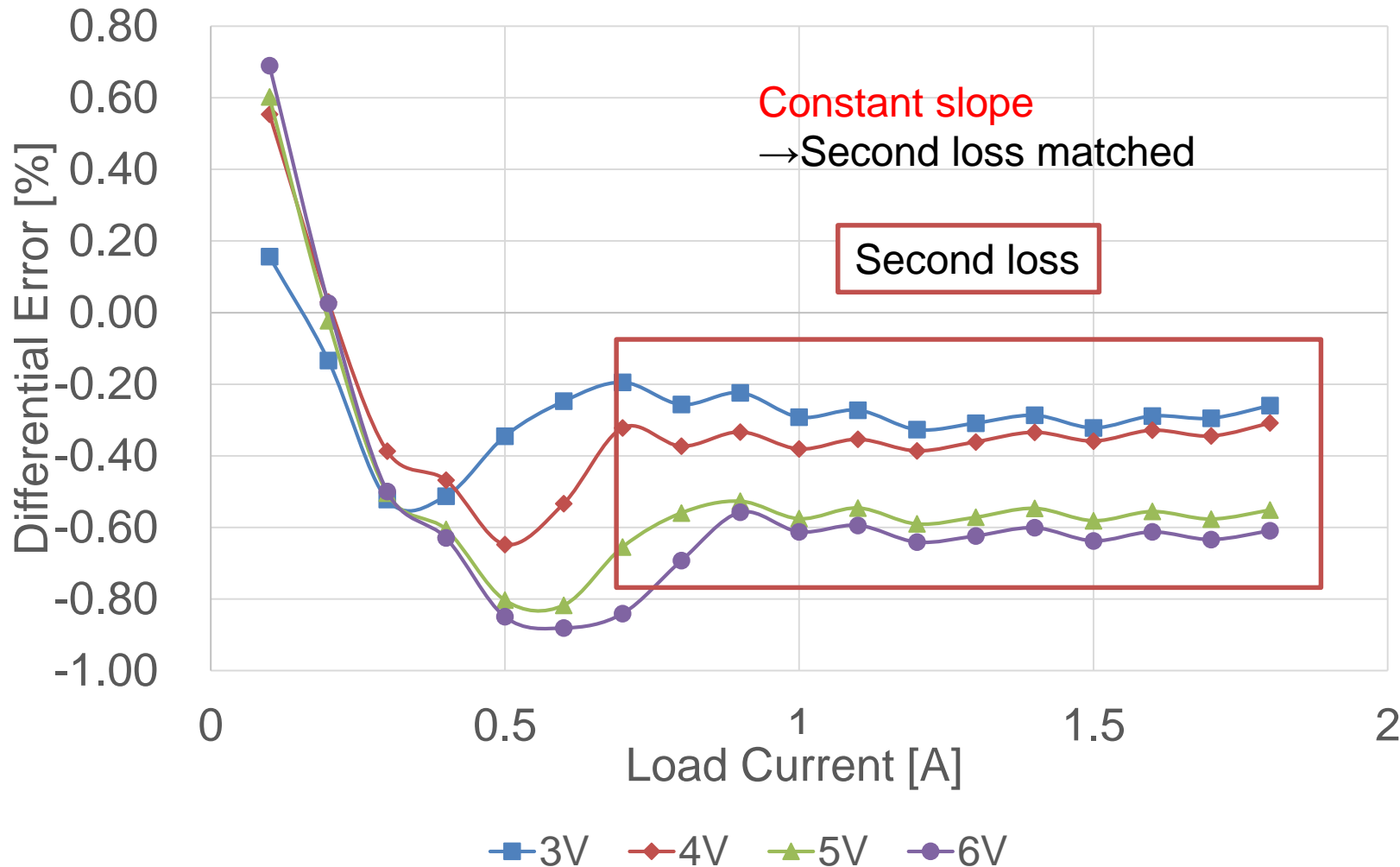
|  |                            |
|--|----------------------------|
| <b>Input Voltage <math>V_i</math></b>          | 3.0V/4.0V/5.0V/6.0V        |
| <b>Output Voltage <math>V_o</math></b>         | 1.8V                       |
| <b>Switching frequency <math>f_{sw}</math></b> | 550kHz                     |
| <b>Inductor <math>L</math></b>                 | 1 $\mu$ H                  |
| <b>Capacitor <math>C</math></b>                | 200 $\mu$ F(100uF*2+1.0nF) |



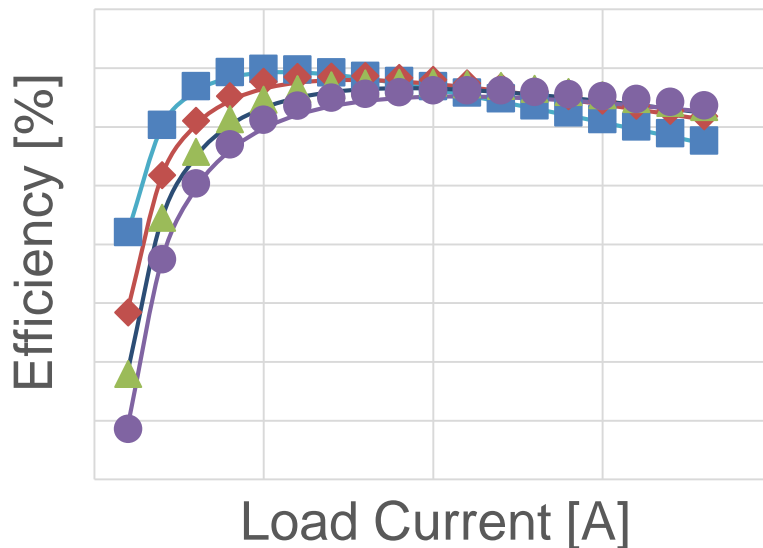
# Fitting Result



# Fitting Result – Error



# Component Value Estimation Result



|                                   |       |
|-----------------------------------|-------|
| Turn-on time of MOSFET $T_{on}$   | 2nsec |
| Turn-off time of MOSFET $T_{off}$ | 4nsec |

## Estimation result

|   |  |
|---|--|
| Inductor ESR                              | 10m $\Omega$   |
| Capacitor ESR                             | 1m $\Omega$  |
| High side ON resistor of MOSFET $R_{ds1}$ | 30m $\Omega$ at 3V<br>20m $\Omega$ at 4V<br>15m $\Omega$ at 5V<br>10m $\Omega$ at 6V |
| Low side ON resistor of MOSFET $R_{ds2}$  | 45m $\Omega$ at 3V<br>30m $\Omega$ at 4V<br>24m $\Omega$ at 5V<br>20m $\Omega$ at 6V |
| Quiescent current of IC $I_{IC}$          | 4.8mA at 3V<br>5.1mA at 4V<br>5.2mA at 5V<br>5.3mA at 6V                             |

# Transfer Function Calculation

Transfer function of power stage is necessary for phase compensation

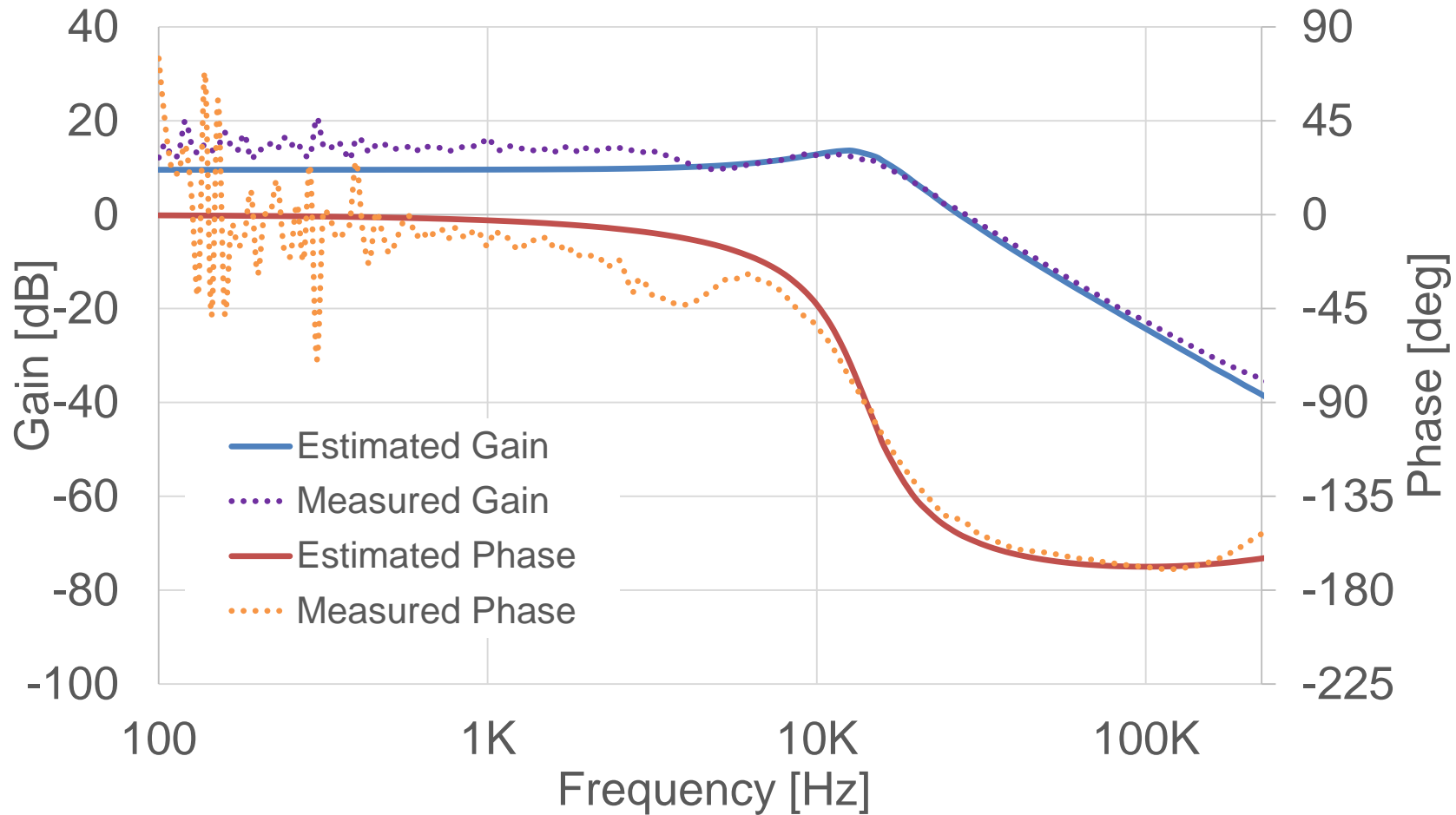


Possible to use estimated values

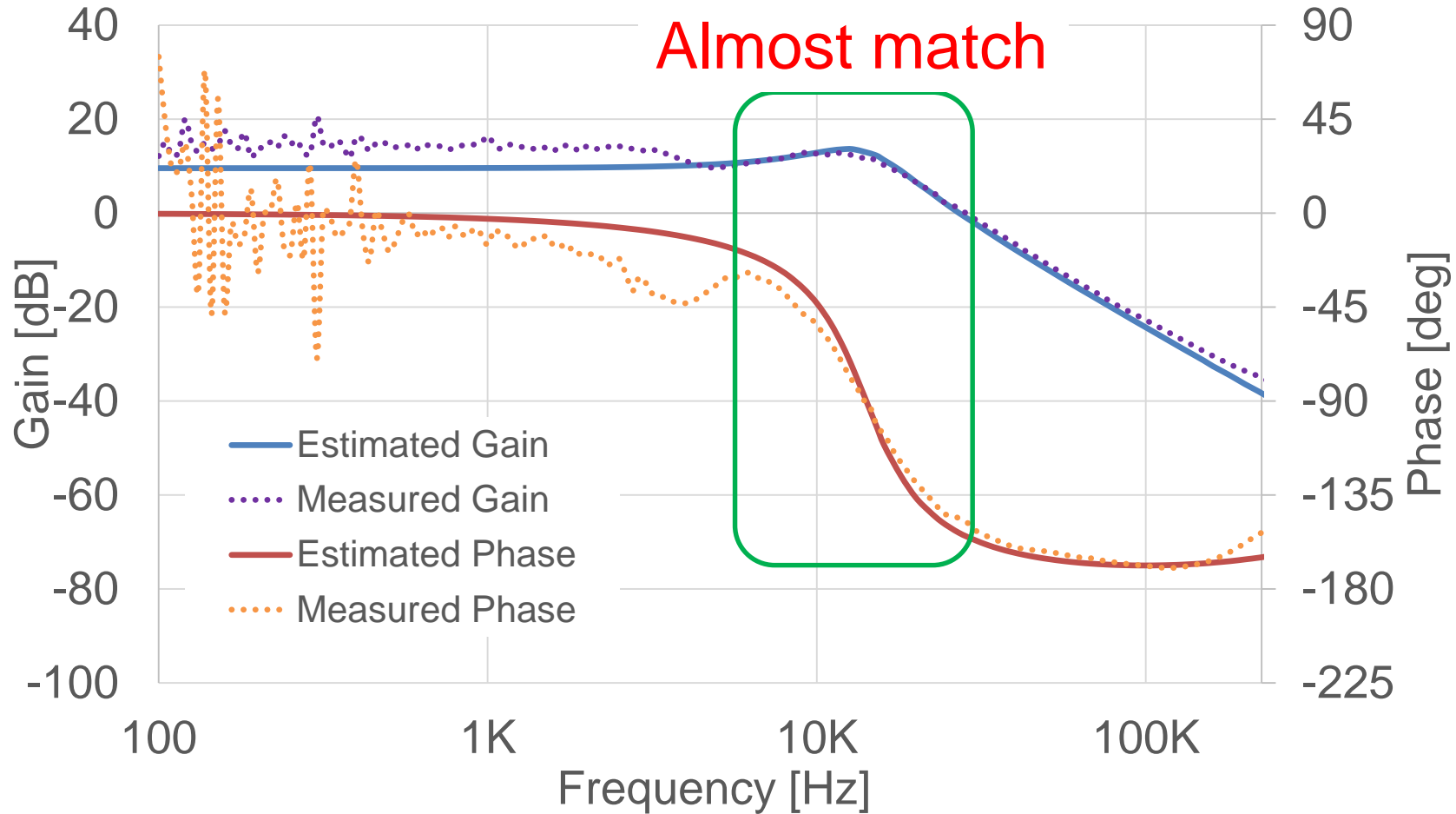
Parameters of  $G_{dv}$  at 3.0V

|  |              |   |              |
|--|--------------|---|--------------|
| Switching Frequency $f_{sw}$             | 550kHz       | Input Voltage $V_i$                     | 3.0V         |
| Inductor $L$                             | 0.8 $\mu$ H  | Capacitor $C$                           | 160 $\mu$ F  |
| Inductor ESR $r_L$                       | 10m $\Omega$ | Capacitor ESR $r_C$                     | 1m $\Omega$  |
| High side MOSFET DC resistance $r_{ds1}$ | 30m $\Omega$ | Low side MOSFET DC resistance $r_{ds2}$ | 45m $\Omega$ |

# Transfer Function Comparison



# Transfer Function Comparison



**Estimation result can be used  
for phase compensation**

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- Proposed a method to derive DC-DC converter component values from measured efficiency curve.
- Calculated the transfer function of power stage using estimation result.
- Measured and estimated results are well matched.



# Future Research

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- More experiment for validation
- Design of phase compensation using estimation result.
- More accurate fitting  
incorporate losses not considered.

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# Back Up

# Power stage transfer function

Power stage transfer function at open loop

$$G_{dv}(s) \Big|_{\substack{\Delta V_i=0 \\ \Delta I_o=0}} = \frac{\Delta V_o}{\Delta D} = \frac{V_i \cdot \omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \left( 1 + \frac{s}{\omega_{esr}} \right)$$

$$= \frac{V_i(1 + j\omega C r_c)}{1 - \omega^2 LC + j\omega C(r_L + r_c + r_{ds})}$$

$$\zeta = \frac{r_L + r_c + r_{ds}}{2} \sqrt{\frac{C}{L}}, \quad \omega_n = \frac{1}{\sqrt{LC}}, \quad \omega_{esr} = \frac{1}{C r_c}$$

Parameter of  $G_{dv}$  at 3.0V

|  |              |   |              |
|--|--------------|---|--------------|
| Switching Frequency $f_{sw}$             | 550kHz       | Input Voltage $V_i$                     | 3.0V         |
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| Inductor ESR $r_L$                       | 10m $\Omega$ | Capacitor ESR $r_c$                     | 1m $\Omega$  |
| High side MOSFET DC resistance $r_{ds1}$ | 30m $\Omega$ | Low side MOSFET DC resistance $r_{ds2}$ | 45m $\Omega$ |