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## Operational Amplifier Stability Research

### Research Objective

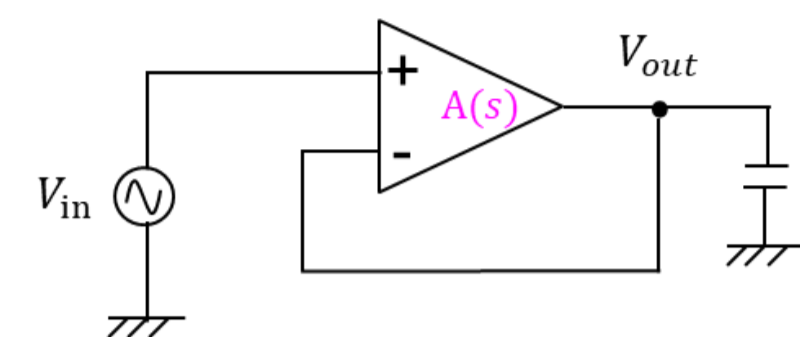
#### Problem

Difficult to get open loop characteristics

#### Our target

Provide an easy-to-use tool to obtain the open loop characteristics from the closed loop operation results

#### Approach



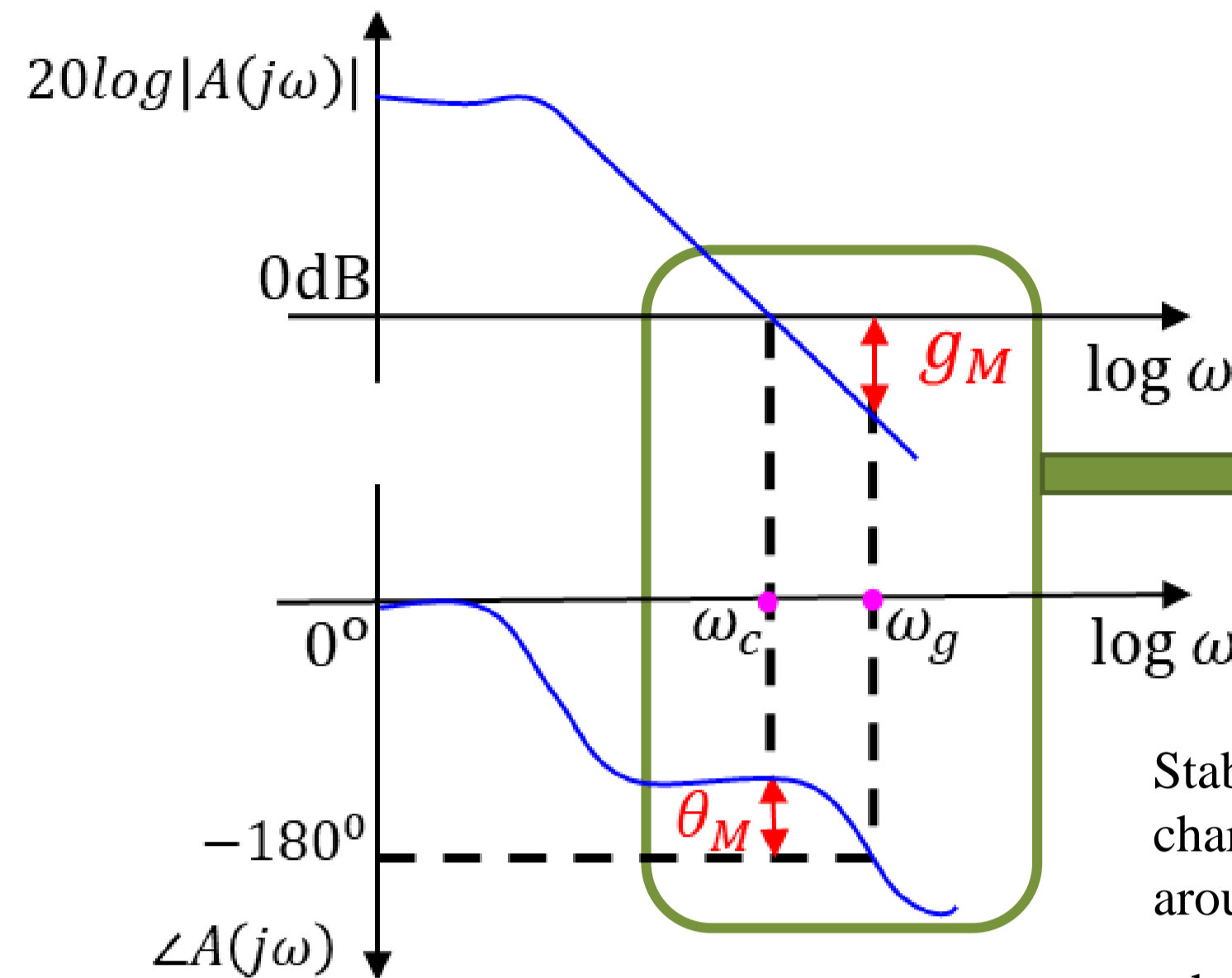
$$\frac{V_{out}}{V_{in}} = W(s) = \frac{A(s)}{1 + A(s)}$$

Closed loop characteristics

$$A(s) = \frac{W(s)}{1 - W(s)}$$

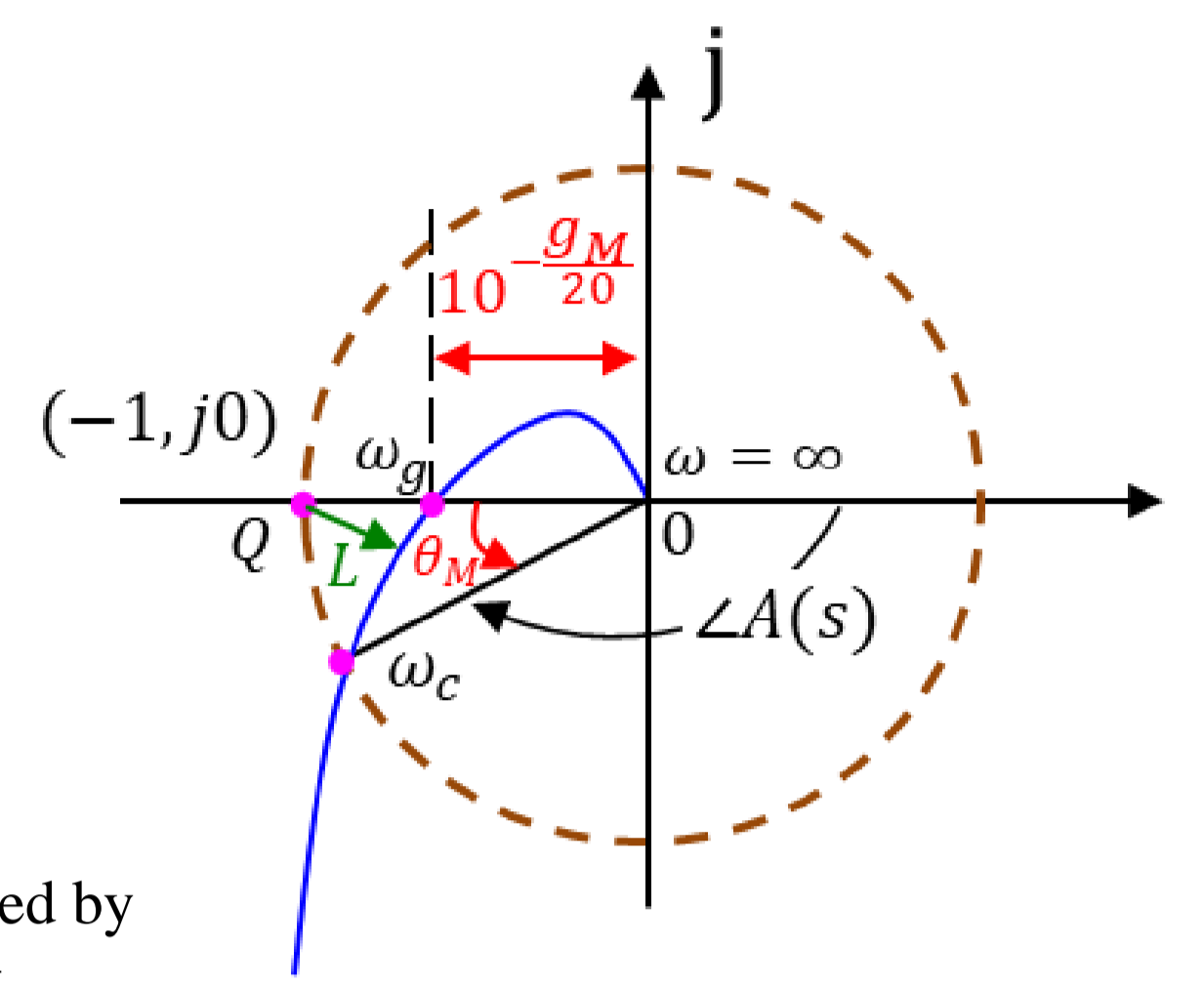
Open loop characteristics

### Bode Plot



Stability is defined by characteristics at around the unit circle, where  $|A(s)|$  is small

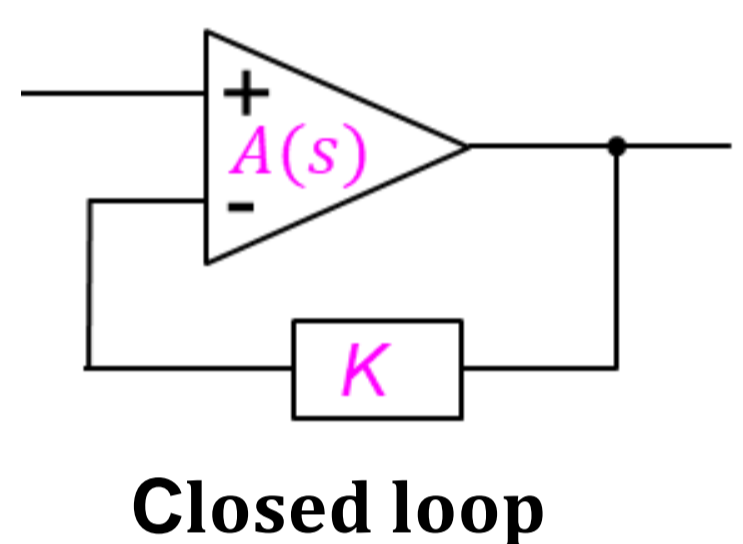
### Nyquist Plot



L: minimum distance to point -1

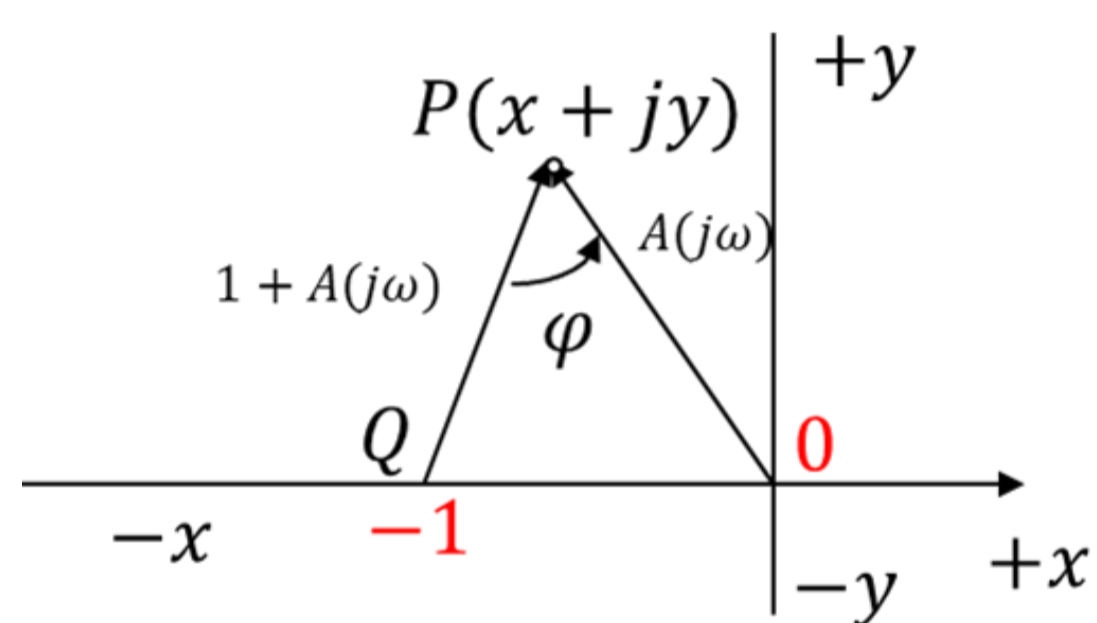
$g_M$ : gain margin  $\theta_M$ : phase margin

## Closed loop $M \cdot \varphi$ locus in open loop Nyquist



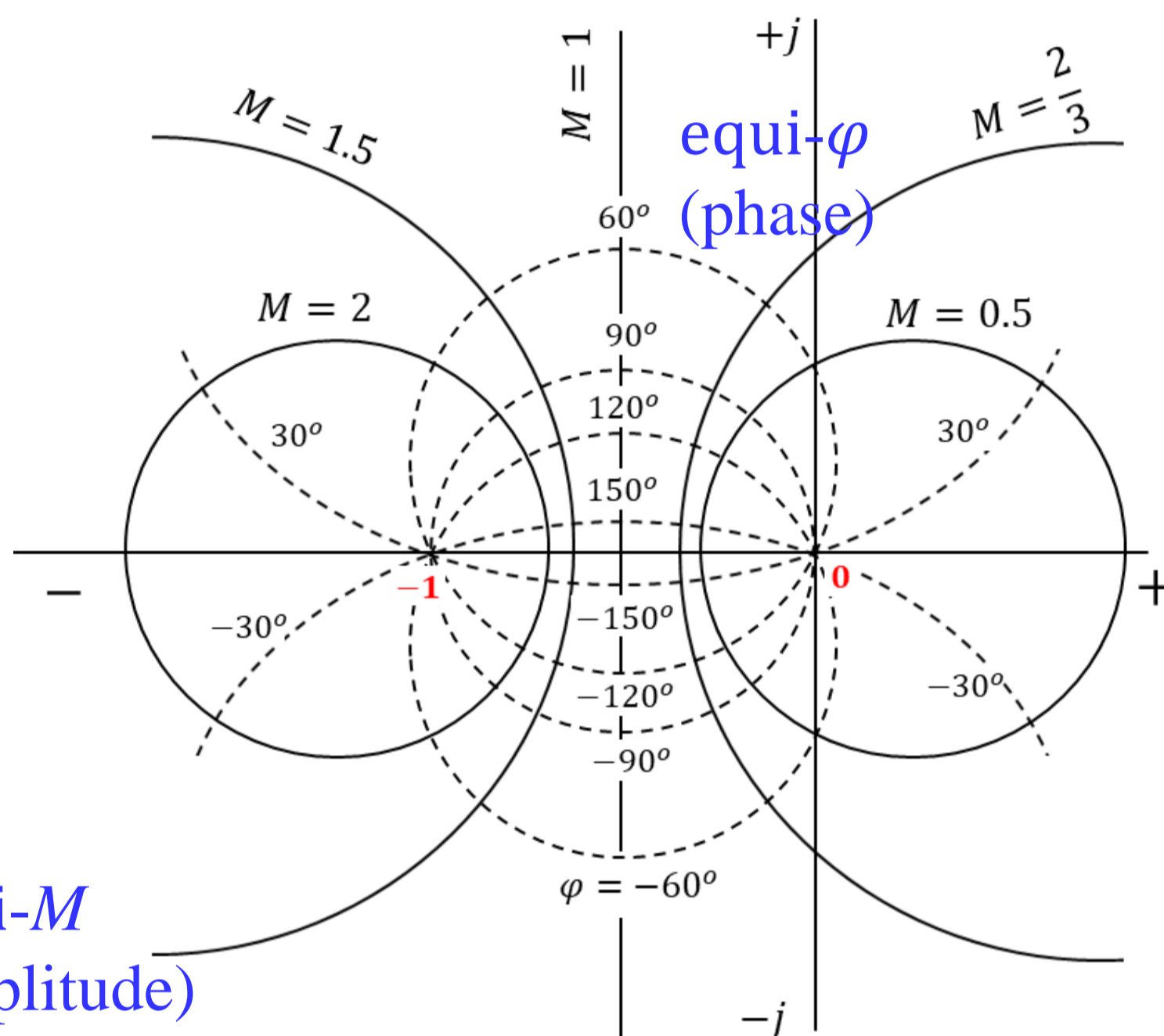
Closed loop

Buffer connection condition:  $K=1$



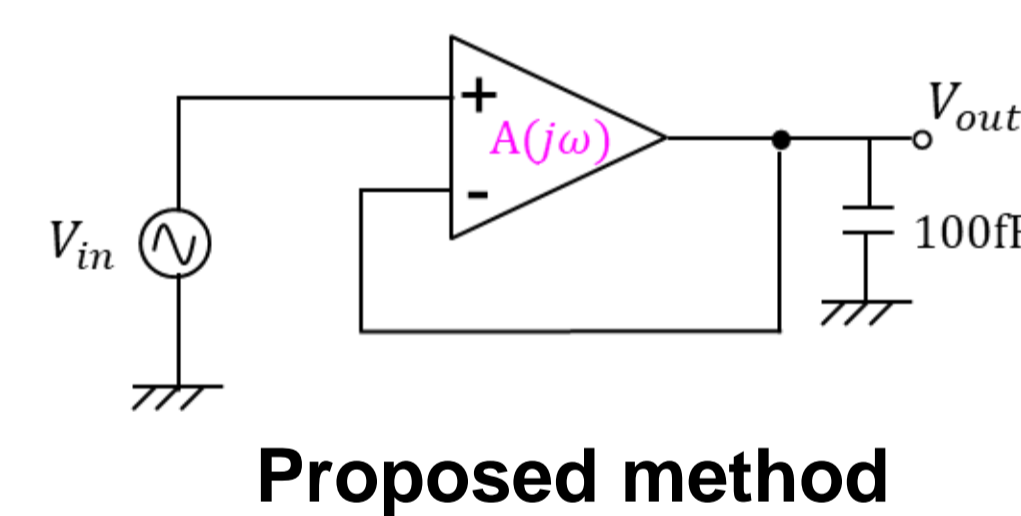
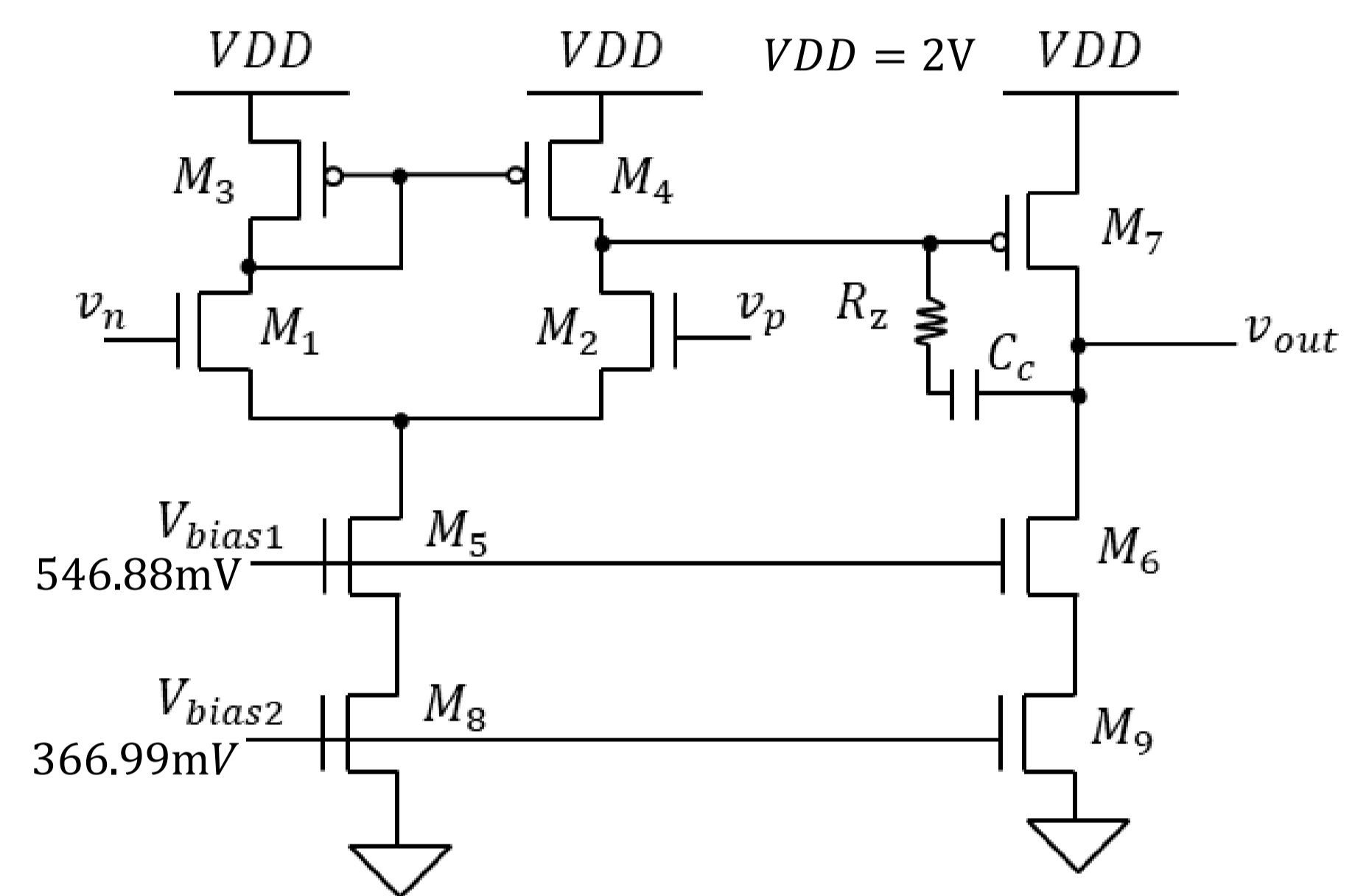
Nyquist plane of open loop transfer function  $A(j\omega)$

$$\overline{OP}: A(j\omega) \quad \overline{QP}: 1 + A(j\omega)$$

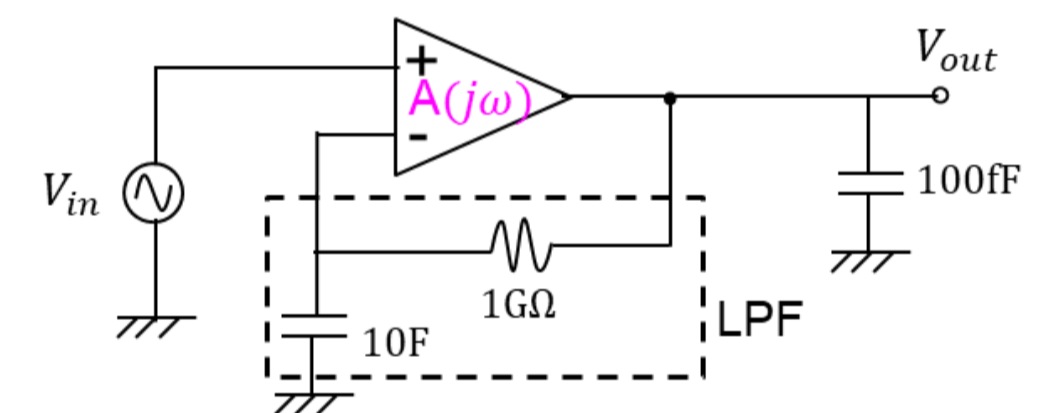


equi-φ (phase)  
equi-M (amplitude)

## Operational amplifier



Proposed method



LPF(Low pass filter) method

closed loop transfer function:

$$W(j\omega) = \frac{A(j\omega)}{1 + 1 * A(j\omega)} = \frac{\overline{OP}}{\overline{QP}} = M e^{j\varphi}$$

$$M = \frac{|\overline{OP}|}{|\overline{QP}|}, \varphi = \angle QPO \quad M^2 = \frac{|\overline{OP}|^2}{|\overline{QP}|^2} = \frac{x^2 + y^2}{(x+1)^2 + y^2}$$

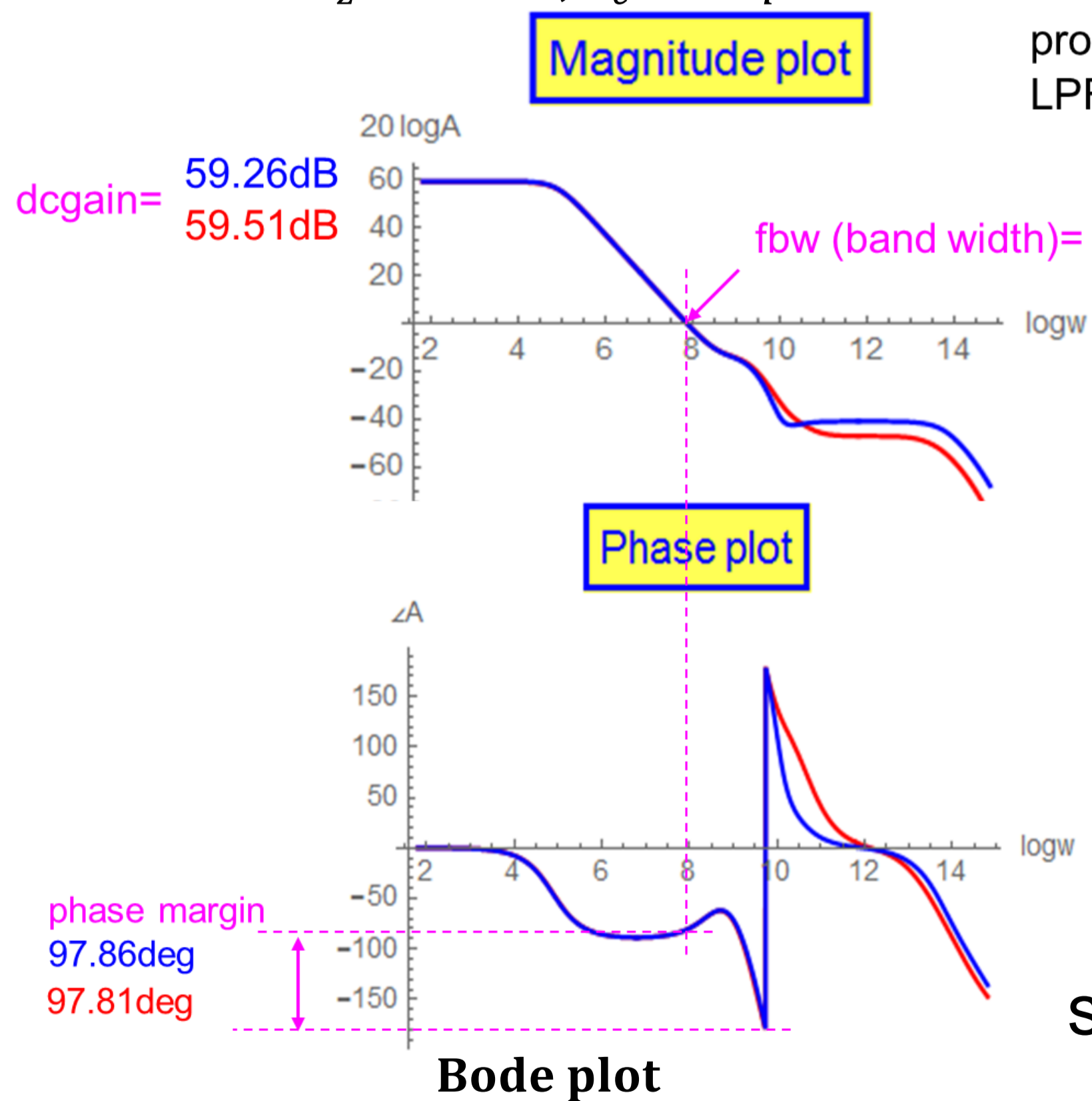
Equation of circumference

$$\left\{x + \frac{M^2}{M^2 - 1}\right\}^2 + y^2 = \left(\frac{M}{M^2 - 1}\right)^2$$

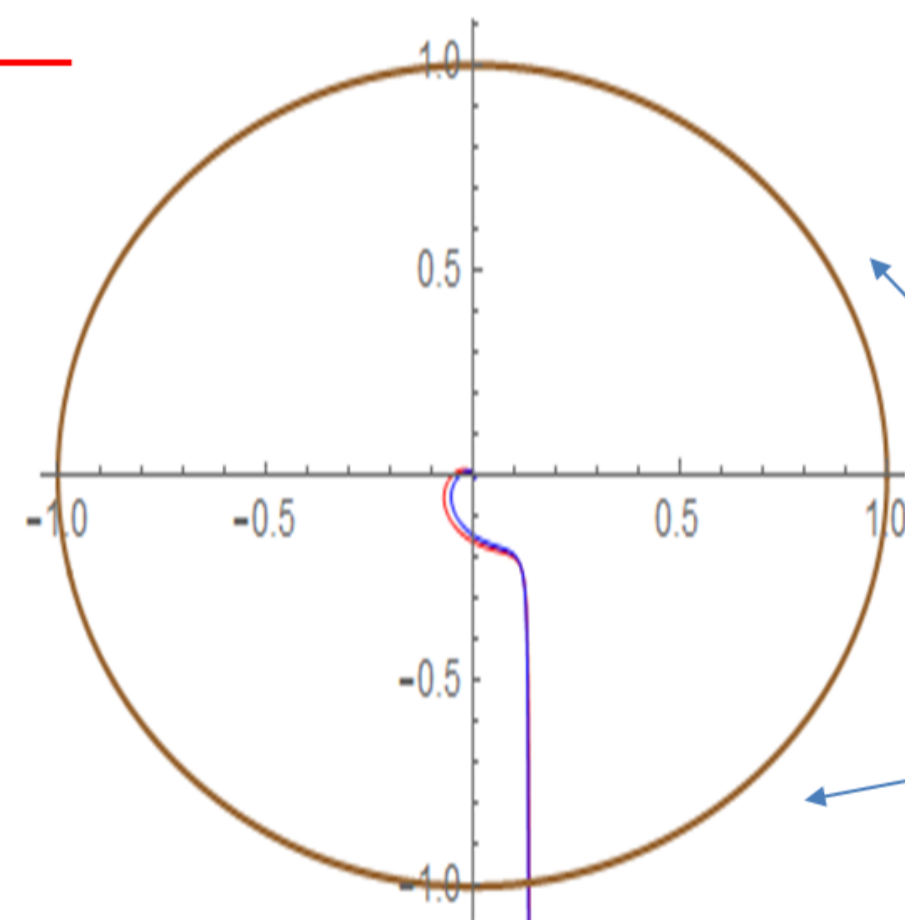
By using different axes on the same complex plane, closed loop and open loop characteristics become a single plot.

## Simulation Result

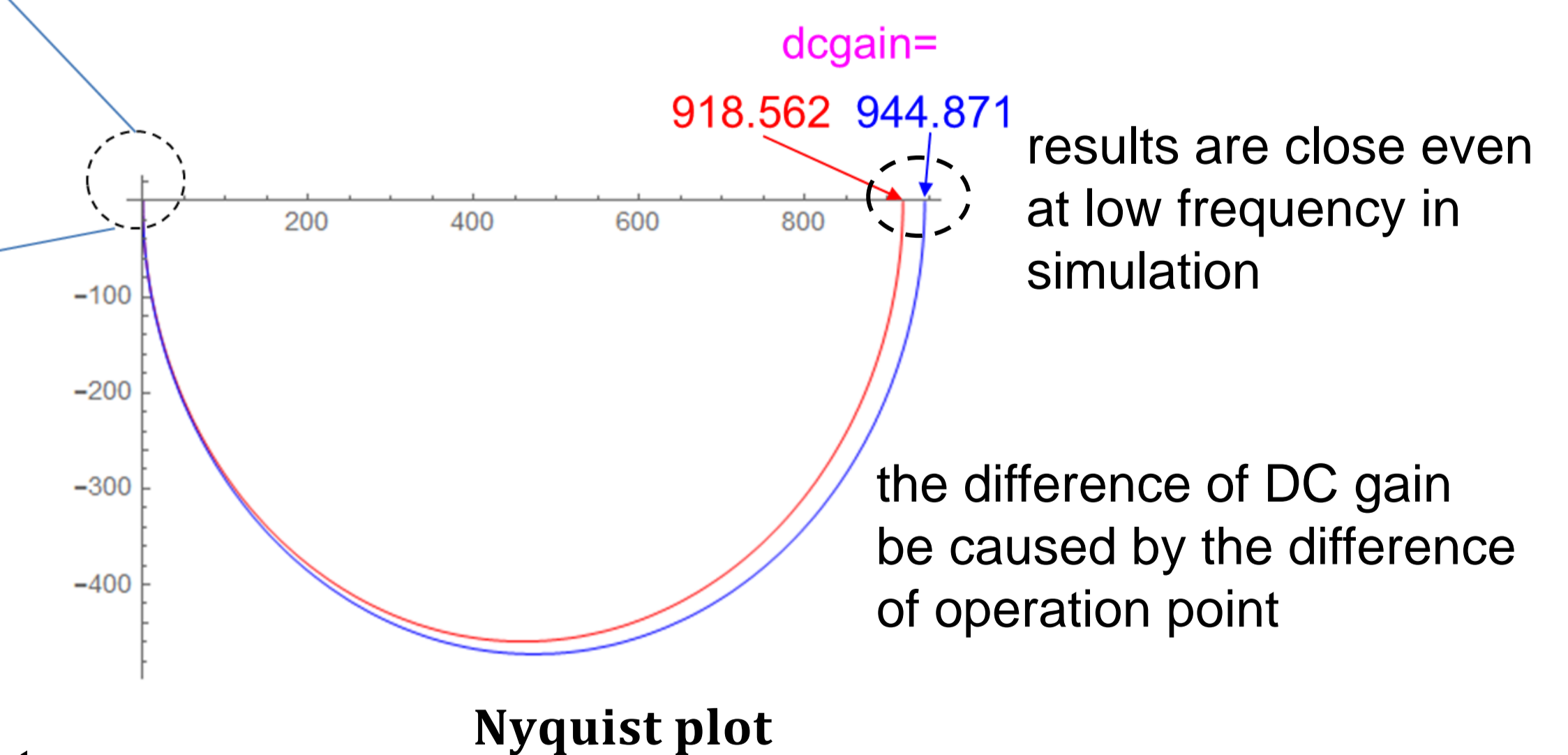
Condition  $R_z = 6.5K\Omega, C_c = 2.4pF$



Bode plot



simulation results are consistent



Nyquist plot

the difference of DC gain be caused by the difference of operation point

## Conclusion

- Tried the conversion method for obtain the open loop characteristics (opamp stability etc.) from closed loop operation results
- The effectiveness of this method be shown by practical example

### Future work

- Apply to more other practical examples
- Provide an easy-to-use tool for anyone