

Design Consideration for LC Analog Filters: Inductor ESR Compensation, Mutual Inductance Effect and Variable Center Frequency

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Rohm Semiconductor



OUTLINE

- Research Background
- Approach
 - Inductor ESR Compensation
 - Application to LC BPF
 - Application to LC BEF
 - Application to Variable Inductor Realization
- Conclusion

OUTLINE

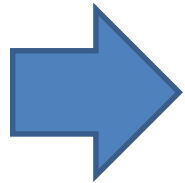
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Research Background

Analog/mixed-signal IC testing systems

- Low distortion sine wave generation
- Total Harmonic Distortion (THD) measurement

Key components



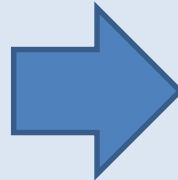
Analog Band Pass Filter (BPF)
and Band Elimination Filter (BEF)

Using dedicated devices

Superior performance

Very costly


Using standard discrete components

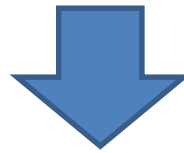


Reasonable

Research Objective

Using inductors on shelf

 Realization of $\left\{ \begin{array}{l} \text{low cost} \\ \text{good performance} \end{array} \right\}$ LC BPF, BEF



For this purpose

Inductor ESR compensation technique

ESR: Equivalent Series Resistance



Parasitic mutual inductor effects, Countermeasure

- Variable inductor realization
- Variable center frequency BPF, BEF

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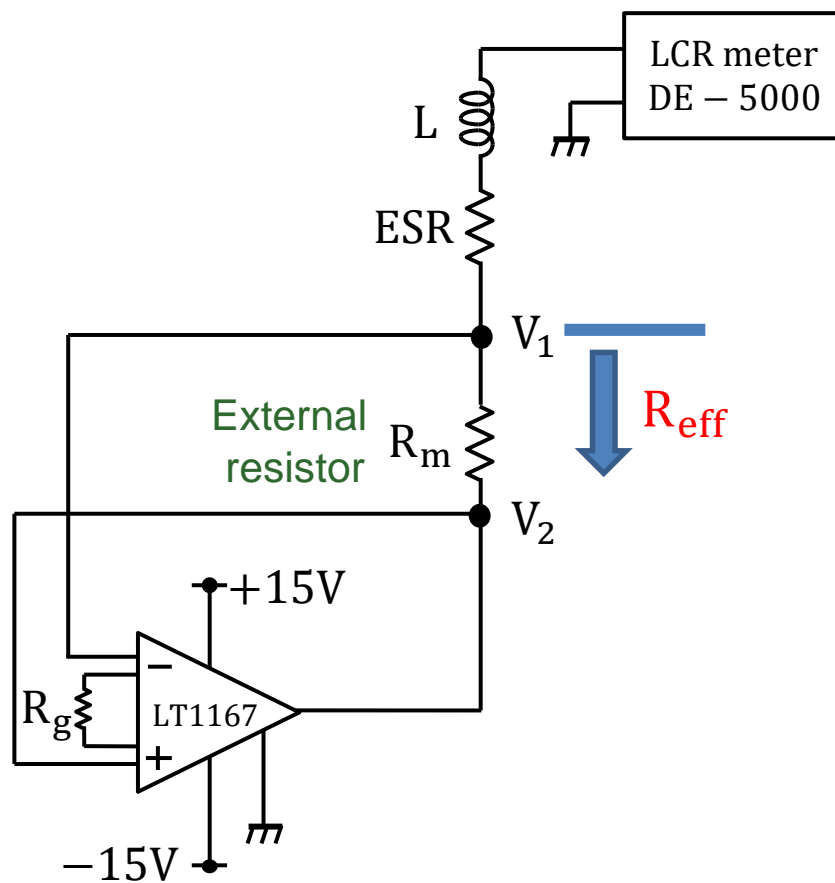
Approach

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Inductor ESR Compensation



Gain G \rightarrow Controllable by resistor R_g

$$V_2 = G(V_2 - V_1)$$

$$R_m I = V_1 - V_2 = \frac{V_2}{1 - G}$$

Effective resistor from node V_1

$$R_{eff} = \frac{V_1}{I} = (1 - G)R_m$$

$$R_{eff} < 0 \text{ for } G > 1$$

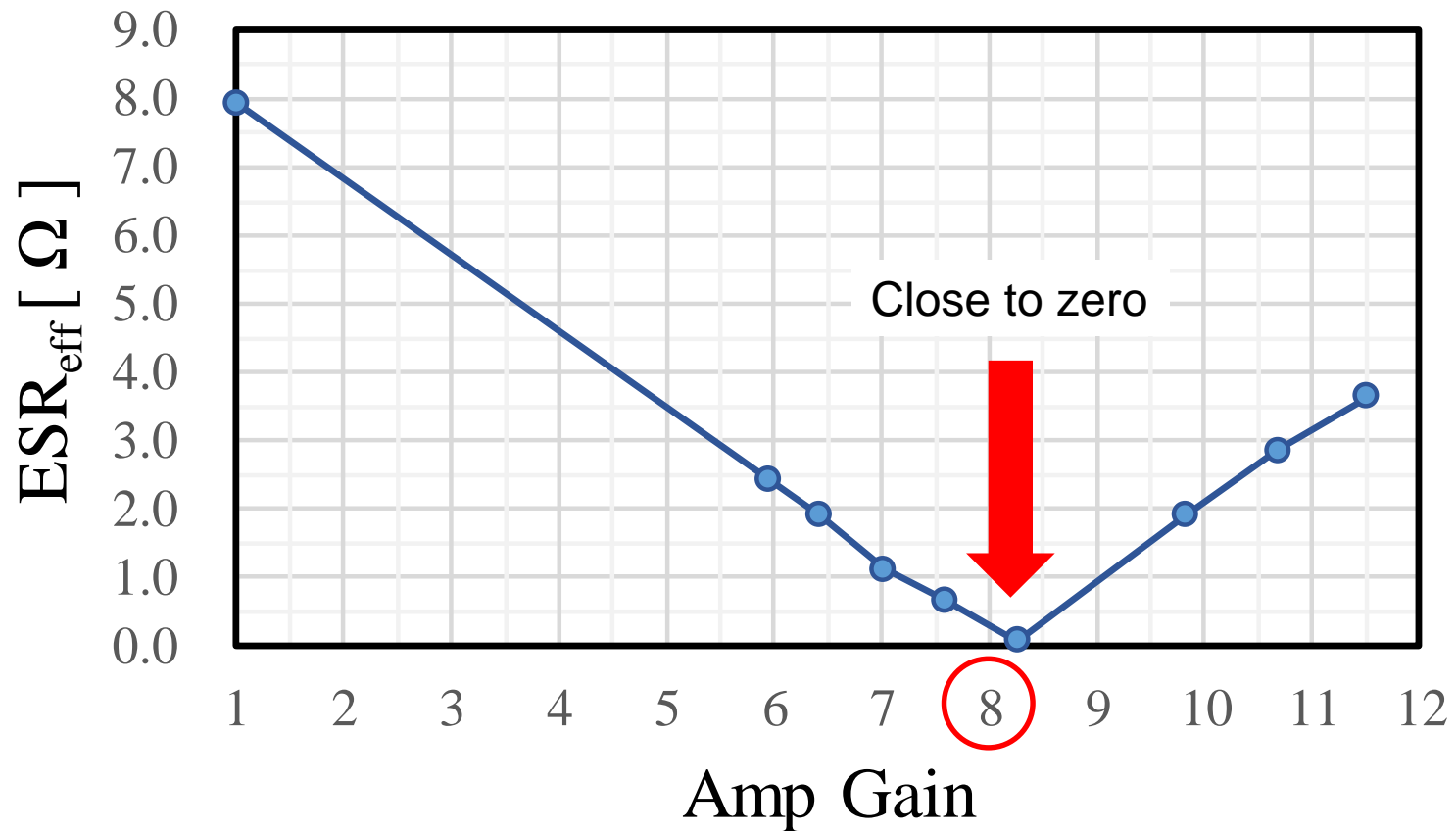
Effective ESR

$$ESR_{eff} = ESR + R_{eff} \rightarrow 0$$

By adjusting G ,
negative effective resistance R_{eff}
 cancels ESR.

Measurement Verification

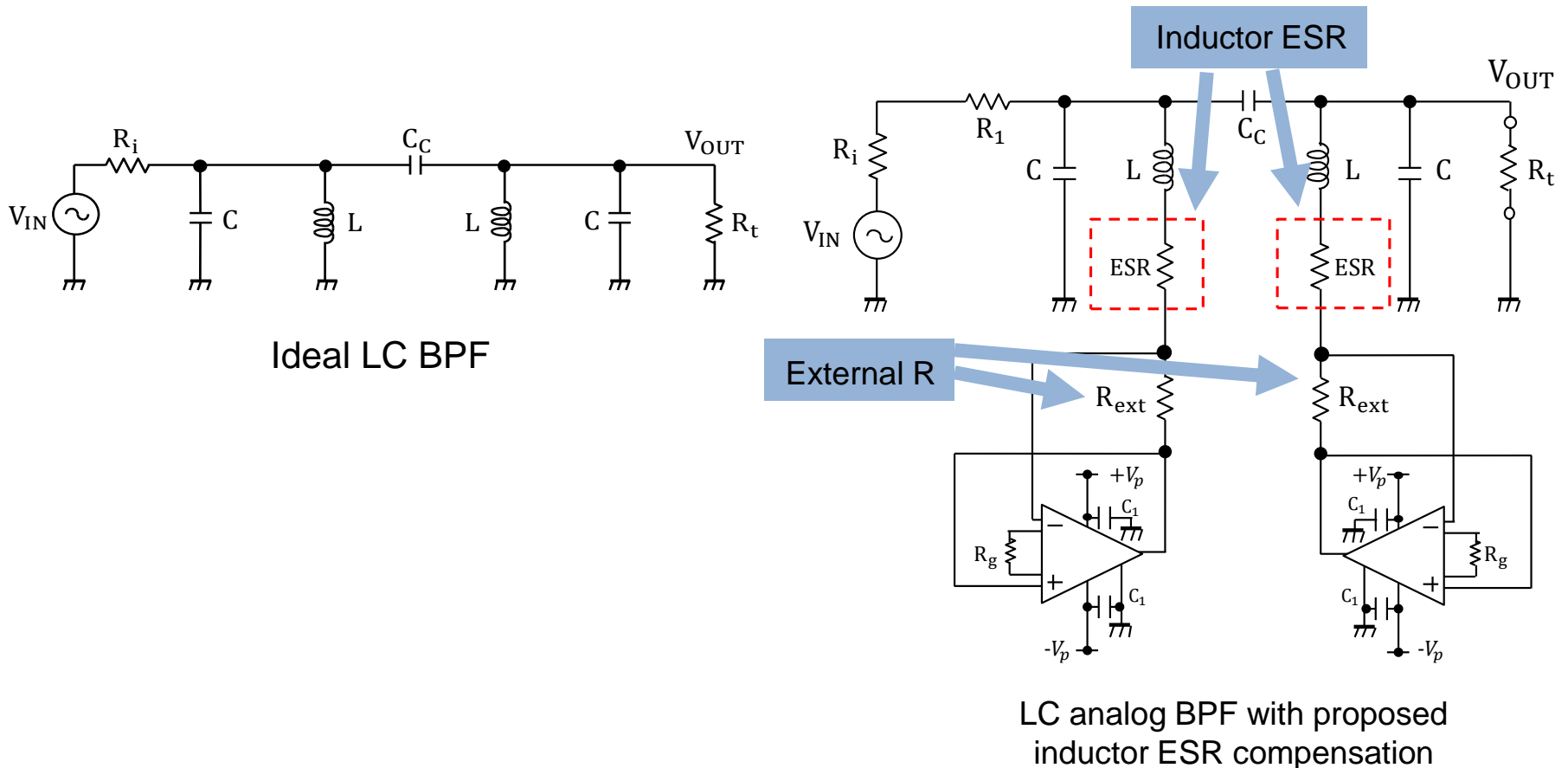
Proposed inductor ESR compensation measured result



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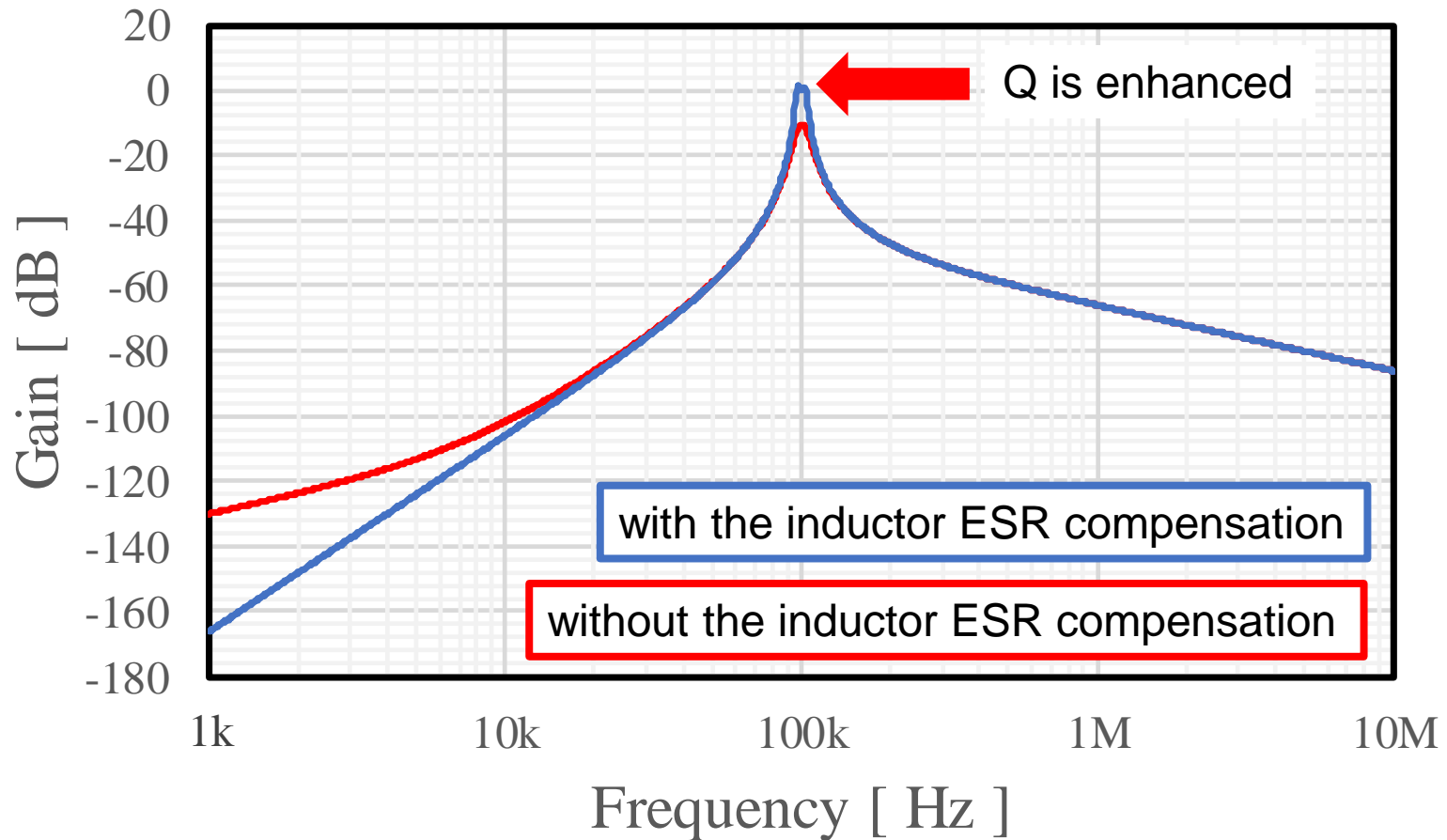
Application to LC BPF



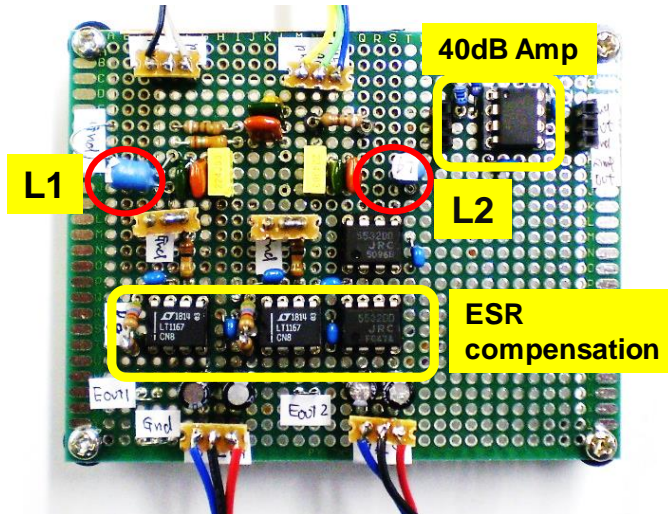
Transfer function of an ideal LC BPF

$$G(s) = \frac{s^3 R_t L^2 C_C}{s^4 R_i R_t L^2 C (2C_C + C) + s^3 L^2 (C + C_C) (R_i + R_t) + s^2 L \{ 2R_i R_t (C_C + C) + L \} + sL (R_i + R_t) + R_i R_t}$$

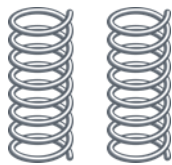
Simulation Verification



Measurement Result of BPF Prototype



LC BPF prototype
with ESR compensation

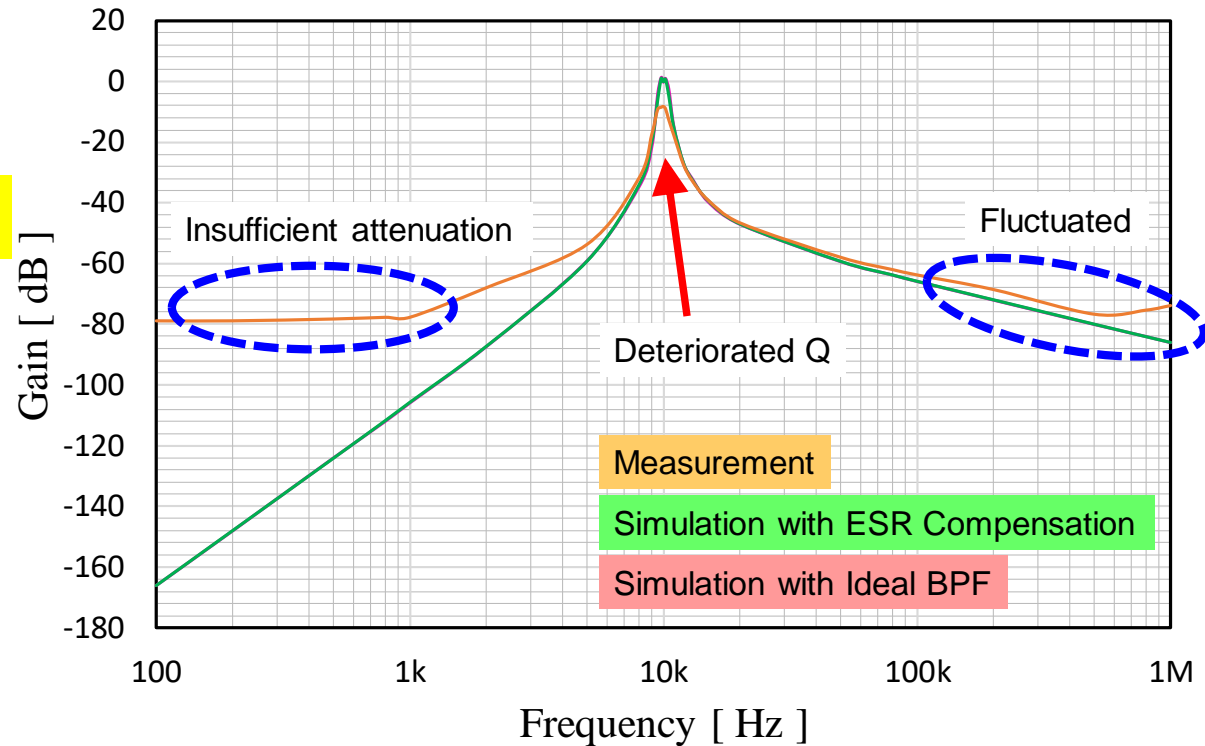


L_1 , L_2 are placed in parallel



Parasitic mutual conductance

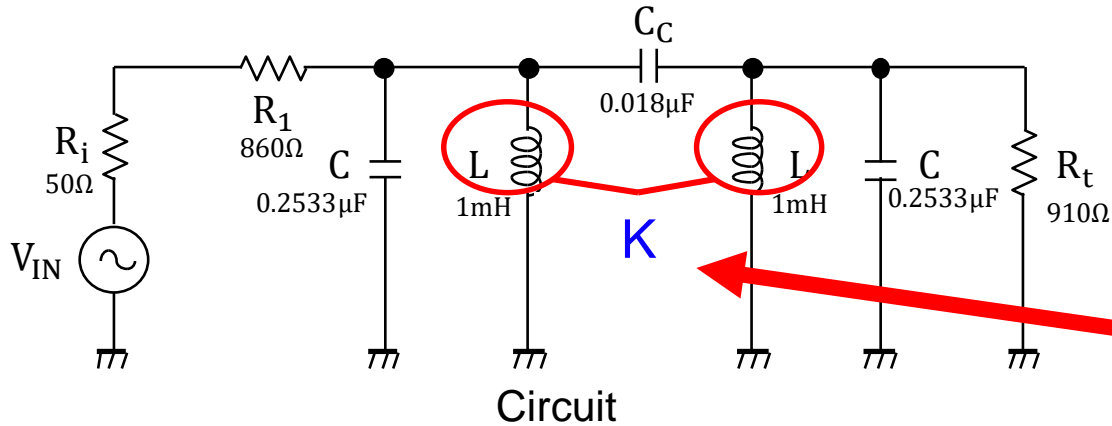
Simulation and measurement result
of BPF with ESR compensation,



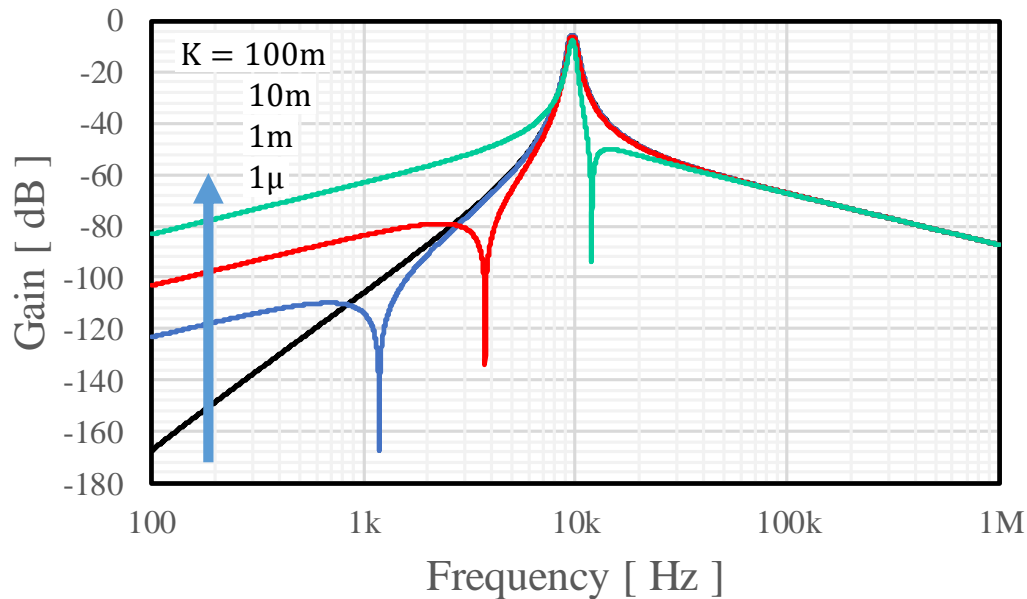
Discrepancies

Effect of Coupling Coefficient K

Simulation of mutual inductance effect



Coupling coefficient



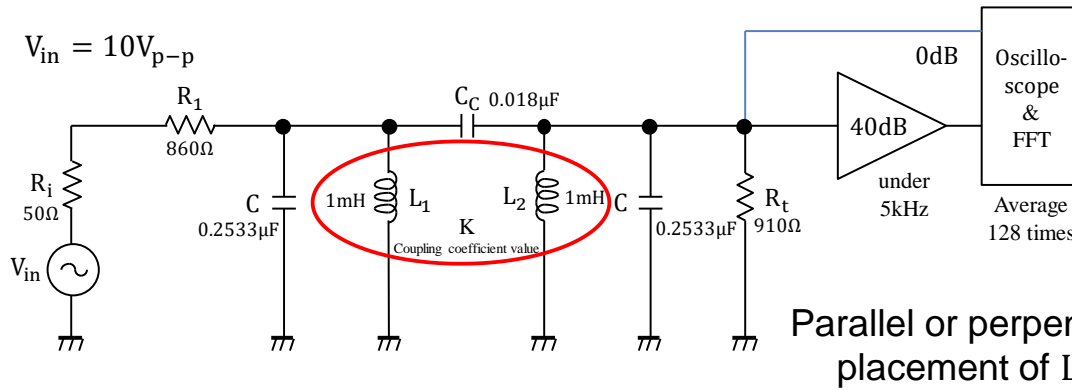
K increases



Stop band attenuation
in low frequency side
becomes **worse**.

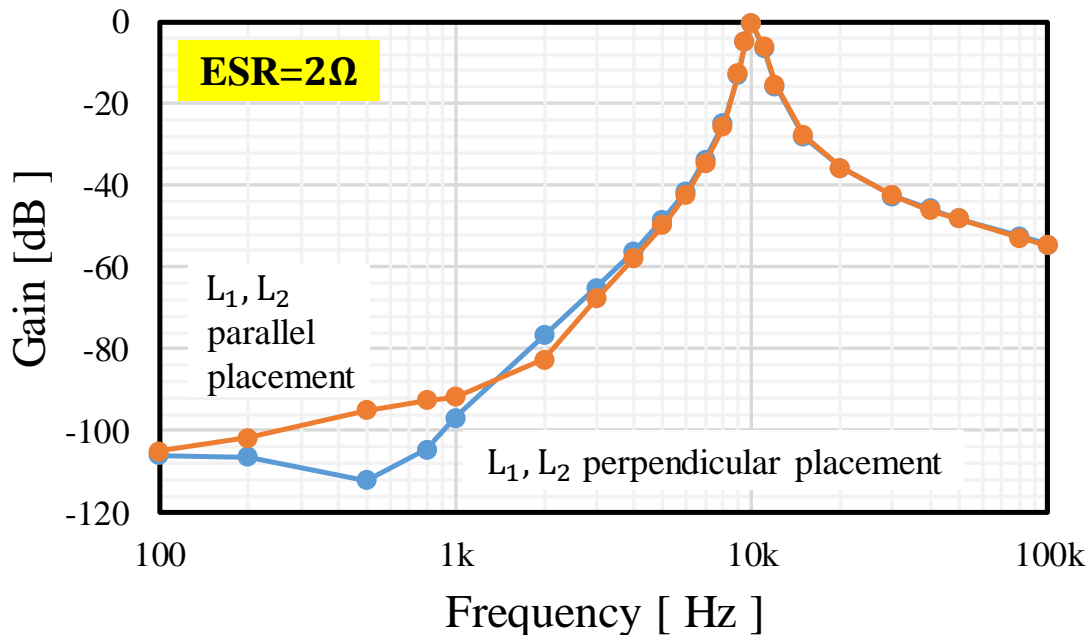
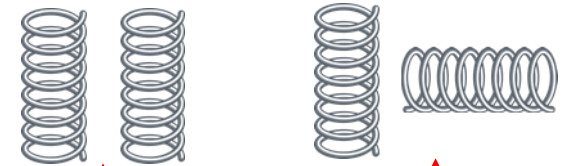
L_1, L_2 Parallel or Perpendicular Placement

BPF measurement result



For accurate measurements in stopband,

- Amplifier of 40 dB gain under 5kHz
- 128 times averaging



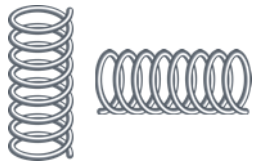
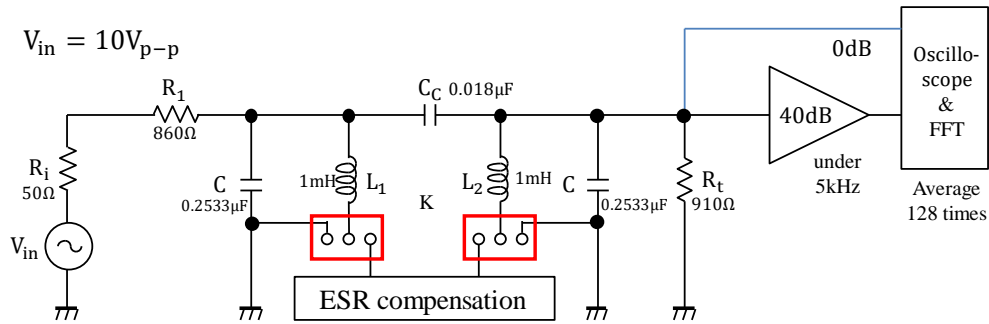
L_1, L_2 are placed in perpendicular

Mutual inductance reduction

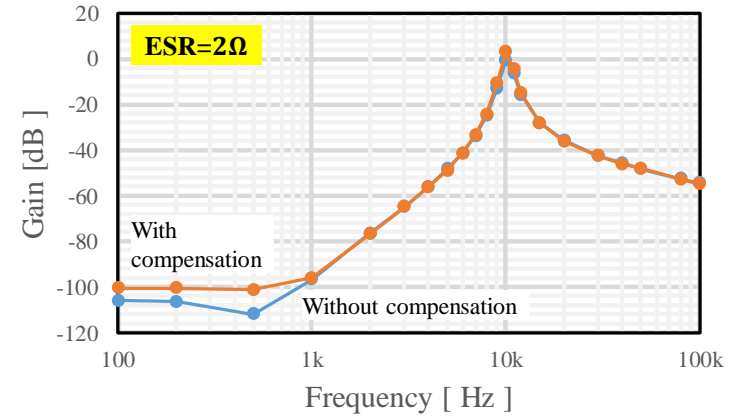
Stop band attenuation

Improved

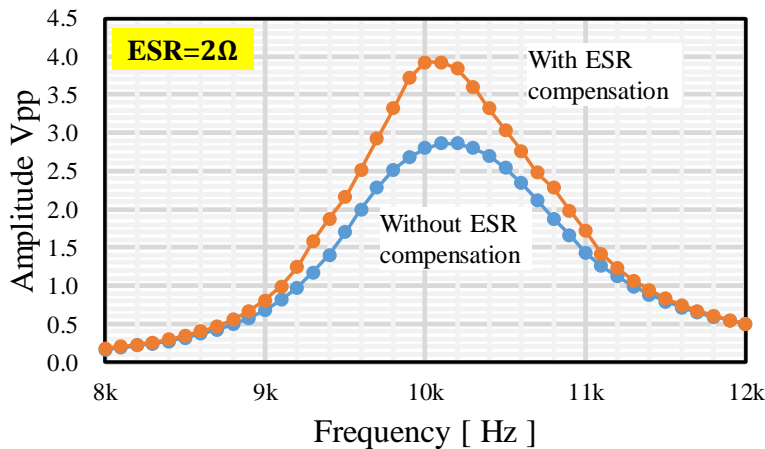
Measurement of 2nd BPF Prototype



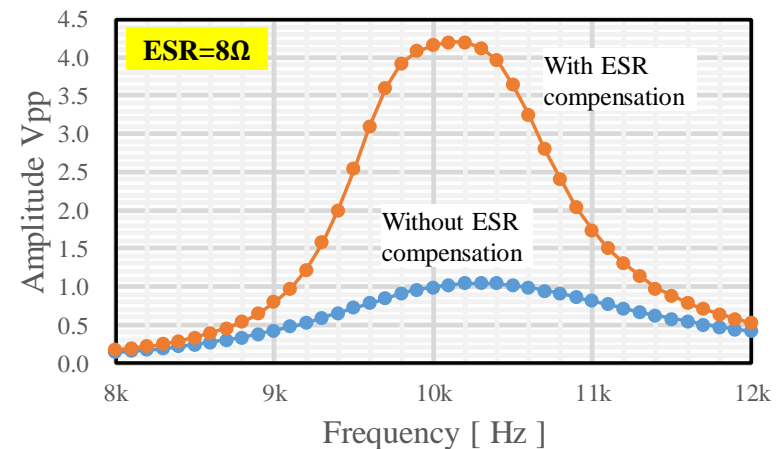
Perpendicular placement
of L_1, L_2



Measured result with ESR of 2Ω



Enlarged with ESR of 2Ω



Enlarged with ESR of 8Ω

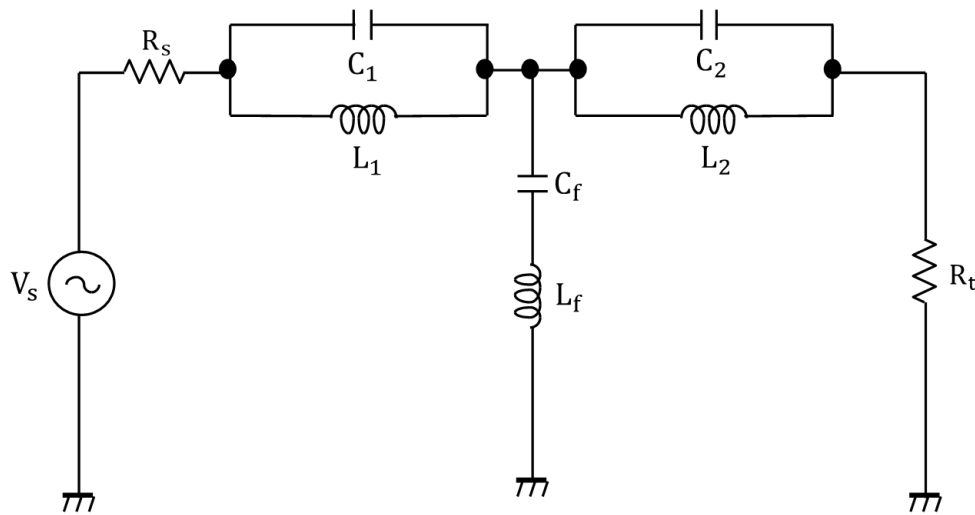
Q is enhanced

OUTLINE

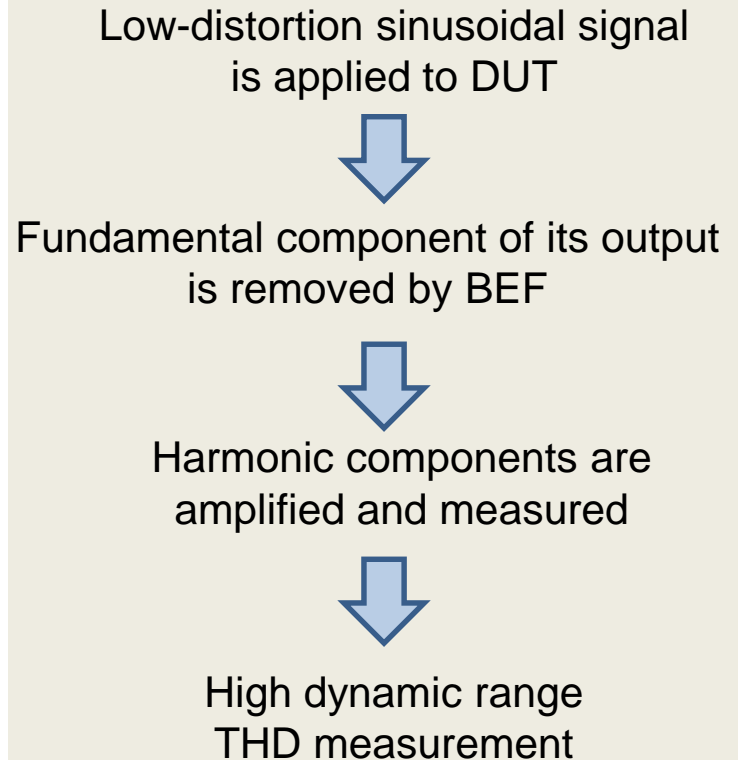
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Application to LC BEF

BEF for THD measurement



LC BEF circuit

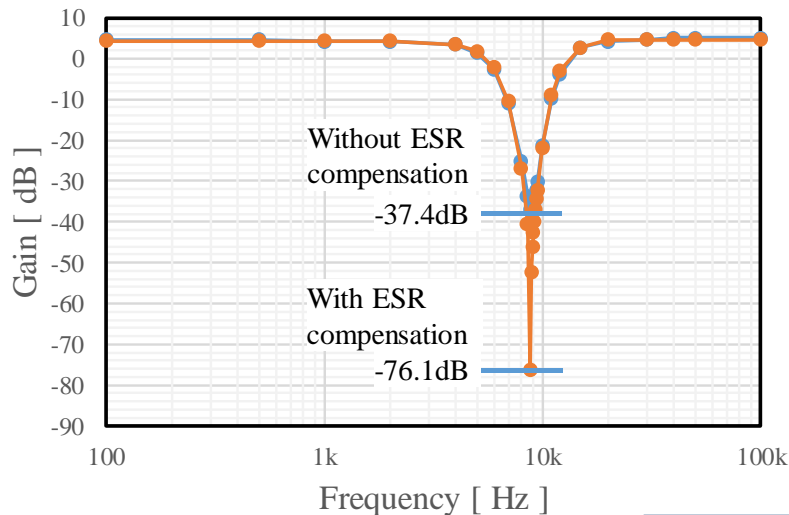
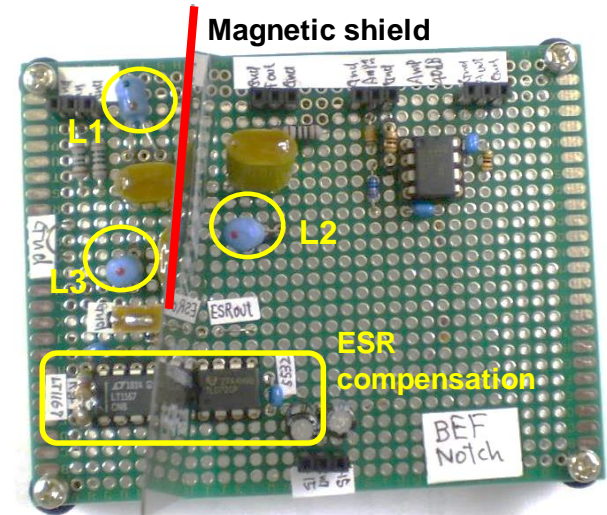
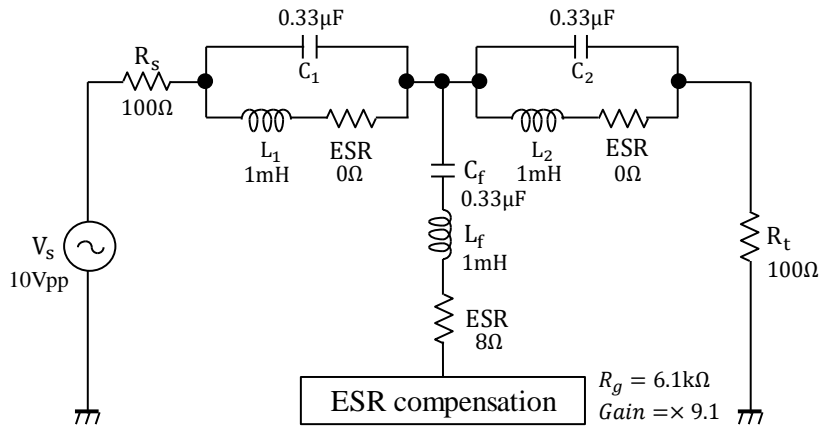


Transfer function

$$G(s) = \frac{(s^2 L_1 C_1 + 1)(s^2 L_f C_f + 1)(s^2 R_t L_2 C_2 + R_t)}{(s^2 R_s L_1 C_1 + s L_1 + R_s) \{ (s^2 L_f C_f + 1)(s^2 L_2 C_2 + 1) + s C_f (s^2 R_t L_2 C_2 + s L_2 + R_t) \} + (s^2 L_1 C_1 + 1)(s^2 L_f C_f + 1)(s^2 R_t L_2 C_2 + s L_2 + R_t)}$$

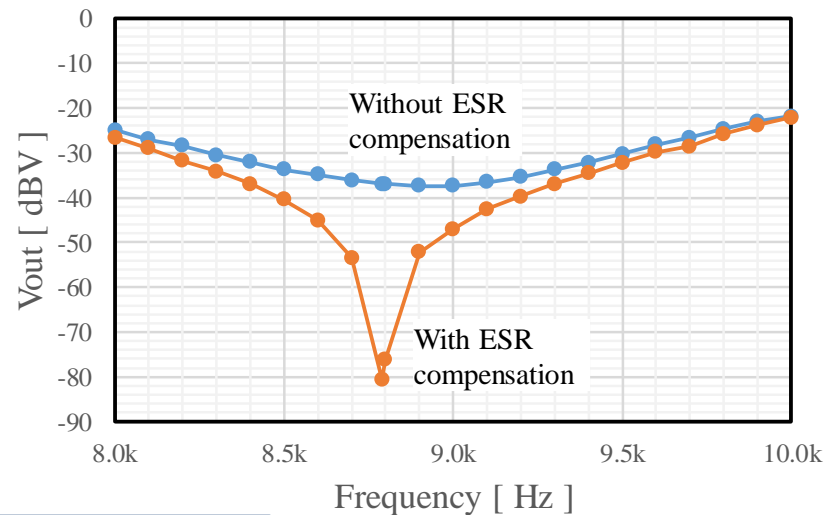
BEF Prototype with Inductor ESR Compensation

BEF with inductor ESR compensation



Measured result

Notch → sharper

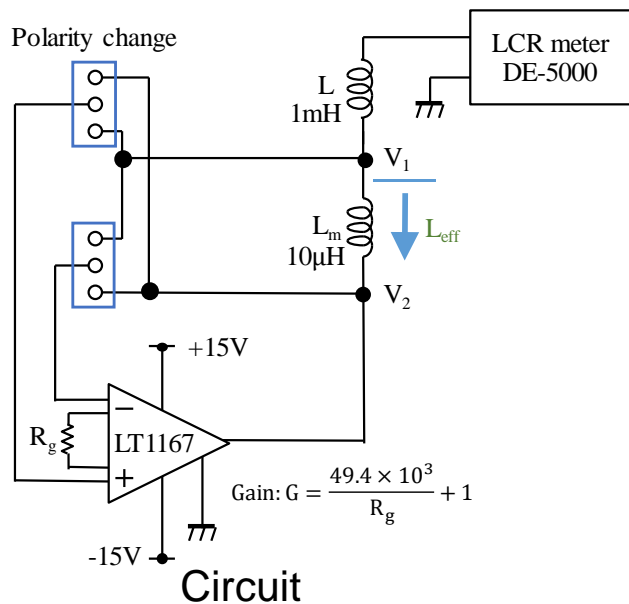


Enlarged

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Application to Variable Inductor Realization



$$V_2 = G(V_2 - V_1), \quad j\omega L_m I = V_1 - V_2 = V_1 / (1 - G)$$

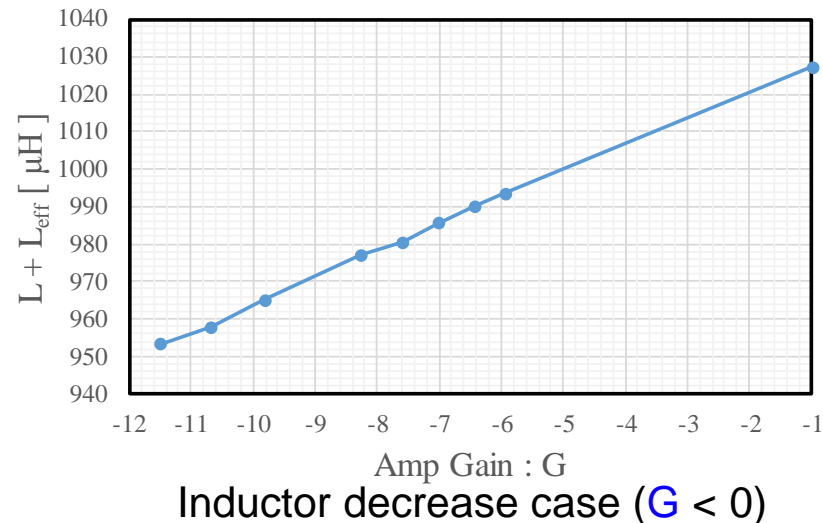
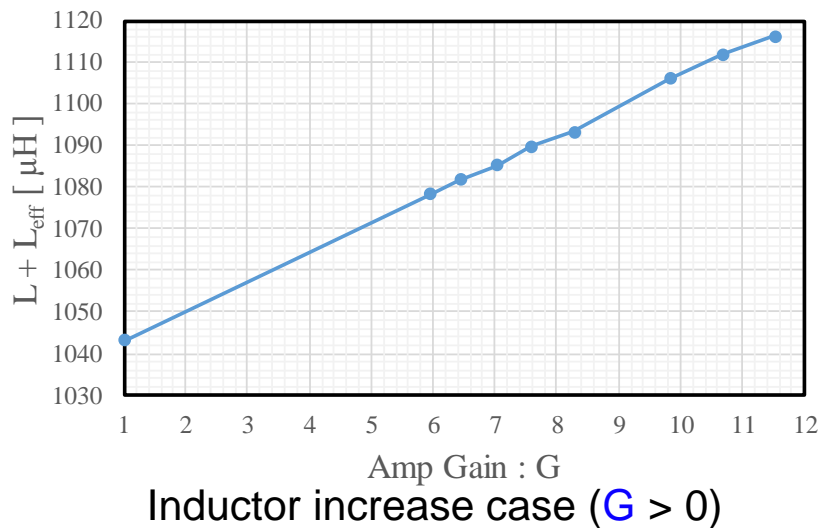
Effective inductor from node V_1 :

$$L_{\text{eff}} = V_1 / (j\omega I) = (1 - G)L_m$$

G can be positive or negative by polarity switch

Total inductor $L_{\text{total}} = L_{\text{eff}} + L$

Measured results with polarity switch change



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Conclusion

For low-cost analog/mixed-signal test systems

- Analog LC BPF and BEF
 - Inductor ESR compensation for high Q
 - Variable center frequency
 - Parasitic mutual inductance effects
 - ➔ Placement of inductors
- Verification with circuit simulation and experiments

Thank you for listening !